

# Systematic design of advanced control structures

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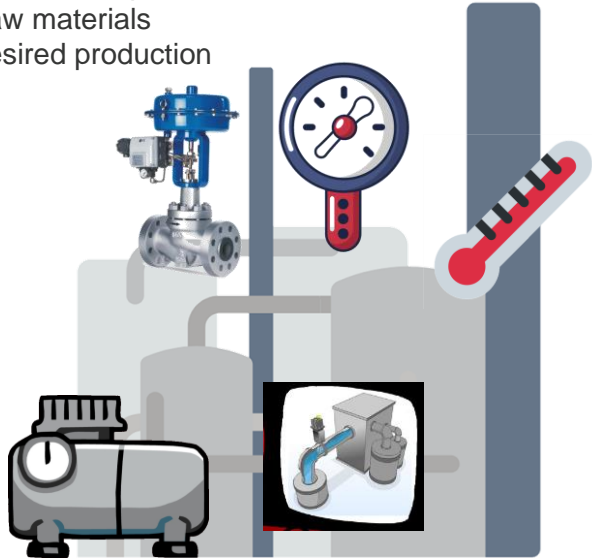
# Content

- Motivation and scope
- Active constraint switching with advanced control structures (chapter 2)
  - Case study: mixing
  - Case study: distillation column
  - Case study: cooling cycle (chapter 3)
  - Case study: cooler (chapter 4)
- MV to MV constraint switching
  - Split range control
    - Design of standard split range controllers (chapter 5)
    - Generalized split range controller (chapter 6)
  - Multiple controllers with different setpoints (chapter 7)
- Improved PI control for tank level (chapter 8)
- Conclusions

# Motivation and scope

## DV: disturbance variable ( $d$ )

- Ambient temperature
- Raw materials
- Desired production



## CV: controlled variable (output, $y$ )

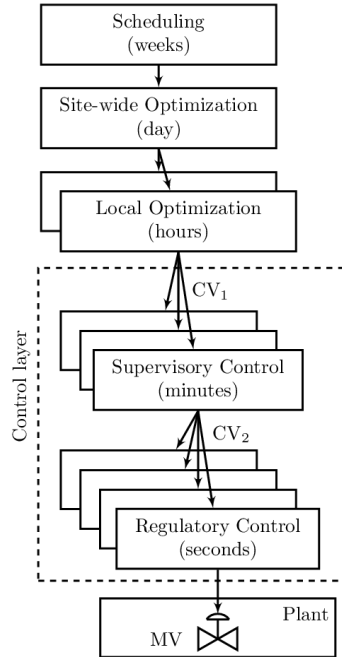
- Temperature
- Pressure
- Concentration

## MV: manipulated variable (input, $u$ )

- Valve opening
- Compressor rotational speed



# Motivation and scope



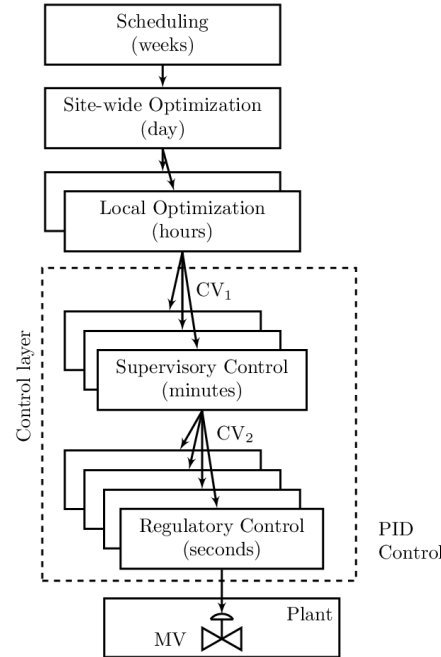
## Top-down analysis:

S1-S4: Identify steady-state optimal operation

## Bottom-up analysis:

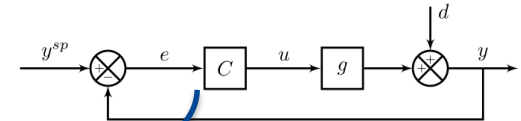
S5-S7: Design control structure

# Motivation and scope



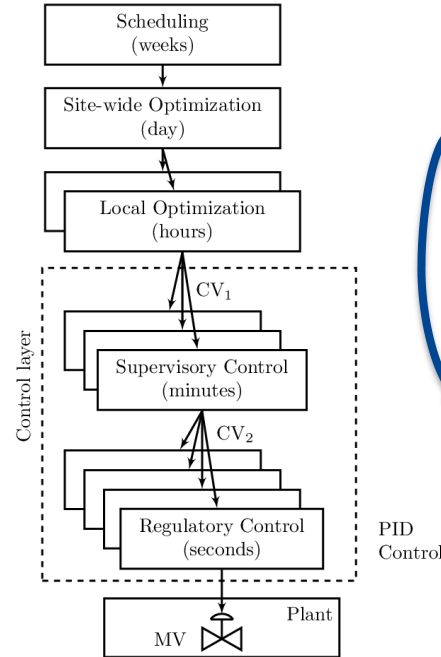
## Bottom-up analysis:

- S5: regulatory control layer
- S6: supervisory control layer
- S7: online optimization layer



$$u(t) = u^0 + K_C \left( e(t) + \frac{1}{\tau_I} \int_0^t e(t) + \tau_d \frac{de(t)}{dt} \right)$$

# Motivation and scope



Bottom-up analysis:

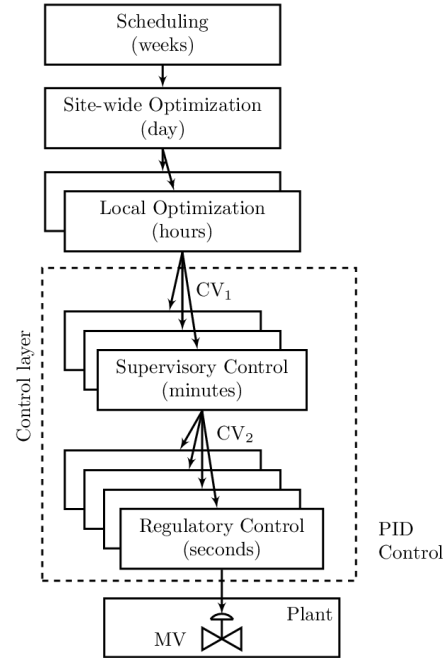
S5: regulatory control layer

**S6: supervisory control layer**

S7: online optimization layer

Keeps operation  
in the right  
active constraint region

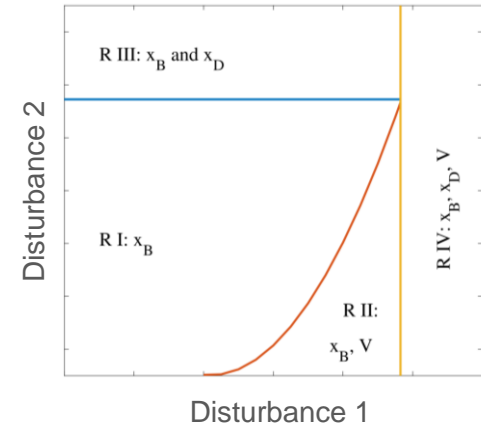
# Motivation and scope



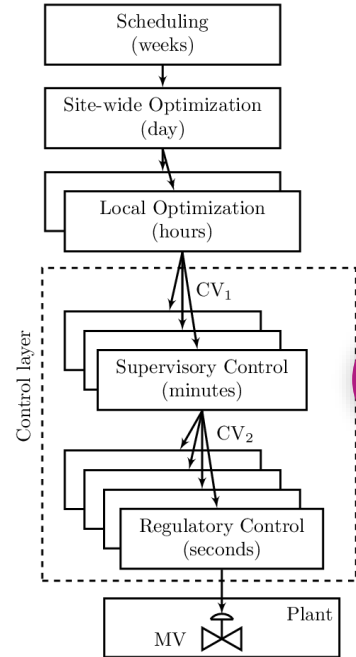
## S6: supervisory control layer

### Constraint region

«region in the disturbance space defined by which constraints are active within it»



# Motivation and scope



MPC or Advanced Control Structures

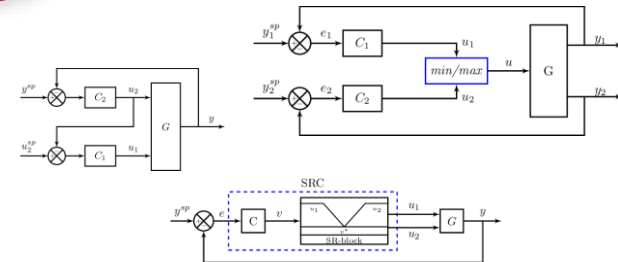
## S6: supervisory control layer

### Model predictive control

$$\min \sum_{k=1}^N \left( \omega_1 \| (T_{H_k} - T_H^{SP}) \|^2 + \omega_2 \| (F_{H_k}^{max} - F_{H_k}) \|^2 \right)$$

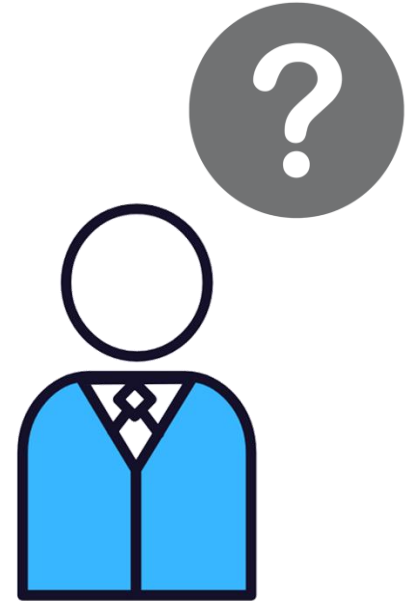
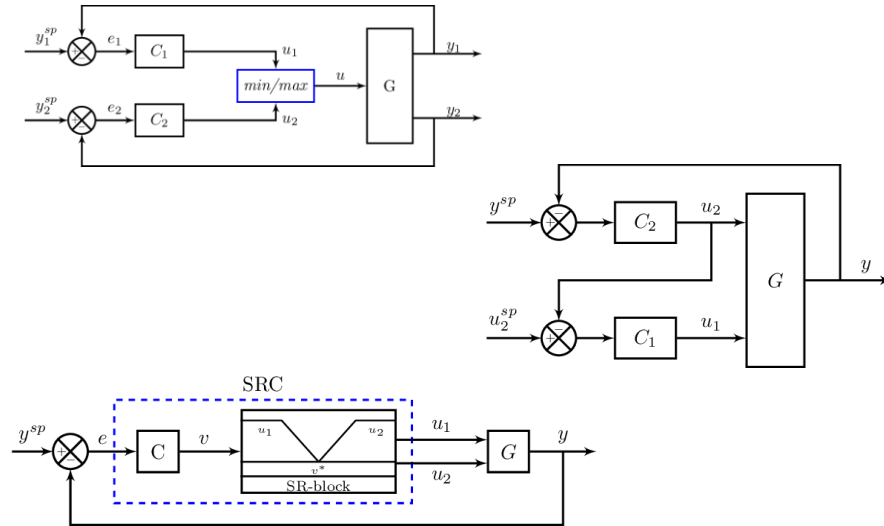
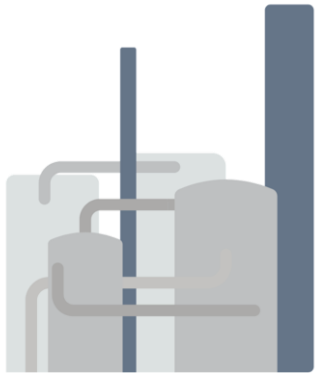
$$\text{s.t.} \left. \begin{aligned} T_{k,i} &= f(T_{H_{k,i}}, T_{H_{k,i-1}}, T_{C_{k,i}}, T_{C_{k,i+1}}, F_{H_k}, F_{C_k}) \\ 0 &\leq F_{H_k} \leq F_H^{max} \\ 0 &\leq F_{C_k} \leq F_C^{max} \\ 0 &\leq \Delta F_{H_k} \leq 0.1 F_H^{max} \\ 0 &\leq \Delta F_{C_k} \leq 0.1 F_C^{max} \end{aligned} \right\} \begin{aligned} &\forall k \in \{1, \dots, N\} \\ &\forall k \in \{1, \dots, N-1\} \end{aligned}$$

### Advanced control structures





# Active constraint switching with classical advanced control structures



# Active constraint switching with classical advanced control structures

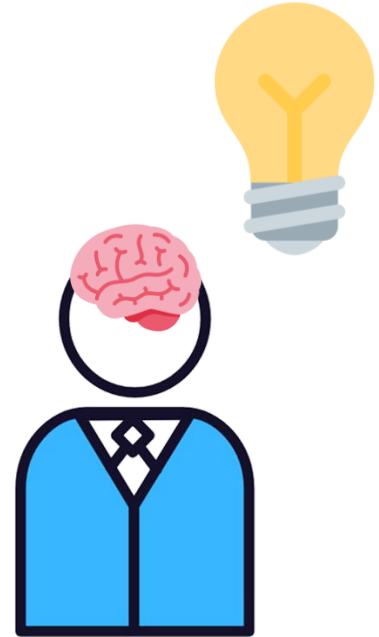
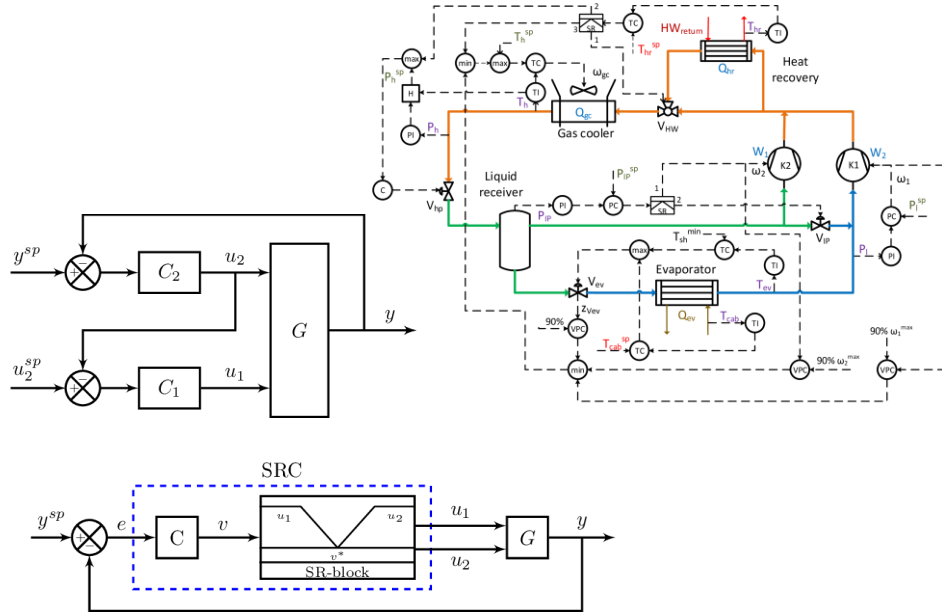
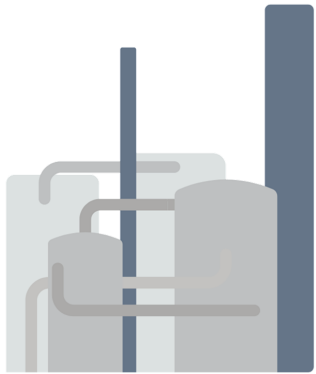


Figure taken from [www.transmittershop.com/blog/causes-solutions-annoying-noise-control-valves](http://www.transmittershop.com/blog/causes-solutions-annoying-noise-control-valves)

# Active constraint switching with classical advanced control structures

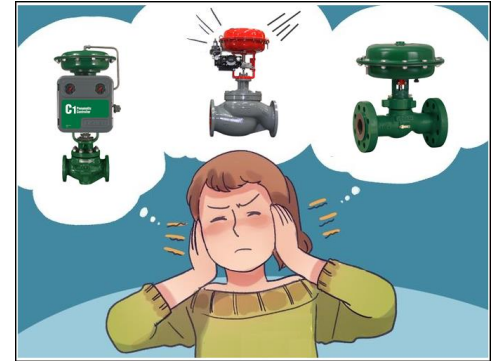
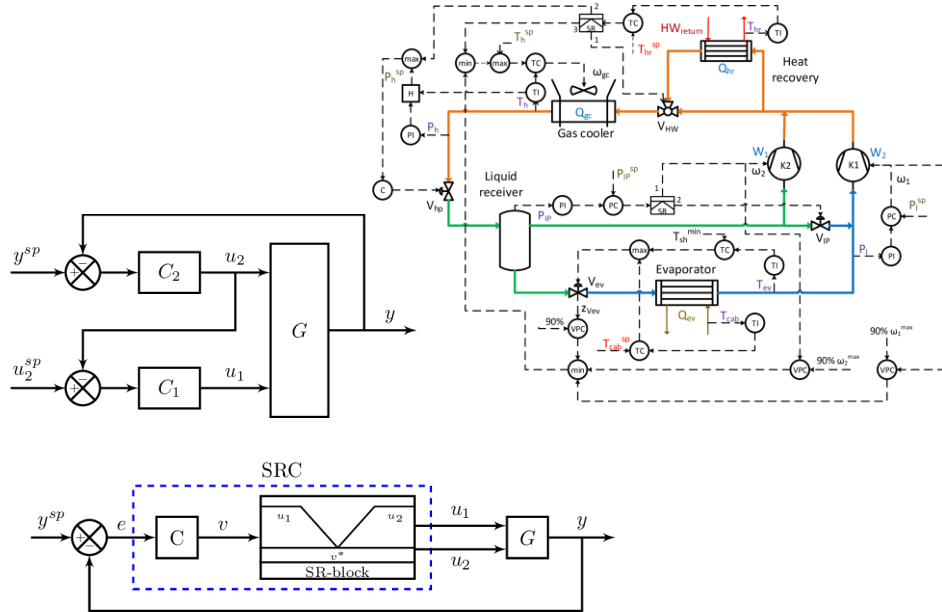
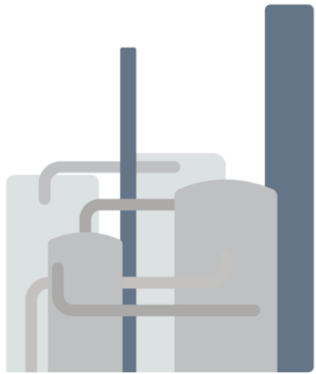
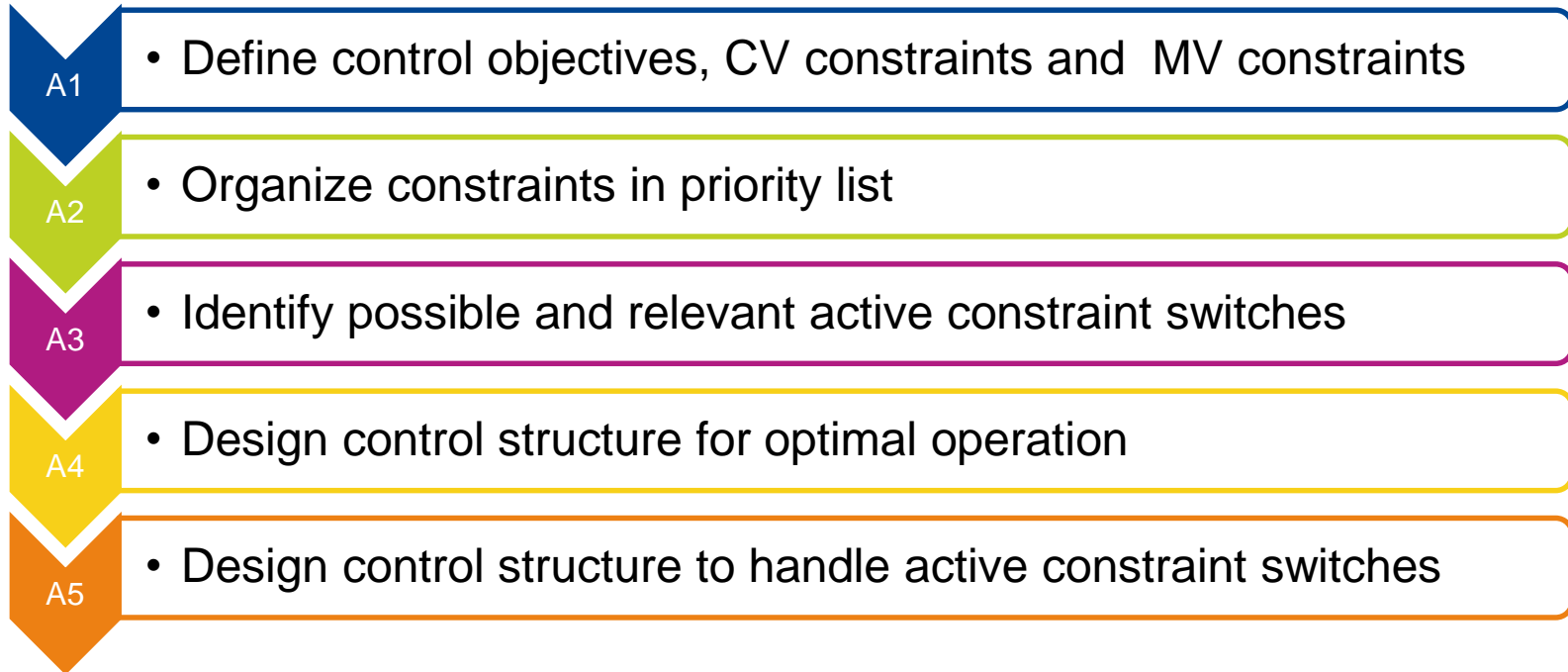


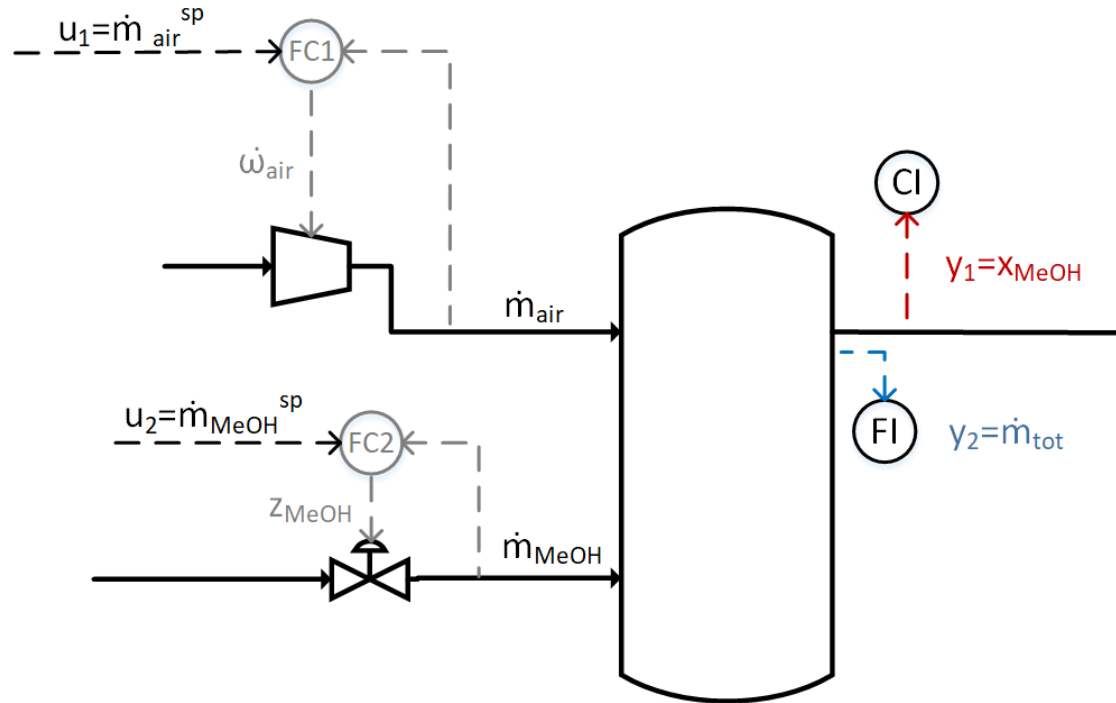
Figure taken from [www.transmittershop.com/blog/causes-solutions-annoying-noise-control-valves](http://www.transmittershop.com/blog/causes-solutions-annoying-noise-control-valves)

# Design procedure for active constraint switching with classical advanced control structures



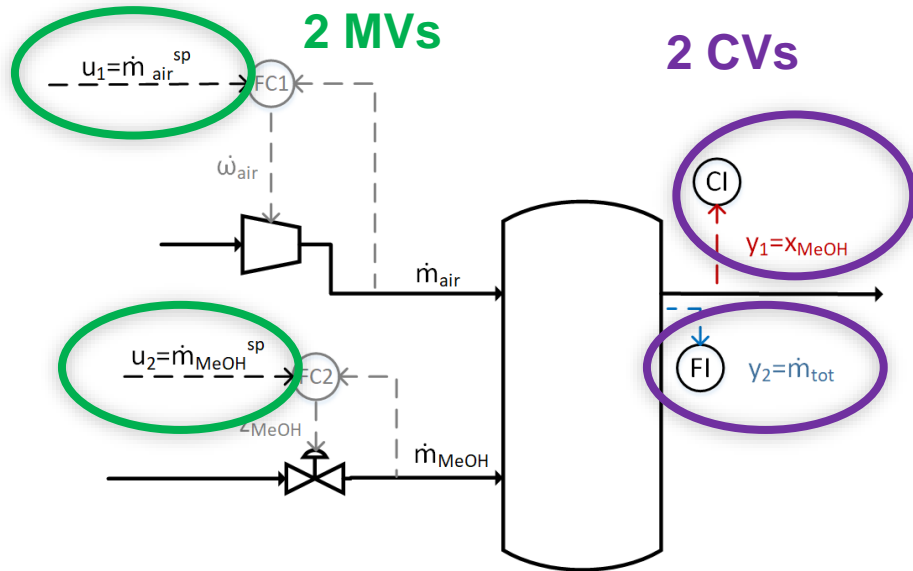
# Design procedure for active constraint switching

**Case study:**  
Mixing of  
air and MeOH



# Design procedure for active constraint switching

Step A1: Define control objectives, CV constraints and MV constraints

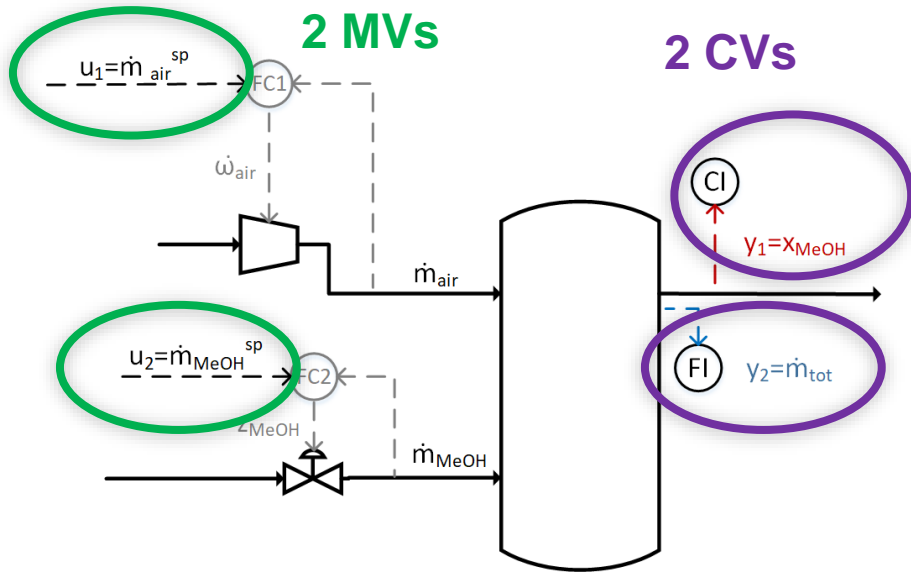


## Control objectives:

- Keep  $y_1 = x_{MeOH} = 0.10 \leftarrow$  ideal
- Keep  $y_1 = x_{MeOH} > 0.08$
- Control  $y_2 = \dot{m}_{tot} \leftarrow$  ideal

# Design procedure for active constraint switching

Step A1: Define control objectives, CV constraints and MV constraints



## Control objectives:

- Keep  $y_1 = x_{\text{MeOH}} = 0.10$
- Keep  $y_1 = x_{\text{MeOH}} > 0.08$
- Control  $y_2 = \dot{m}_{\text{tot}}$

Variable	Units	Maximum	Nominal
$y_1 = x_{\text{MeOH}}$	kmol/kmol	0.10	0.10
$y_2 = \dot{m}_{\text{tot}}$	kg/h		26860
$u_1 = \dot{m}_{\text{air}}$	kg/h	25800	23920
$u_2 = \dot{m}_{\text{MeOH}}$	kg/h		2940

$u_1$  is has a maximum value

# Design procedure for active constraint switching

Step A2: Organize constraints in priority list

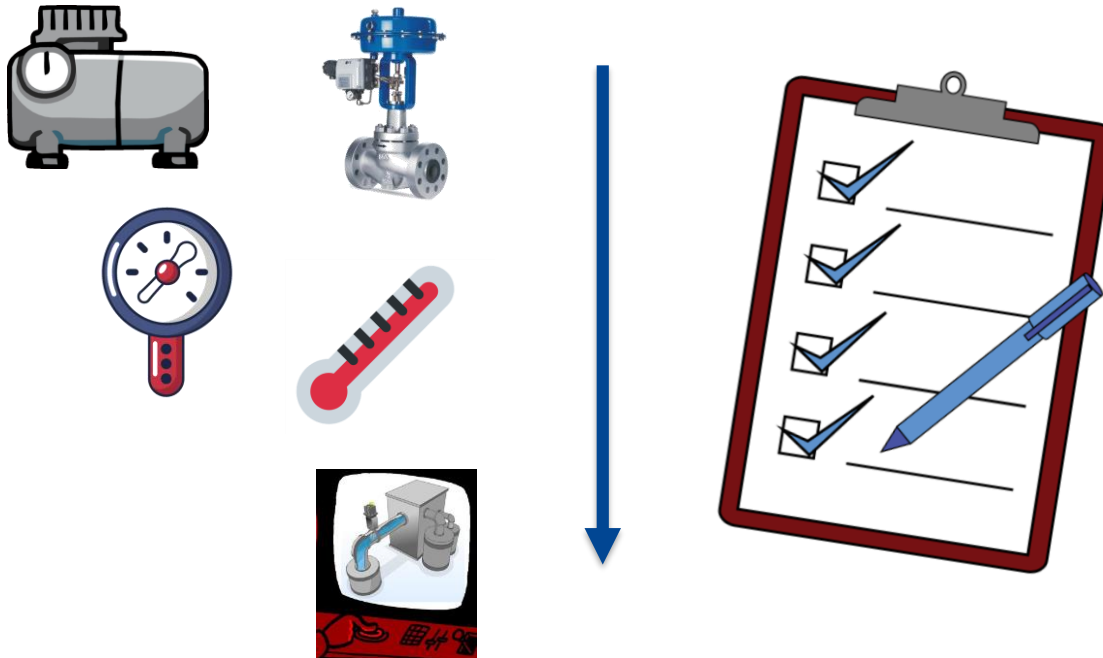


Figure from [www.indelac.com/blog/control-valves-vs.-regulators-in-control-applications](http://www.indelac.com/blog/control-valves-vs.-regulators-in-control-applications)



# Design procedure for active constraint switching

## Step A2: Organize constraints in priority list

(P1) Physical MV inequality constraints

- Constraint on air flow ( $u_1$ )
- Constraint on MeOH flow ( $u_2$ )

$$\dot{m}_{air}^{min} \leq \dot{m}_{air} \leq \dot{m}_{air}^{max}$$
$$\dot{m}_{MeOH}^{min} \leq \dot{m}_{MeOH} \leq \dot{m}_{MeOH}^{max}$$

(P2) Critical CV inequality constraints

- Constraint (max and min) on  $x_{MeOH}$  ( $y_1$ )

$$x_{MeOH}^{min} \leq x_{MeOH} \leq x_{MeOH}^{max}$$

(P3) Less critical CV and MV constraints

- Setpoint on  $x_{MeOH}$  ( $y_1$ )

$$x_{MeOH} = x_{MeOH}^{sp}$$

(P4) Desired throughput

- Setpoint on  $m_{tot}$  ( $y_2$ )

$$\dot{m}_{tot} = \dot{m}_{tot}^{sp}$$

(P5) Self-optimizing variables

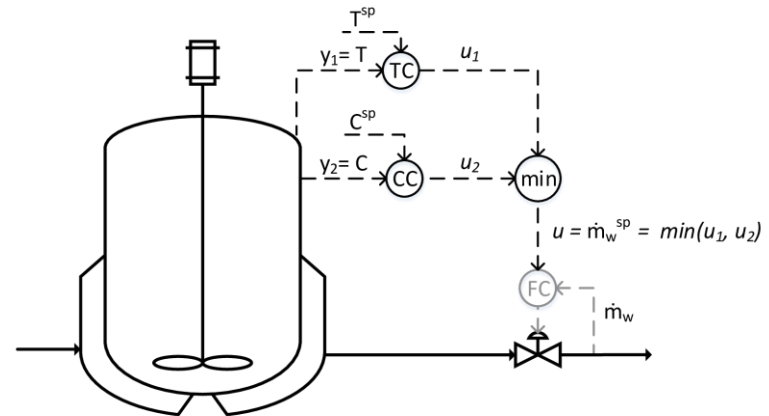
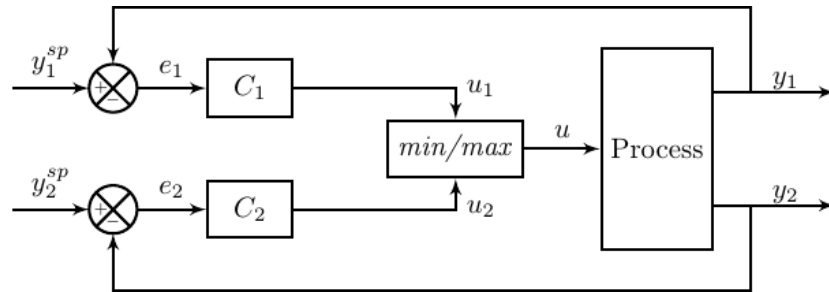
- No unconstrained degrees of freedom

# Design procedure for active constraint switching

Step A3: Identify possible and relevant active constraint switches

- **Case 1: CV to CV constraint switching**

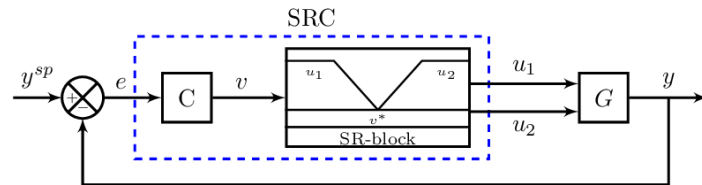
One MV switching between two alternative CVs.



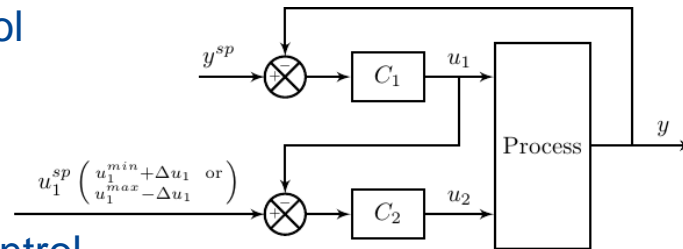
# Design procedure for active constraint switching

Step A3: Identify possible and relevant active constraint switches

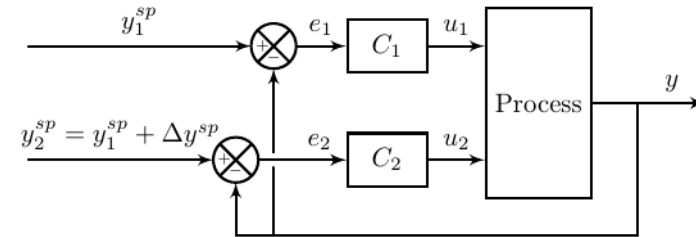
- **Case 2: MV to MV constraint switching**  
More than one MV for one CV.



Split range control



Valve position control



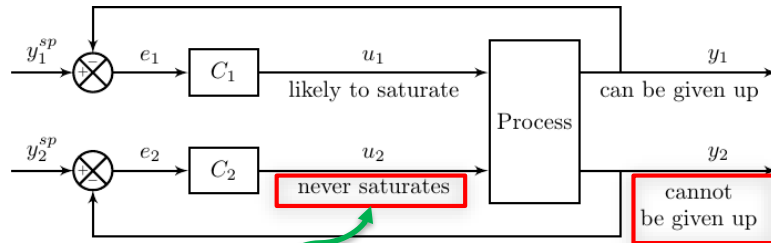
Different controllers  
with different setpoints

# Design procedure for active constraint switching

Step A3: Identify possible and relevant active constraint switches

- **Case 3: MV to CV constraint switching**

MV controlling a CV that may saturate; no extra MVs



*MV that does not saturate*

*High priority CV: always controlled*

## Input saturation pairing rule

«an MV that is likely to saturate at steady-state should be paired with a CV that can be given up»

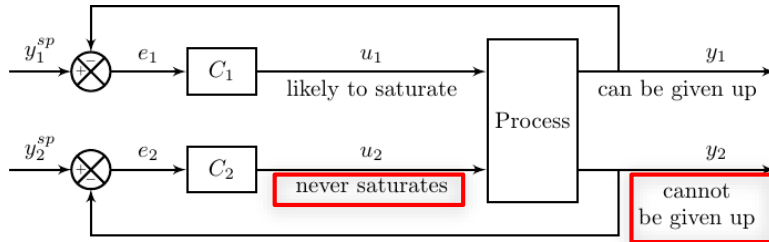
*Low priority CV*

# Design procedure for active constraint switching

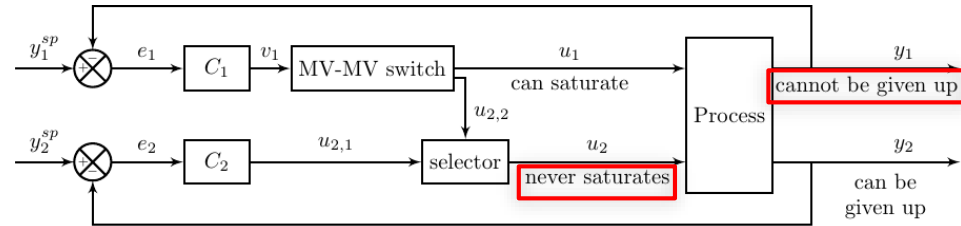
Step A3: Identify possible and relevant active constraint switches

- **Case 3: MV to CV constraint switching**

MV controlling a CV that may saturate; no extra MVs



Following input  
saturation pairing rule



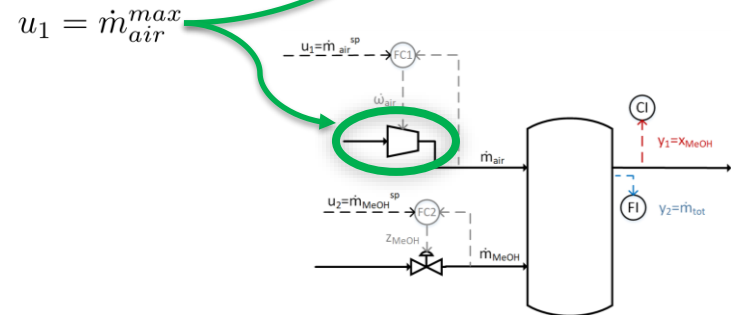
**NOT** following input  
saturation pairing rule

# Design procedure for active constraint switching

Step A3: Identify possible and relevant active constraint switches

- At nominal operation point all constraints are satisfied
  - **Constraint switch:**
    - Reach maximum air flow ( $u_1$ )
- ↓
- Lose a degree of freedom (**case 3**)
    - Must give up controlling the constraint with the lowest priority (desired throughput)

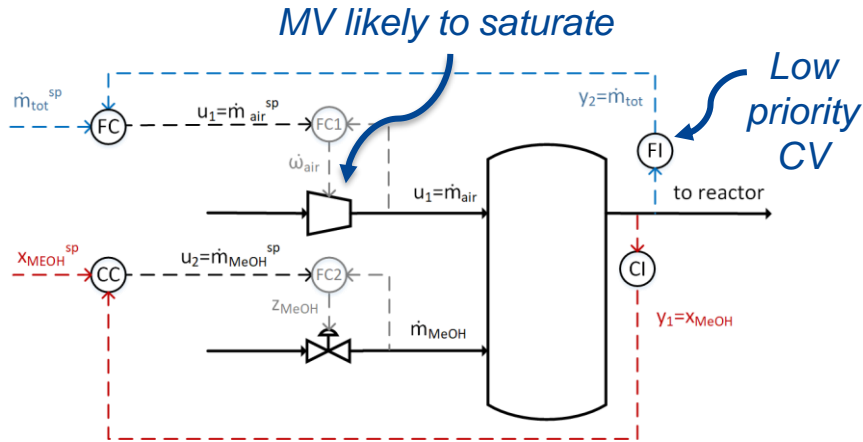
Variable	Units	Maximum	Nominal
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$y_2 = \dot{m}_{tot}$	kg/h		26860
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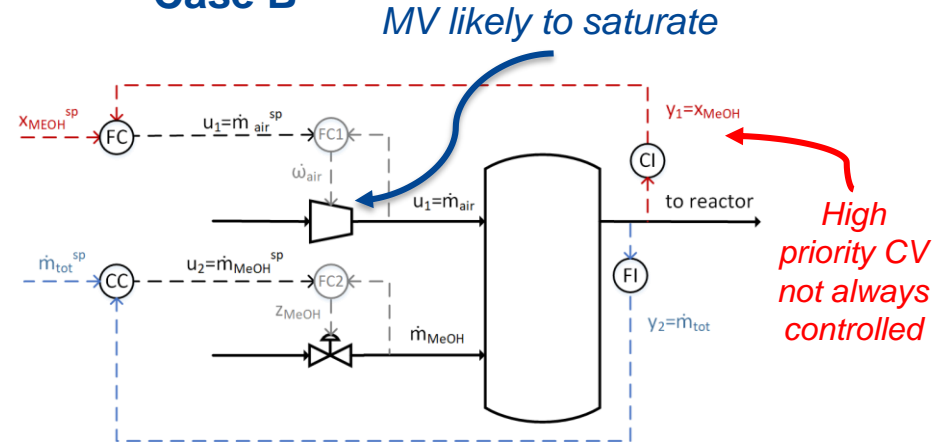
# Design procedure for active constraint switching

Step A4: Design control structure for optimal operation

## Case A



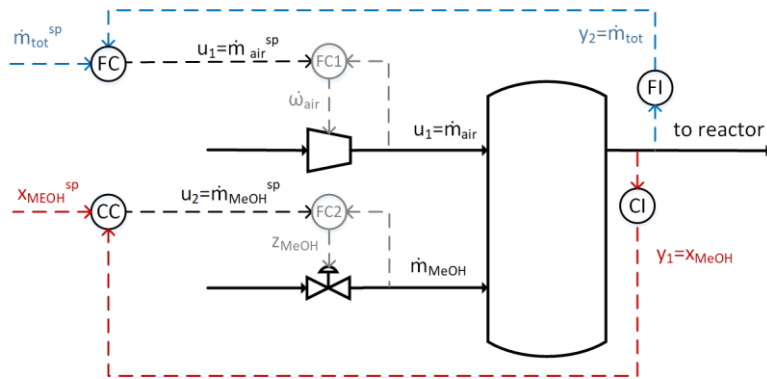
## Case B



# Design procedure for active constraint switching

Step A4: Design control structure for optimal operation

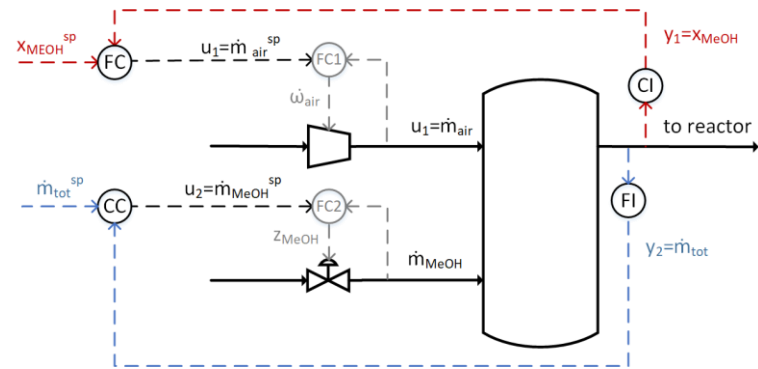
## Case A



Following input  
saturation pairing rule

## Case B

*Needs MV to CV  
switching*



NOT following input  
saturation pairing rule

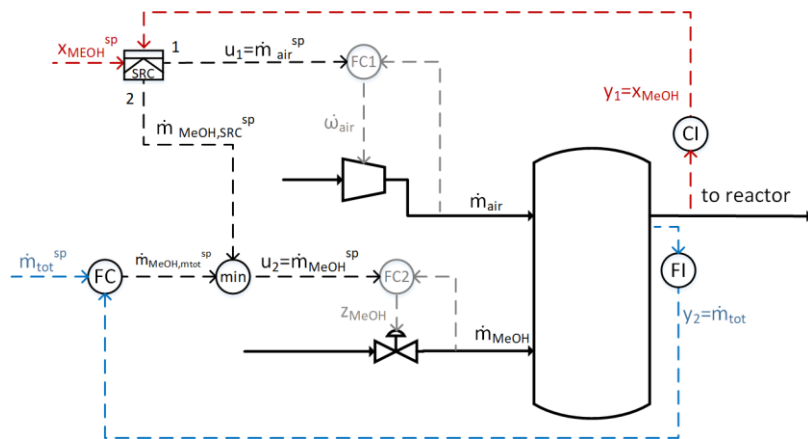


# Design procedure for active constraint switching

Step A5: Design control structure to handle active constraint switches

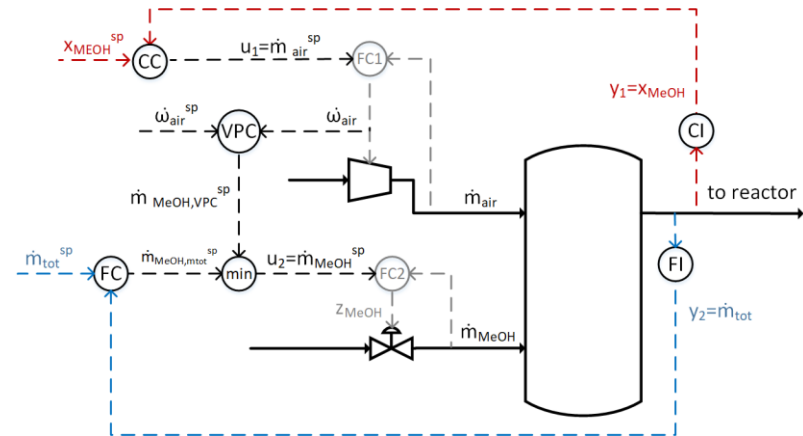
## Case B-SRC

Split range control+selector



## Case B-VPC

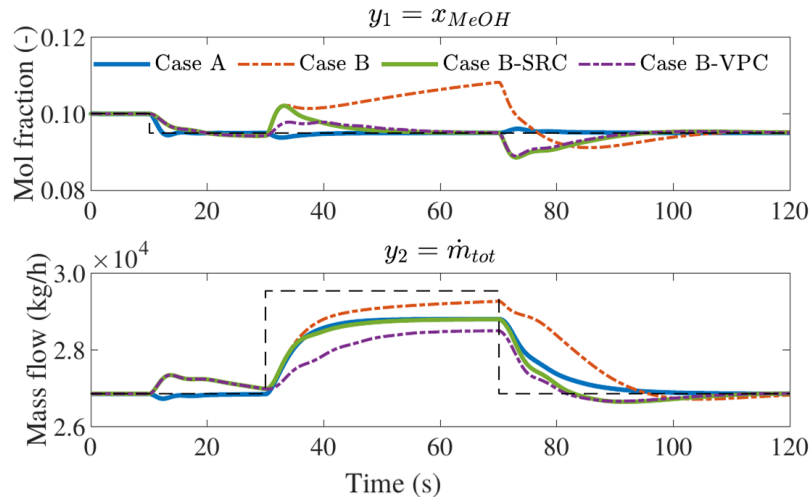
Valve position control + selector



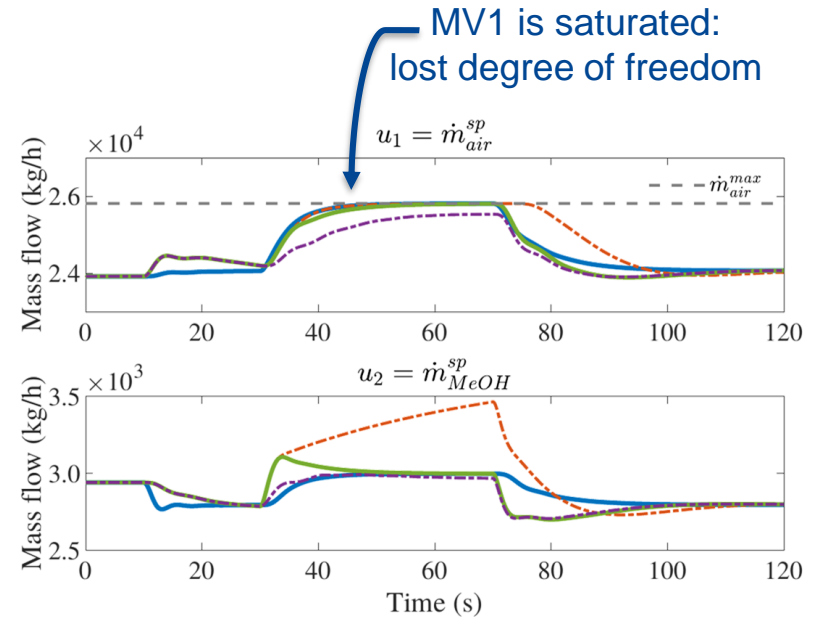
# Design procedure for active constraint switching

**Case study:** Mixing of air and MeOH

**High priority CV: concentration**



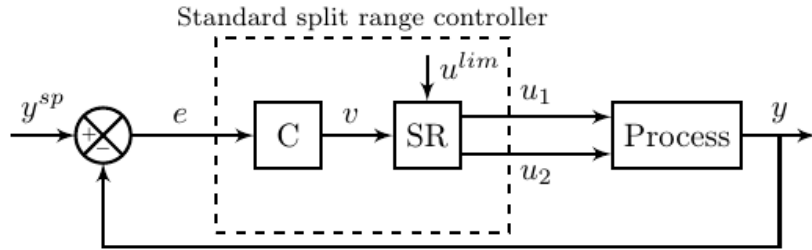
**Low priority CV (throughput)**



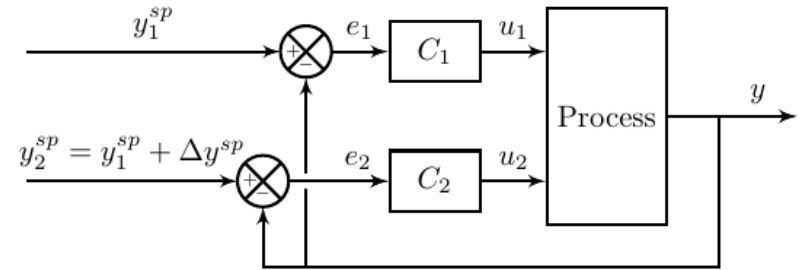
**MV2 is not saturated:**  
It should be used to control the high priority CV

# MV to MV constraint switching

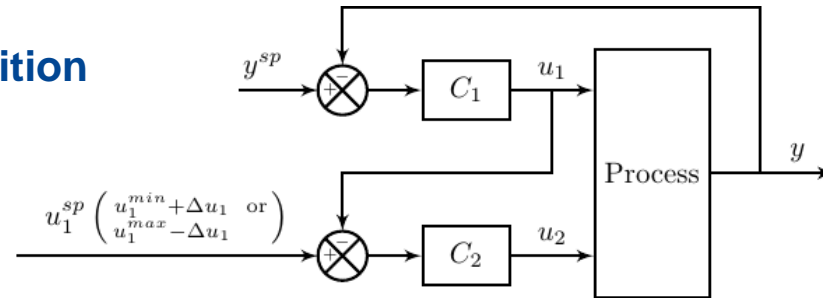
## Split range control



## Different controllers with different setpoints



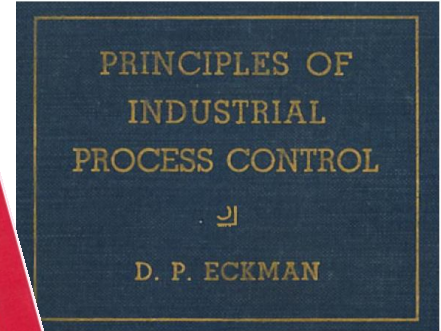
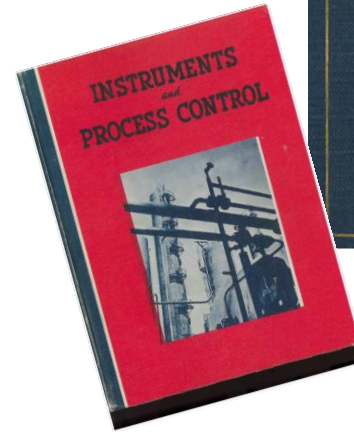
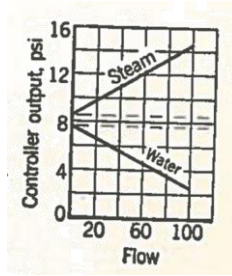
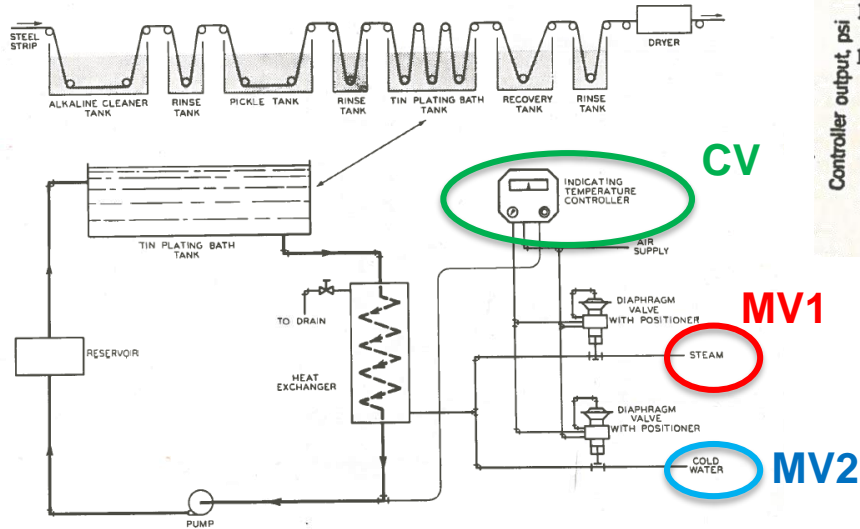
## Valve position control



# Classical split range control

INSTRUMENTS AND PROCESS CONTROL

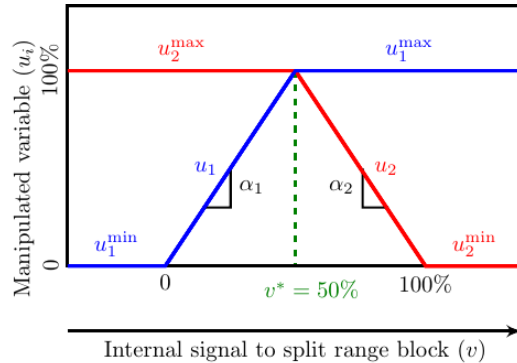
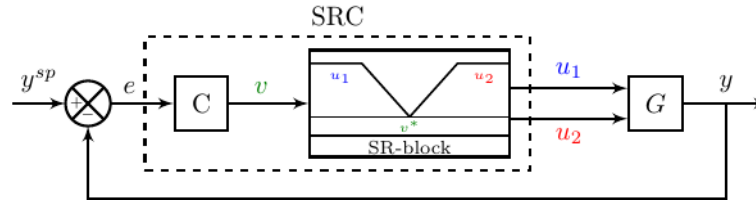
Information Sheet 9



Eckman, D.P. (1945). Principles of industrial control, New York.

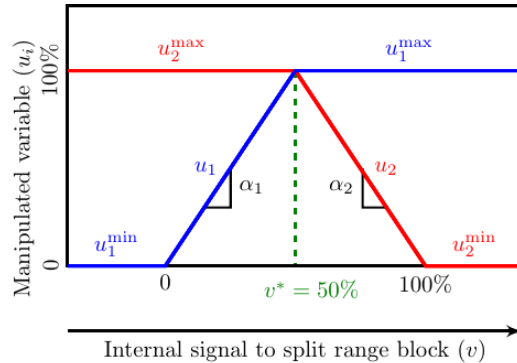
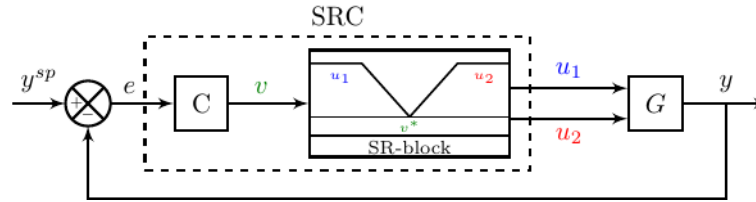
Monogram of Instruments and Process Control prepared at Cornell, NY, in 1945

# Classical split range control



- $v$  internal signal to split range block  $\rightarrow$  limited physical meaning
- $v^*$  split value
- $u_i$  controller output  $\rightarrow$  physical meaning
- $\alpha_i$  gain from  $v$  to  $u_i$   $\rightarrow$  slope

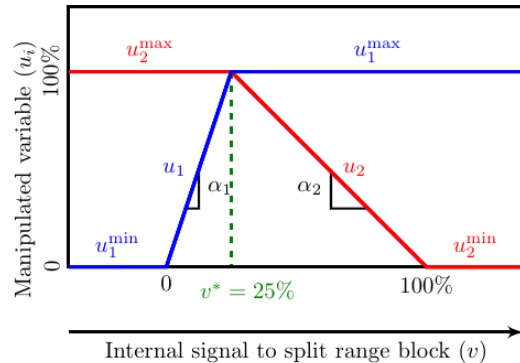
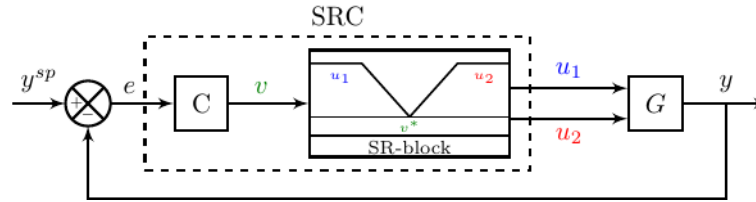
# Classical split range control



- $v$  internal signal to split range block  $\rightarrow$  limited physical meaning
- $v^*$  split value  $\rightarrow$  degree of freedom
- $u_i$  controller output  $\rightarrow$  physical meaning
- $\alpha_i$  gain from  $v$  to  $u_i$   $\rightarrow$  slope

$$u_i = u_{i,0} + \alpha_i v \quad \forall i \in \{1, \dots, N\}$$

# Classical split range control



- $v$  internal signal to split range block  $\rightarrow$  limited physical meaning
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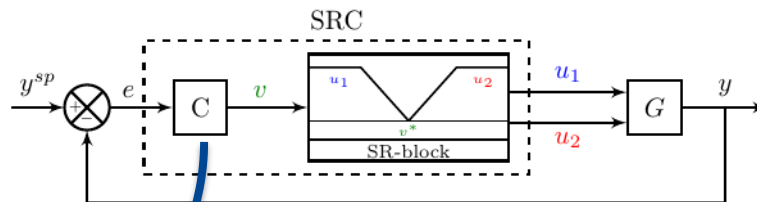
$$u_i = u_{i,0} + \alpha_i v \quad \forall i \in \{1, \dots, N\}$$

# Design of split range control: select slopes

**Goal:** get desired loop gain at crossover frequency

$$|g C|$$

$$\omega_c = \frac{1}{\tau_C}$$



$$C(s) = K_C \left( 1 + \frac{1}{\tau_I s} \right)$$

Fast process

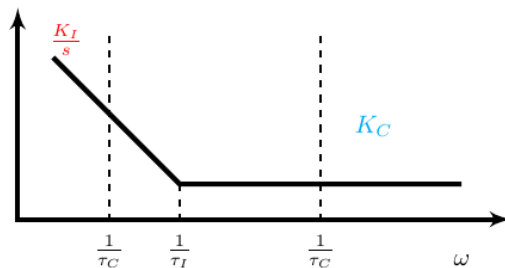
$$K_{I,i} = \alpha_i K_I$$

$$K_I = \frac{K_C}{\tau_I}$$

Desired gain for  $u_i$

DOF

Common gain in C



Slow process

$$K_{C,i} = \alpha_i K_C$$

Desired gain for  $u_i$

DOF

Common gain in C

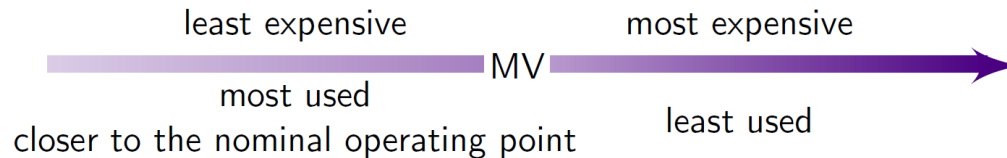


# Design of split range control: order of MVs

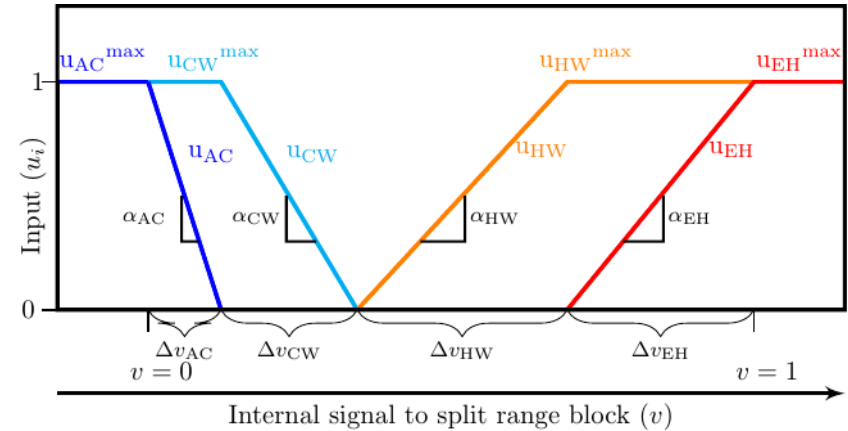
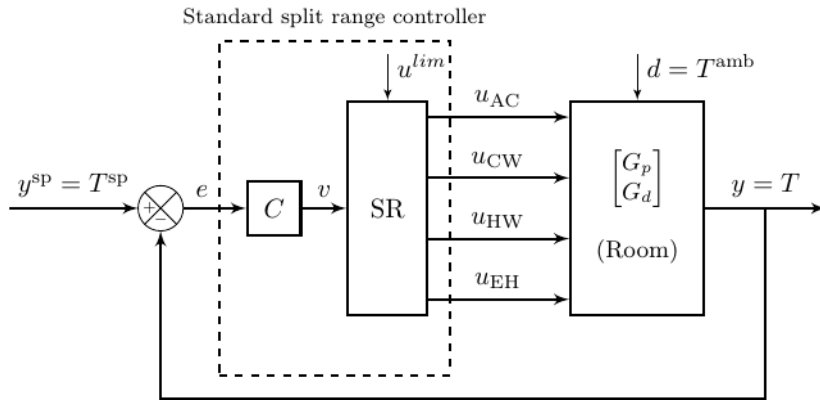
Define the desired operating point for every MV

Group the MVs according to the effect on the CV

Within each group, define order of use



# Design of split range control



$u_1 = u_{AC}$  : air conditioning (AC)

$u_2 = u_{CW}$  : cooling water (CW)

$u_3 = u_{HW}$  : heating water (HW)

$u_4 = u_{EH}$  : electrical heating (EH)

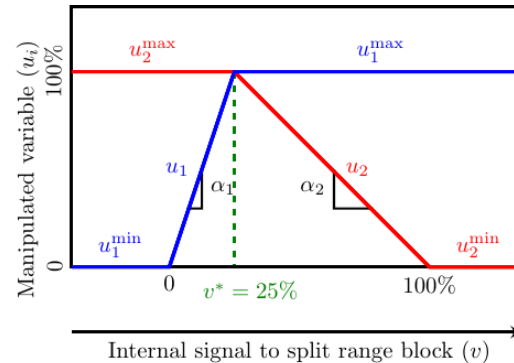
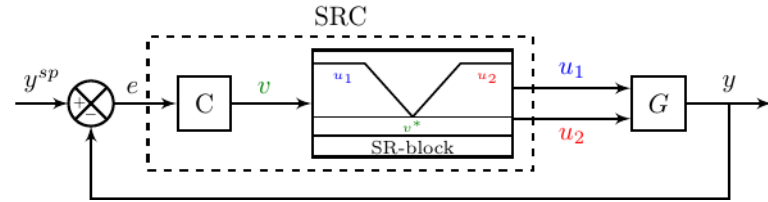
# Classical split range control: a compromise

$$C(s) = K_C \left( 1 + \frac{1}{\tau_I s} \right)$$

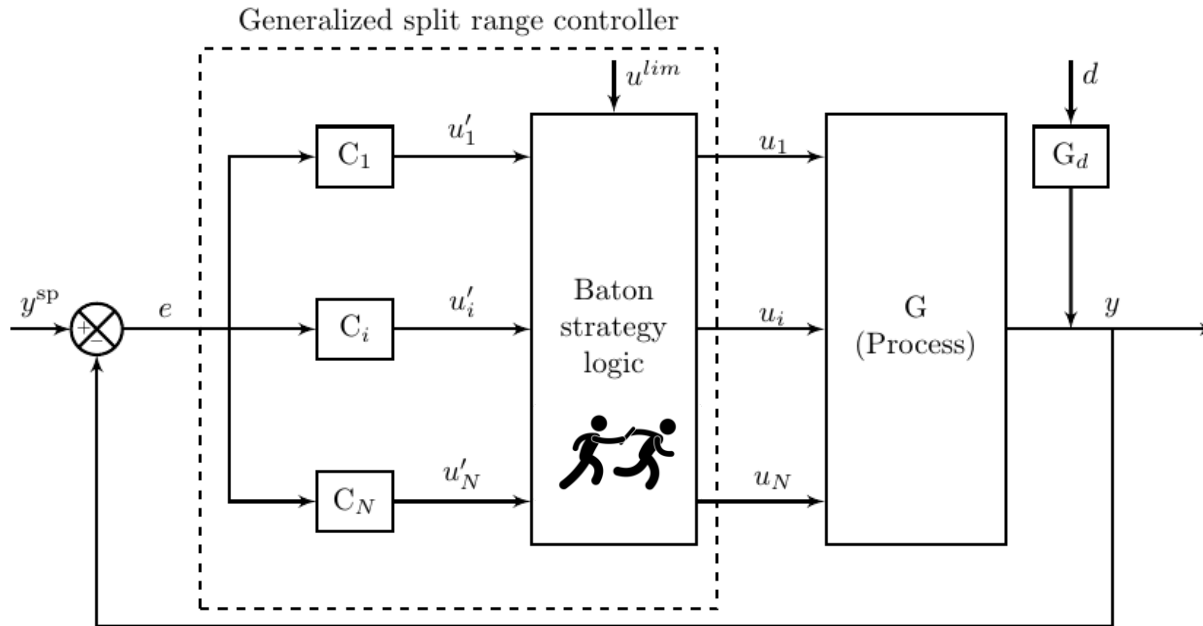
2 tuning parameters

$$K_{C,i} = \alpha_i K_C$$

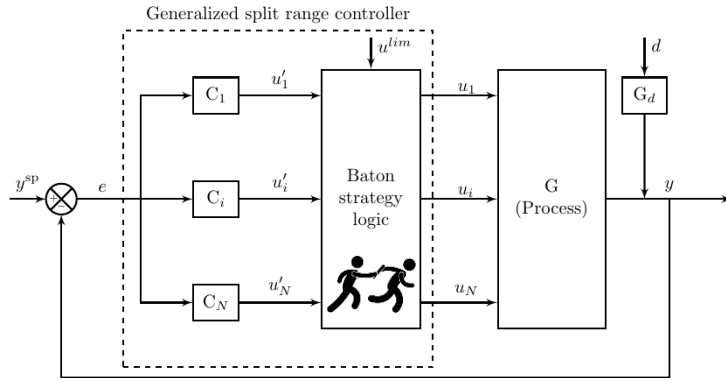
1 DOF



# Generalized split range controller



# Generalized split range controller



## Preliminary step:

- Define order of use of MVs ( $j=1, \dots, N$ )
- Tune controllers

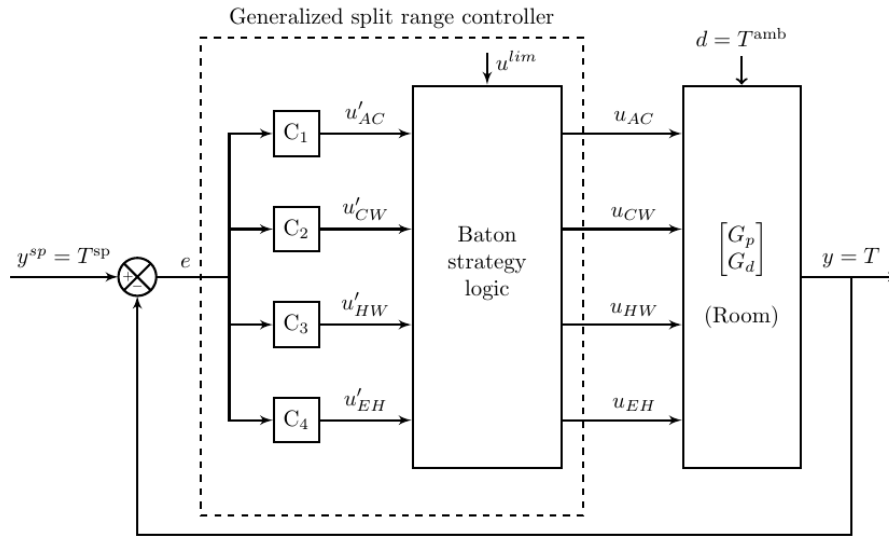
## «Baton strategy» logic

$k$  is the active input

- $C_k$  computes  $u'_k$  (suggested value for  $u_k$ )
- If  $u_k^{\min} < u'_k < u_k^{\max}$ 
  - Keep  $u_k$  active and  $u_k \leftarrow u'_k$
  - Keep remaining  $u_i$  at limiting value
- else
  - Set  $u_k = u_k^{\min}$  or  $u_k < u_k^{\max}$ , depending on the reached limit
  - New active input selected according to predefined sequence ( $j = k-1$  or  $j = k+1$ )

The active input will *decide* when to switch and will remain active as long as it is not saturated.

# Generalized split range controller



Value of $u'_k$	Active input (input with baton, $u_k$ )			
	$u_1 = u_{AC}$	$u_2 = u_{CW}$	$u_3 = u_{HW}$	$u_4 = u_{EH}$
$u_k^{min} < u'_k < u_k^{max}$	keep $u_1$ active $u_1 \leftarrow u'_1$ $u_2 \leftarrow u_2^{max}$ $u_3 \leftarrow u_3^{min}$ $u_4 \leftarrow u_4^{min}$	keep $u_2$ active $u_1 \leftarrow u_1^{min}$ $u_2 \leftarrow u'_2$ $u_3 \leftarrow u_3^{min}$ $u_4 \leftarrow u_4^{min}$	keep $u_3$ active $u_1 \leftarrow u_1^{min}$ $u_2 \leftarrow u_2^{min}$ $u_3 \leftarrow u'_3$ $u_4 \leftarrow u_4^{min}$	keep $u_4$ active $u_1 \leftarrow u_1^{min}$ $u_2 \leftarrow u_2^{min}$ $u_3 \leftarrow u_3^{max}$ $u_4 \leftarrow u'_4$
$u'_k \geq u_k^{max}$	keep $u_1$ active (max. cooling)	baton to $u_1$ $u_1^0 = u_1^{min}$	baton to $u_4$ $u_4^0 = u_4^{min}$	keep $u_4$ active (max. heating)
$u'_k \leq u_k^{min}$	baton to $u_2$ $u_2^0 = u_2^{max}$	baton to $u_3$ $u_3^0 = u_3^{min}$	baton to $u_2$ $u_2^0 = u_2^{min}$	baton to $u_3$ $u_3^0 = u_3^{max}$

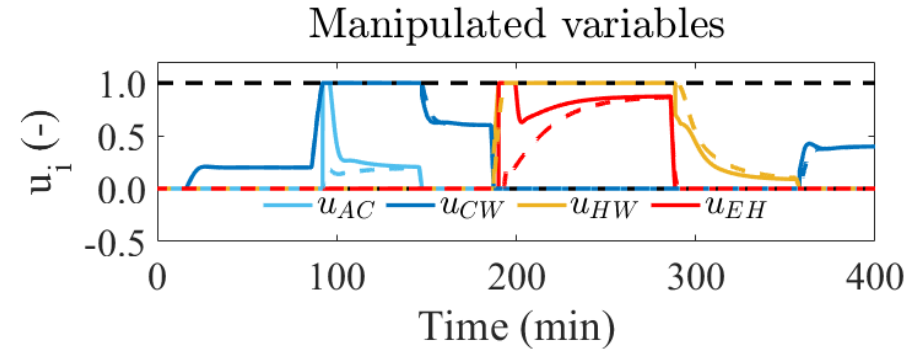
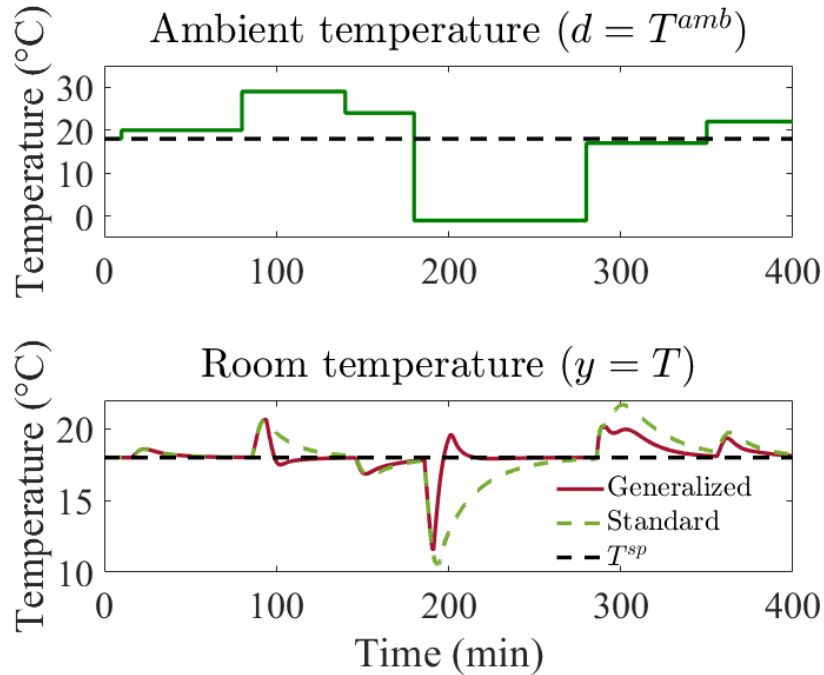
$u_1 = u_{AC}$  : air conditioning (AC)

$u_2 = u_{CW}$  : cooling water (CW)

$u_3 = u_{HW}$  : heating water (HW)

$u_4 = u_{EH}$  : electrical heating (EH)

# Generalized vs standard split range controller



# Generalized split range controller: initialization



$$u'_k(t) = u_k^0 + K_{C,k} \left( e(t) + \frac{1}{\tau_{I,k}} \int_{t_b}^t e(t) \right)$$

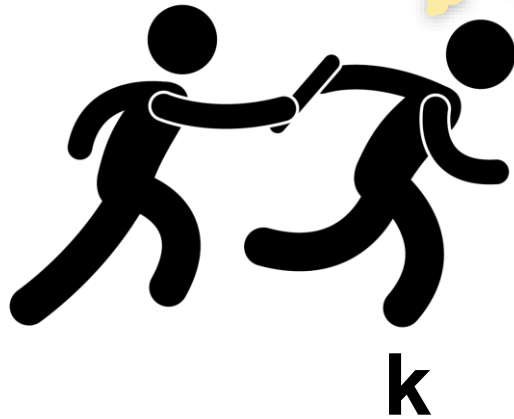
This suggested input was not being applied while input k was not in use

This accumulated error is not due to the previous actions of input k



# Generalized split range controller: initialization

Only use error  
when I receive  
the baton



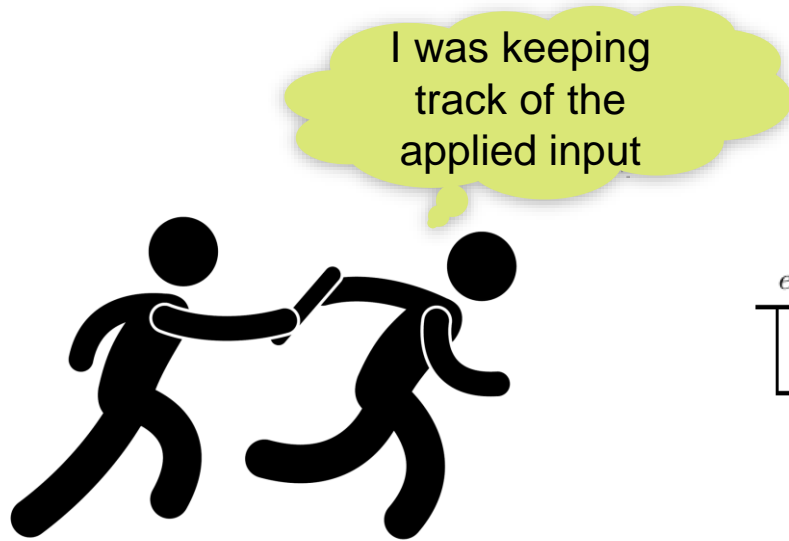
Resetting:

$$u'_k(t) = u_k^0 + K_{C,k} \left( e(t) + \frac{1}{\tau_{I,k}} \int_{t_b}^t e(t) dt \right)$$

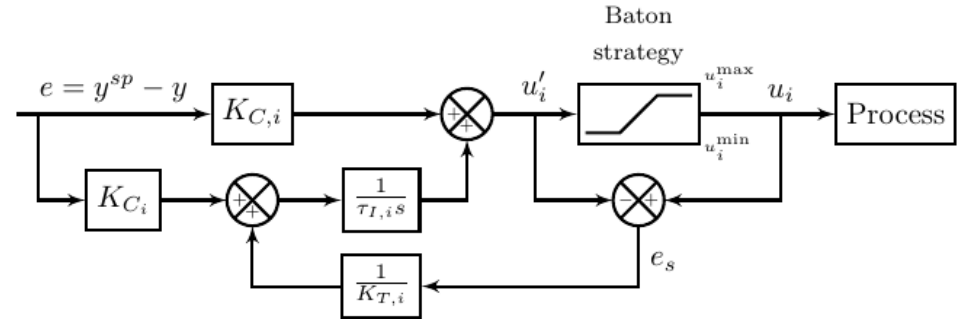
$$u_k(t_b) = u_k^0 + K_{C,k} e(t_b)$$

Initial action proportional to error at  $t_b$

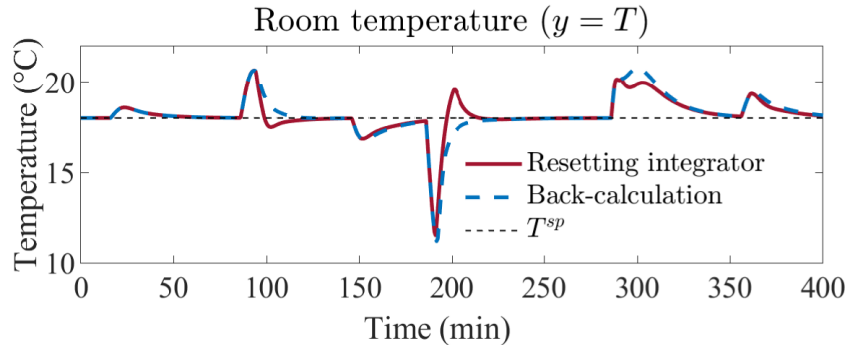
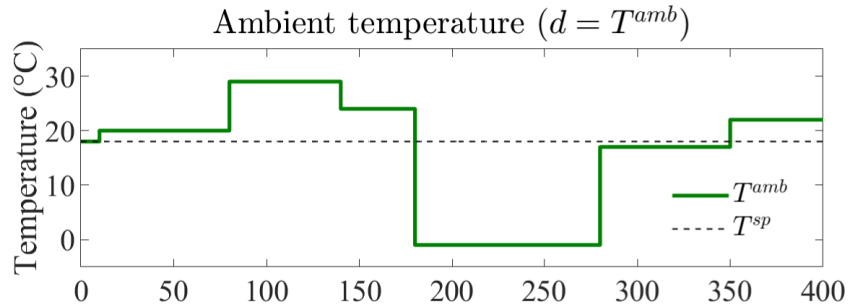
# Generalized split range controller: initialization



Back-calculation:

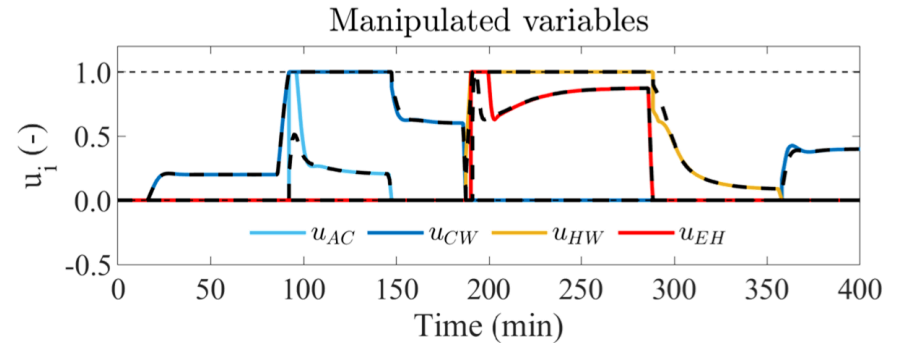
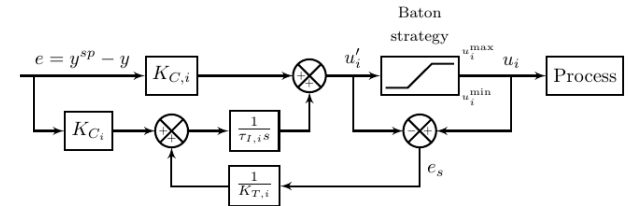


# Generalized split range controller: initialization

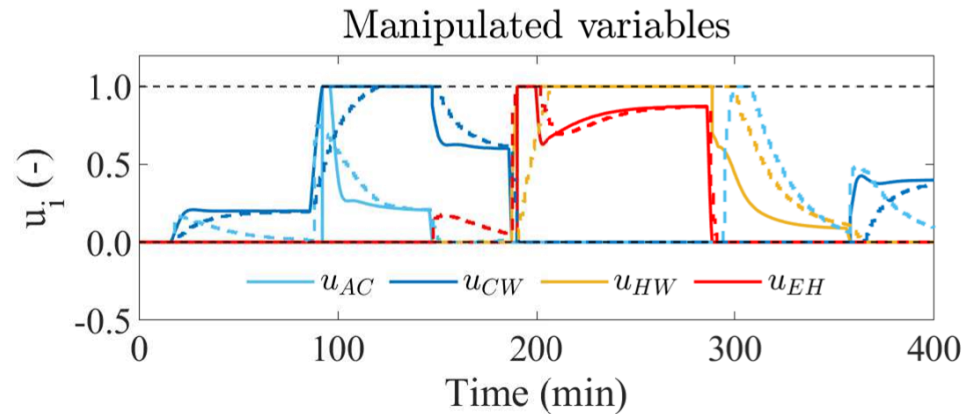
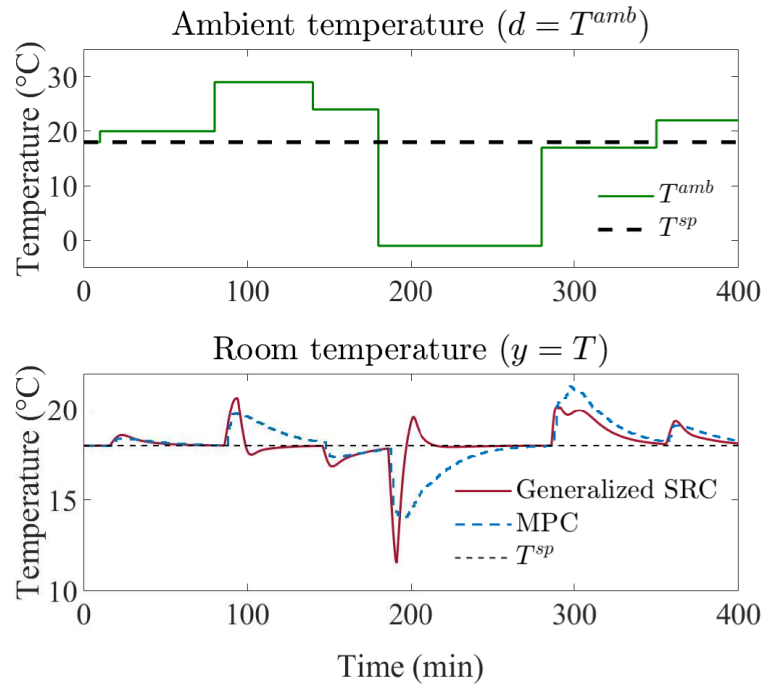


**Resetting:**  $u_k(t_b) = u_k^0 + K_{C,k}e(t_b)$

**Back-calculation:**

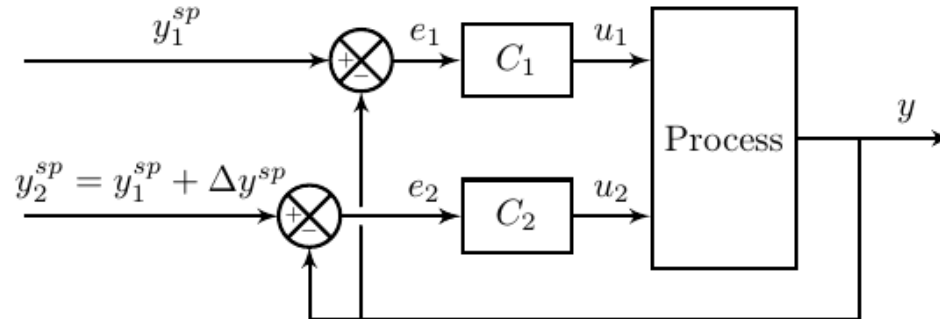


# Generalized split range controller vs MPC

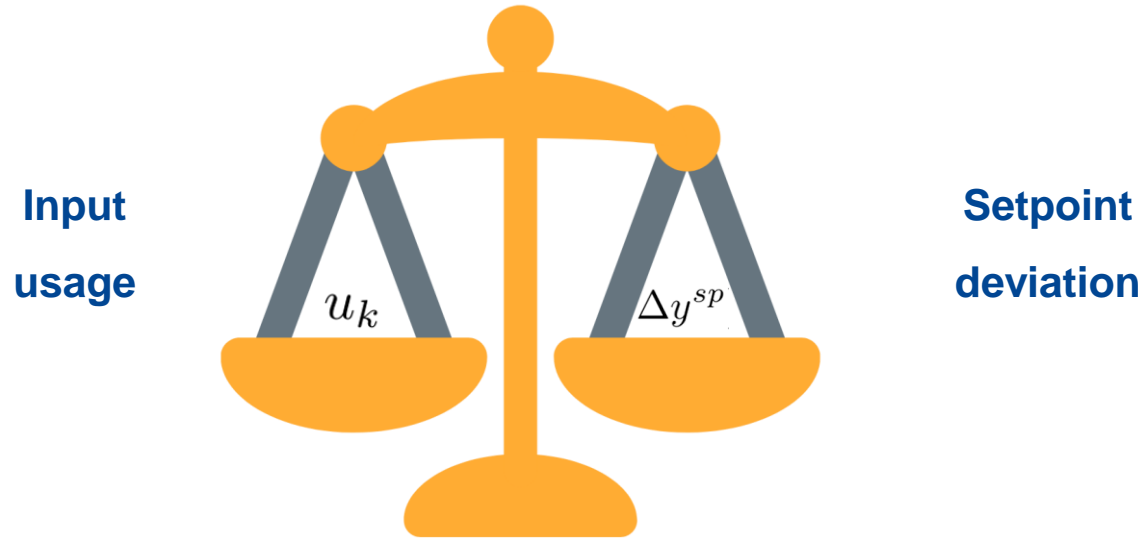


# Multiple controllers with different setpoints

Does this make sense at any point?



# Multiple controllers with different setpoints



$$J(u_k, \Delta y^{sp})$$

# Multiple controllers with different setpoints: Optimal setpoint deviation

Linear for  $u$  and quadratic for  $\Delta y$

$$J = p_{u_k} u_k + p_y (y - y^{sp})^2 + c$$

*Inputs are a linear function of output*

$$u_i = k_i y + u_{i,0}$$

# Multiple controllers with different setpoints: Optimal setpoint deviation

Linear for  $u$  and quadratic for  $\Delta y$

$$J = p_{u_k} u_k + p_y (y - y^{sp})^2 + c$$

Inputs are a linear function of output

$$u_i = k_i y + u_{i,0}$$

Cost when using  $u_k$  as input

$$J = p_{u_k} k_k y + p_y (y - y^{sp})^2 + c_k + p_{u_k} u_{k,0}$$



# Multiple controllers with different setpoints: Optimal setpoint deviation

Linear for  $u$  and quadratic for  $\Delta y$

$$J = p_{u_k} u_k + p_y (y - y^{sp})^2 + c$$

Inputs are a linear function of output

$$u_i = k_i y + u_{i,0}$$

Cost when using  $u_k$  as input

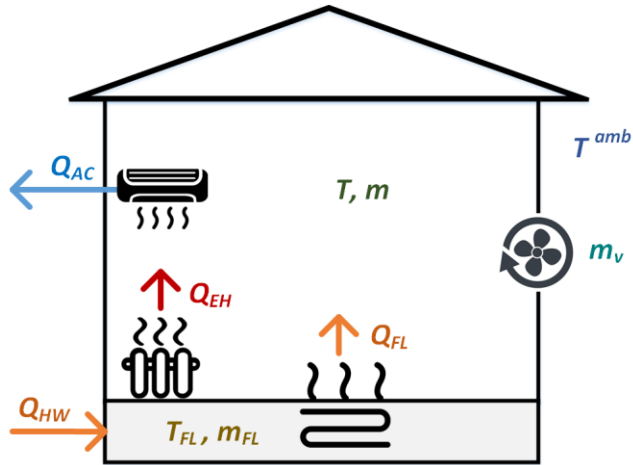
$$J = p_{u_k} k_k y + p_y (y - y^{sp})^2 + c_k + p_{u_k} u_{k,0}$$

$$\frac{dJ}{dy} = 0$$

Optimal  
setpoint deviation  
minimizing cost

$$\Delta y^{sp*} = y^* - y^{sp} = -\frac{p_{u_k} k_k}{2p_y}$$

# Multiple controllers with different setpoints: Case study

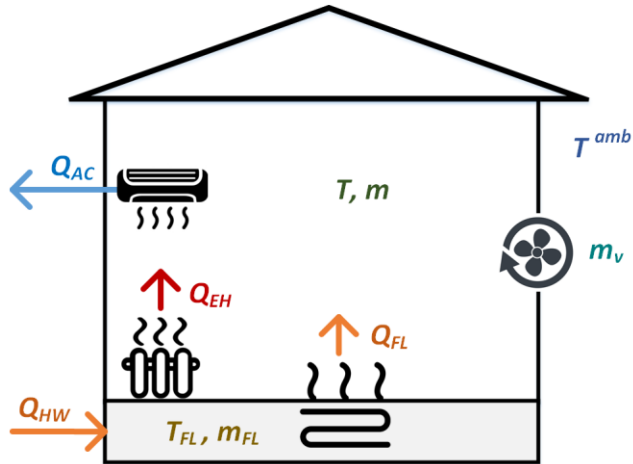


$Q_{AC}$  : air conditioning

$Q_{HW}$  : heating water

$Q_{EH}$  : electrical heating

# Multiple controllers with different setpoints: Room T



$Q_{AC}$  : air conditioning

$Q_{HW}$  : heating water

$Q_{EH}$  : electrical heating

Cost: linear for  $u$  and quadratic for  $\Delta y$

$$J = \underbrace{p_{AC}Q_{AC}}_{p_1 u_1} + \underbrace{p_{HW}Q_{HW}}_{p_2 u_2} + \underbrace{p_{EH}Q_{EH}}_{p_3 u_3} + \underbrace{p_T(T - T^{sp})^2}_{p_y (y - y^{sp})^2} \quad [\$ / s]$$

Inputs ( $Q_i$ ) are a linear function of output ( $T$ )

$$0 = \alpha(T^{amb} - T) + Q_{HW} + Q_{EH} - Q_{AC} \quad [W]$$

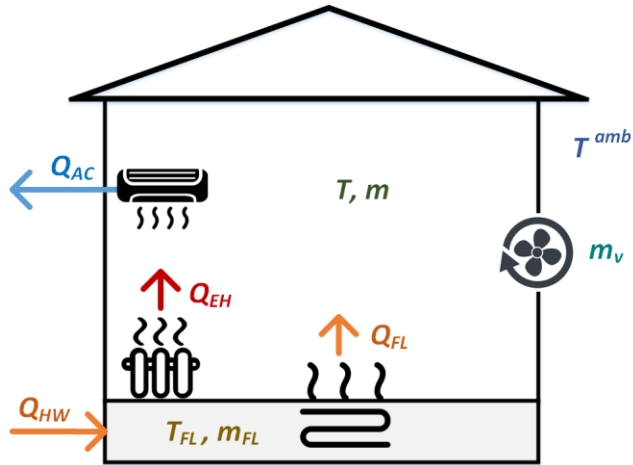
Optimal setpoint deviation minimizing cost

$$\Delta y^{sp,1} = T_{AC}^{sp} - T^{sp} = + \frac{\alpha p_{ac}}{2p_T}$$

$$\Delta y^{sp,2} = T_{HW}^{sp} - T^{sp} = - \frac{\alpha p_{hw}}{2p_T}$$

$$\Delta y^{sp,3} = T_{EH}^{sp} - T^{sp} = - \frac{\alpha p_{el}}{2p_T}$$

# Multiple controllers with different setpoints: Room T



$Q_{AC}$  : air conditioning

$Q_{HW}$  : heating water

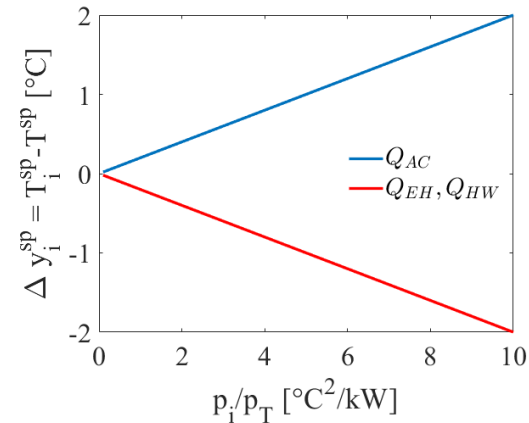
$Q_{EH}$  : electrical heating

Optimal setpoint deviation minimizing cost

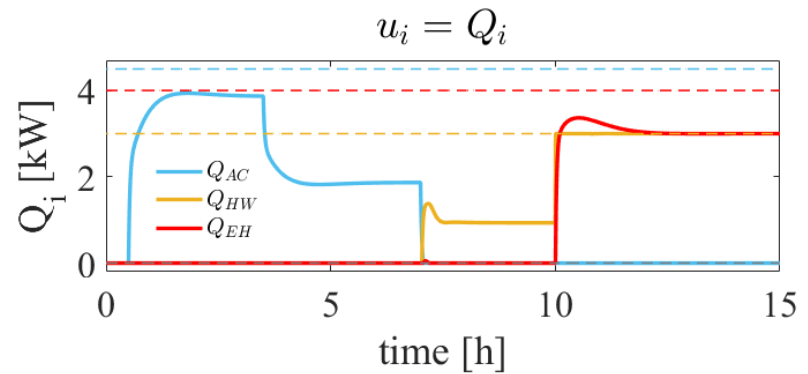
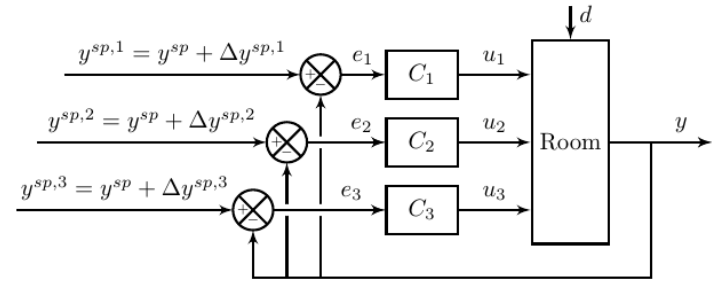
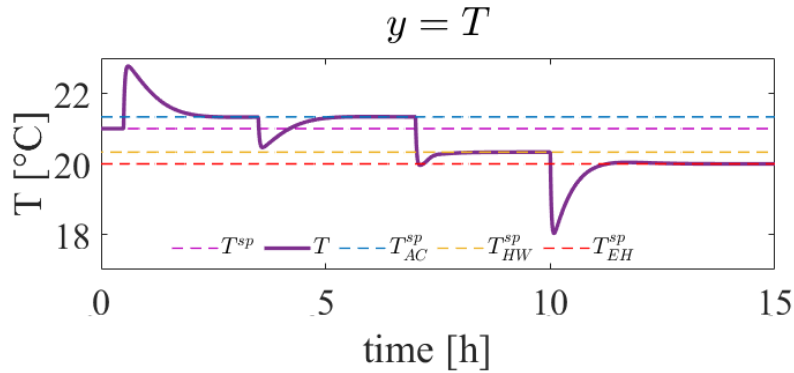
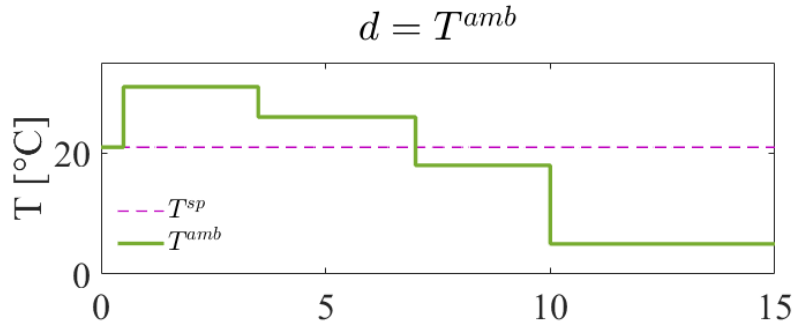
$$\Delta y^{sp,1} = T_{AC}^{sp} - T^{sp} = +\frac{\alpha p_{ac}}{2p_T}$$

$$\Delta y^{sp,2} = T_{HW}^{sp} - T^{sp} = -\frac{\alpha p_{hw}}{2p_T}$$

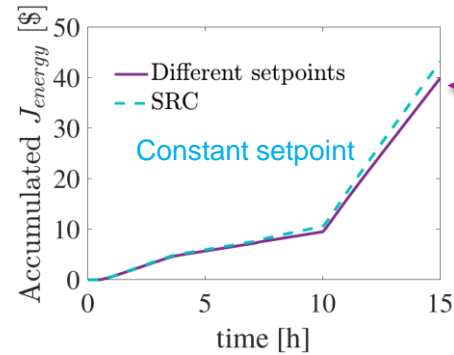
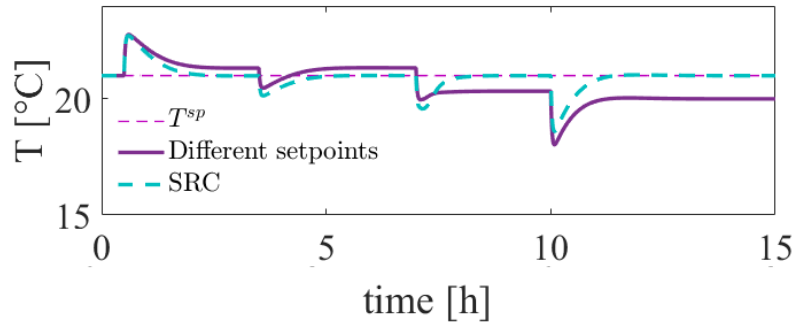
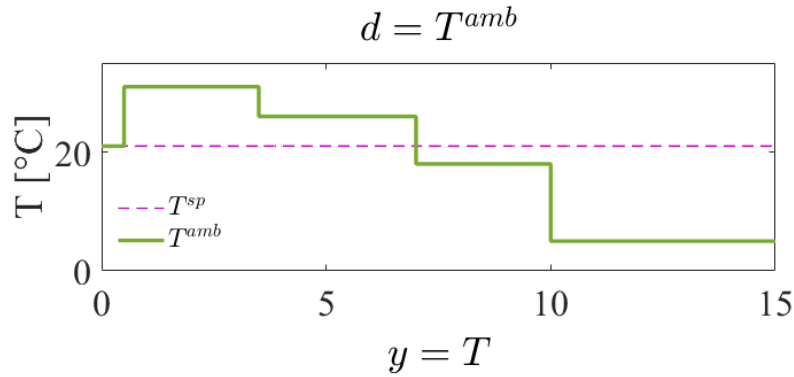
$$\Delta y^{sp,3} = T_{EH}^{sp} - T^{sp} = -\frac{\alpha p_{el}}{2p_T}$$



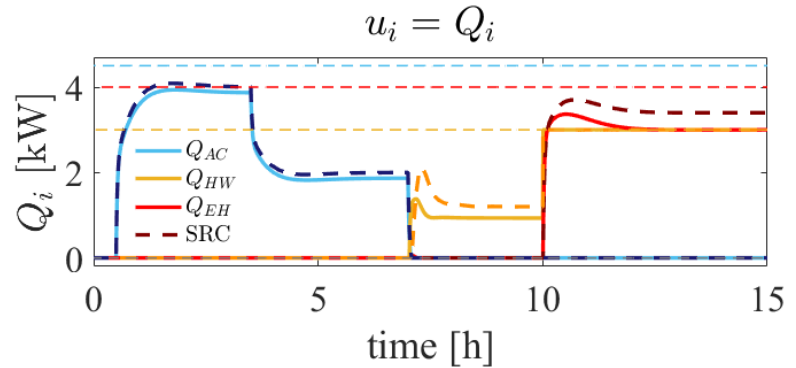
# Multiple controllers with different setpoints: Room T



# Multiple controllers with different setpoints: Room T



Lower accumulated cost with minimum setpoint deviation

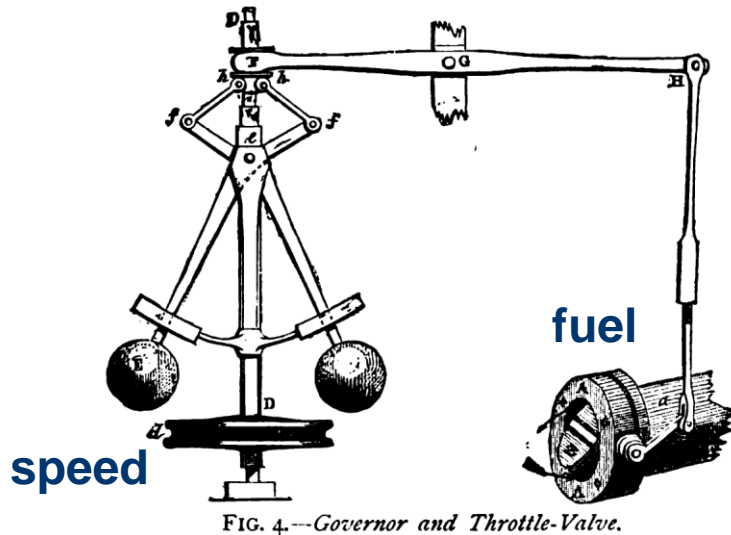


# Final comments

- Steady-state optimal operation may be easily achieved using PID-based control structures
  - Chapters 2,3,4: active constraint switching
  - Chapter 7: optimal setpoints
- Useful to systematically define control objectives, feasibility and tools
  - Priority list of constraints
  - Control structures available for each type of switch (CV-CV, MV-MV, MV-CV)
- Possible to improve performance of PID-based advanced control
  - Chapters 5, 6: design of split range controllers
  - Chapter 8: improved level control

# One final comment

- The “gap” between theory and practice can be in both directions



**Centrifugal governor used in steam engines in the 1780's:**

Proportionally controls fuel flow to maintain engine speed.

Theoretical investigation started about a century later.



# Systematic design of advanced control structures

Thank you for your attention!