

Introduction

Kaibel Arrangements

$V_{min}$  diagram from rigorous simulation

Optimal Operation of  
Kaibel columns

Is it necessary to  
manipulate  $R_V$ ?

Control of Kaibel  
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Our estimation method

Dynamic compensation of static  
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# Optimal Operation of Kaibel Columns

Maryam GHARRDAN

October 24, 2014



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# Thesis Contributions

Chapter 1 Introduction

Chapter 2 a short review on Thermally coupled columns, with focus on Kaibel columns, their design, optimal operation and control.

Chapter 3 Two operation modes

- maximizing the purities in the products with fixed boilup
- minimizing energy with specified product purities

Chapter 4 shortcut design of a Kaibel column using  $V_{min}$  diagram.

Chapter 5 Vapour split as a degree of freedom. Two methods are used to study the effect of vapour split manipulation, namely a shortcut method and rigorous simulations.

Chapter 6 short review of self-optimizing methods.



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**Chapter 7** Control of Kaibel column for the case of maximizing purities of products with fixed boilup.

**Chapter 8** Short review on static estimators.

**Chapter 9** A new class of static estimators for four different scenarios:

- open
- primary variables are controlled
- secondary variables are controlled
- estimation of primary variables are controlled.

**Chapter 10** Control of Kaibel column for specified product composition

**Chapter 11** Dynamic compensation for static estimators



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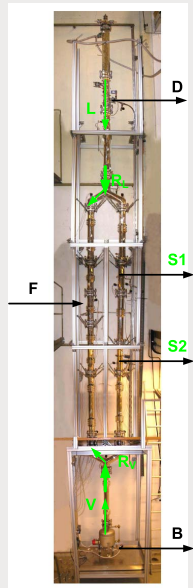
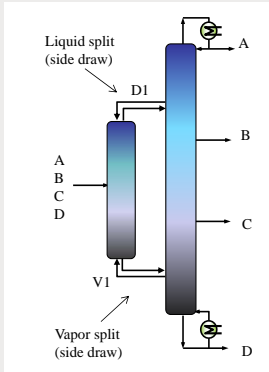
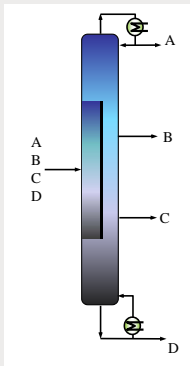
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# DoF

$$u = [ R_L \quad R_V \quad L \quad V \quad S_1 \quad S_2 ]$$



# $V_{min}$ diagram

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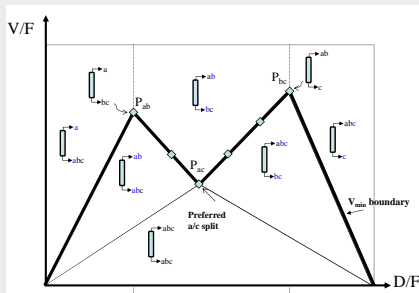
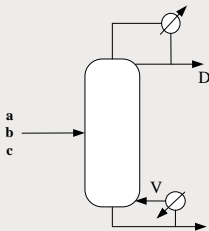


Figure:  $V_{min}$  diagram for a ternary feed



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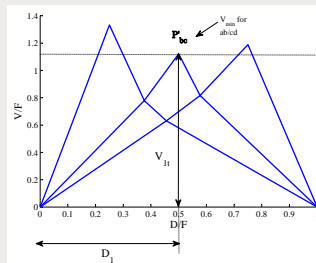
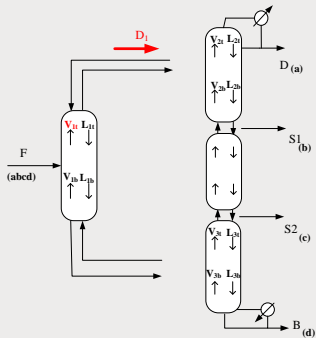
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**Figure:**  $V_{min}$  diagram for the prefractionator of Kaibel distillation column (b/c split)



# $V_{min}$ diagram for Kabel distillation column

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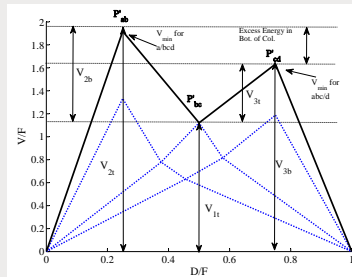
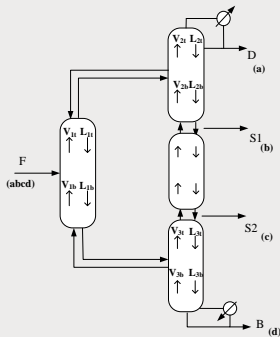
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**Table:** Procedure of making the  $V_{min}$  diagrams from rigorous simulations

Line	Specifications
0 - a/b	$R_{C2,bot} = UB$ , Increase D while $R_{C1,top} < UB$ ,
a/b - a/c	$R_{C1,top} = UB$ , Increase D while $R_{C3,top} < LB$ ,
a/c - b/c	$R_{C3,bot} = UB$ , Increase D while $R_{C2,top} < UB$
b/c - b/d	$R_{C2,top} = UB$ , Increase D while $R_{C4,top} < LB$
b/d - c/d	$R_{C4,top} = UB$ , Increase D while $R_{C3,top} < UB$
c/d - end	$R_{C3,top} = LB$ , Increase D while $R_{C1,bot} < LB$
a/c - a/d	$R_{C1,top} = UB$ , Increase D while $R_{C4,top} < LB$
a/d - b/d	$R_{C4,bot} = UB$ , Increase D while $R_{C2,top} < UB$



# $V_{min}$ from rigorous simulation

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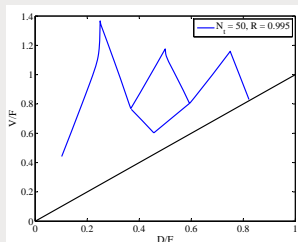
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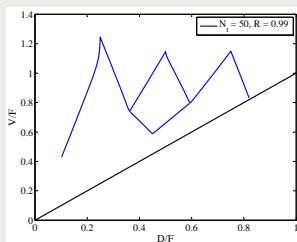
## Estimation

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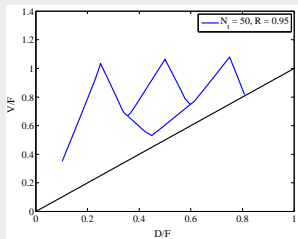
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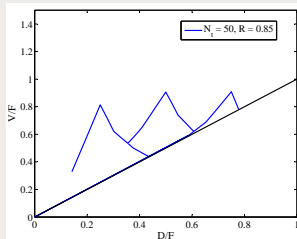
(a)



(b)



(c)



(d)



# Definition of the Objective Function

Two different ways to operate a column:

**Mode 1** Specify the product purities and use the remaining DOF for minimizing the vapor consumption (motivation to introduce thermally-coupled columns)

**Mode 2** Fix the column boilup at the maximum and try to get the most out of the column (when energy is relatively cheap)



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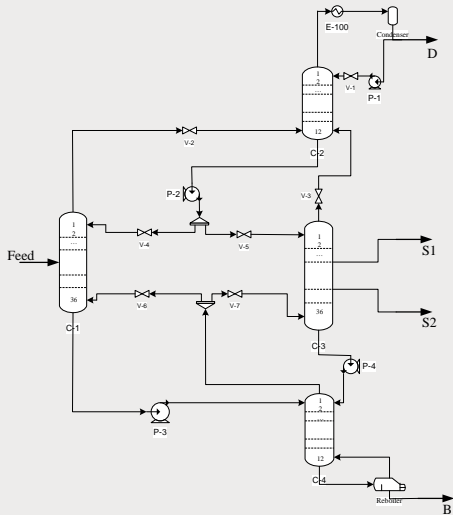


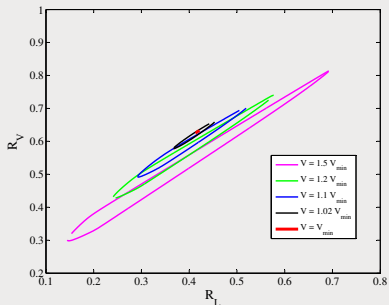
Figure: Simulation flowsheet of Kaibel distillation column

# Mode 1

The optimal values are obtained by plotting the contours manually.

DoF

$$u = \begin{bmatrix} R_L & R_V \end{bmatrix}$$



**Figure:** Contours of constant boilup as a function of vapour and liquid splits at constant product purities



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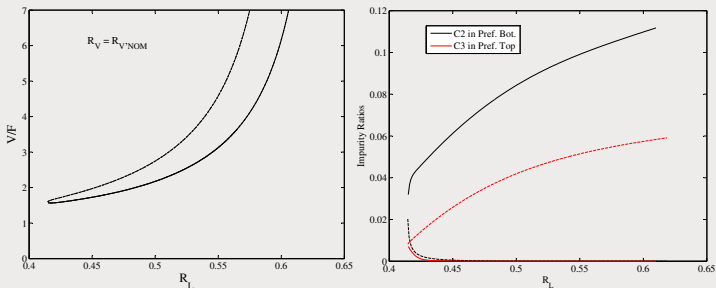
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**Figure:** (Left) Boilup rate as a function of liquid split at constant vapour split and product purities, (Right) Impurities in the top and bottom of prefractionator



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Obs!

Multiplicity is seen in the  
solution

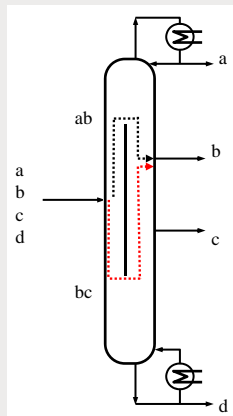


Figure: Paths of impurity flow to  
side streams

# Mode 1: Impurities along a boilup contour

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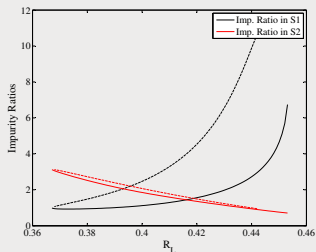
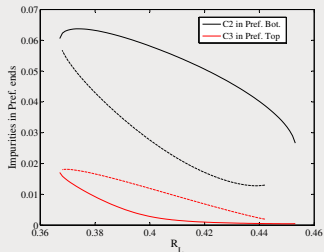
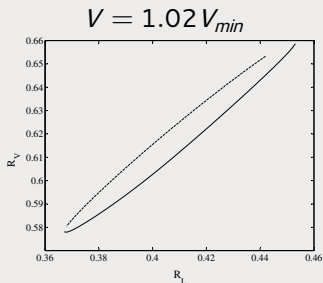
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# Mode 2:

Objective J is to minimize the loss compared to the ideal profit (pure products).

$$J = D(1 - x_D) + S_1(1 - x_{S1}) \\ + S_2(1 - x_{S2}) + B(1 - x_B)$$

DoF

$$u = [ R_L \quad R_V \quad L \quad S_1 \quad S_2 ]$$

Optimization is done in MATLAB using GA method



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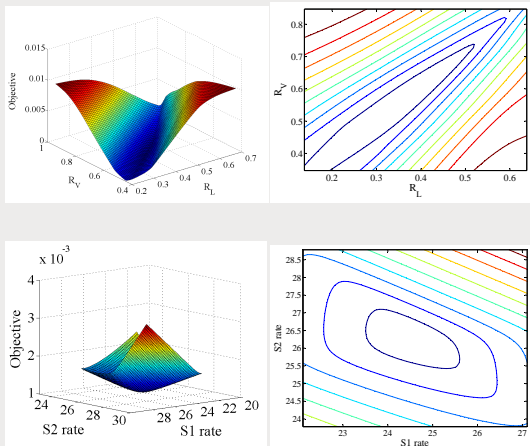
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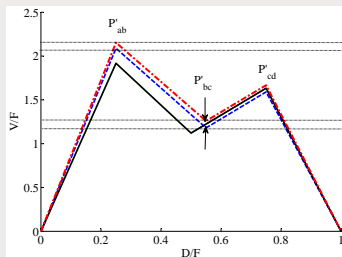
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**Figure:** Mode 2 with fixed boilup: 3-D surfaces and contour plot of impurity sum (cost  $J$ ) as a function of degrees of freedom with the other variables fixed at their optimal values.

$$R_V = R_{V,nom}?$$

$V_{min}$  diagram for the nominal feed properties (black) and new feed composition with optimal (blue) and fixed  $R_V$  (red)



**Figure:** b/c composition change from 0.25/0.25 to 0.30/0.20 with optimal  $R_V = 0.5649$  and fixed  $R_V = 0.5846$



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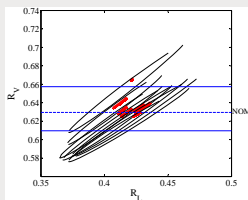
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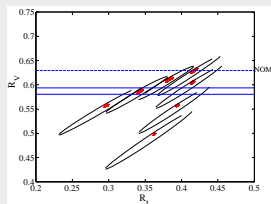
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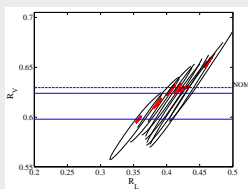
$$R_V = R_{V,nom}?$$



Change in a/b composition



Change in b/c composition



Change in c/d composition

Contours of boilups up to 2% more than minimum energy for different feed composition changes in A/B, B/C and C/D



# Comparison of energy saving for two different vapour split values

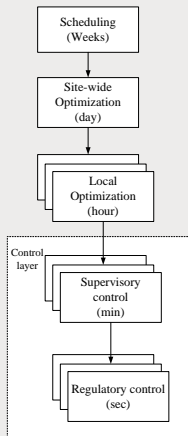
Compositions	$(x_a/x_b)$		$(x_b/x_c)$		$(x_c/x_d)$	
	$R_{V,nom}$	$R_{V,lower}$	$R_{V,nom}$	$R_{V,lower}$	$R_{V,nom}$	$R_{V,lower}$
0.1 / 0.4	0.8%	2.7%	14.2%	8.67%	2.7%	-0.02%
0.15 / 0.35	0.07%	1.41%	6.96%	2%	0.65%	0.5%
0.2 / 0.3	0%	0.96%	0.8%	0.05%	0%	0.97%
0.3 / 0.2	0%	1.1%	0.85%	0.33%	0%	0.67%
0.35 / 0.15	0%	1.12%	3.58%	0.16%	0%	0.68%
0.4 / 0.1	0%	0.8%	6.54%	6.98%	0.5%	1.9%



# General procedure for control structure design

## I Top-down (focus on steady-state economics)

- 1 Define operational objectives (optimal operation):
  - Cost function  $J$  (to be minimized)
  - Constraints
- 2 Objective: Find regions of active constraints
  - Identify steady-state DOF
  - expected disturbances.
  - Optimize the operation wrt the DOF for the expected disturbances (off-line analysis)
  - Select primary controlled variables CV1s (Self-optimizing)
- 3 Select location of throughput manipulator



## II Bottom-up (focus on dynamics) <sup>1</sup>

- ④ Select structure of regulatory control layer (including inventory control):
  - Select 'stabilizing' controlled variables CV2
  - Select inputs (valves) and 'pairings' for controlling CV2 (Decision 4)
    - ① Stabilizes the process and avoids drift
    - ② If possible, use same regulatory layer for all regions
- ⑤ Select structure of supervisory control
  - Controls primary CV1's
  - Supervises regulatory layer
  - Performs switching between CV1s for different regions
- ⑥ Select structure of (or need for) optimization layer (RTO)
  - Updates setpoints for CV1 (if necessary)

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<sup>1</sup>Skogestad, S., 2004, Control Structure Design for Complete Chemical Plants, Computers and Chemical Engineering, 28, 219-234



# Loss Method

## OBJECTIVE

Self-optimizing control is when we can achieve an acceptable loss with constant setpoint values, for the controlled variables in the presence of disturbance and noise.

2

$$L(\mathbf{H}, \mathbf{d}, \mathbf{e}) = \mathbf{J}(\mathbf{u}, \mathbf{d}, \mathbf{e}^x)_{\mathbf{c}=\mathbf{c}^*} - \mathbf{J}(\mathbf{u}^{opt}(\mathbf{d}), \mathbf{d})$$

where  $\mathbf{d}$  and  $\mathbf{e}$  are constrained to satisfy the following inequality

$$\| \begin{bmatrix} \mathbf{d}' & \mathbf{n}^x \end{bmatrix}^T \|_2 \leq 1$$

and  $\mathbf{d} = \mathbf{W}_d \mathbf{d}'$  and  $\mathbf{n}^x = \mathbf{W}_{n^x} \mathbf{n}^{x'}$ .

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<sup>2</sup>Skogestad, S. (2000). Plantwide control: The search for the self-optimizing control structure. *Journal of Process Control* 10, 487-507





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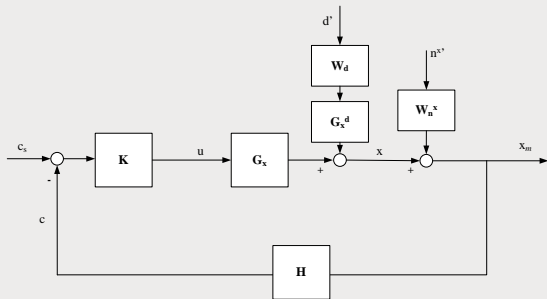
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Assumption: Linear steady-state measurement model,

$$x = \mathbf{G}_x u + \mathbf{G}_x^d d$$

The actual measurements  $x_m$ , containing noise  $n^x$  is

$$x_m = x + n^x$$

The CVs of the form  $c = \mathbf{H}x_m$



$\mathbf{H}$  is found by solving

$$\min_{\mathbf{H}} \left\| \mathbf{J}_{uu}^{1/2} (\mathbf{H}\mathbf{G}_x)^{-1} \mathbf{H}\tilde{\mathbf{F}} \right\|_F^2$$

where  $\tilde{\mathbf{F}} = \begin{bmatrix} \mathbf{F}\mathbf{W}_d & \mathbf{W}_{n^x} \end{bmatrix}$ .

$\mathbf{F}$ : optimal sensitivity matrix. It can be found

- using  $\mathbf{F} = -\mathbf{G}_x \mathbf{J}_{uu}^{-1} \mathbf{J}_{ud} + \mathbf{G}_x^d$
- numerically from its definition  $\mathbf{F} = \frac{dy_{opt}}{dd}$  ✓

$\mathbf{J}_{uu}$  can be difficult to obtain, especially if one relies on numerical methods, and also taking the difference can introduce numerical inaccuracy.



# Mode 2; Control Structure design

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- 5 steady-state DOF: reflux rate, side stream flows, liquid split and vapor split
- Need to find 5 CVs: Single temperatures
- Throughput Manipulator (TPM): column feed
- Assumed that the temperature loops in the upper layer are used for stabilization too
- Disturbances: feed flow rate ( $F$ ), feed composition ( $z_F$ ) and feed liquid fraction ( $q$ ), setpoints of controllers.



# Optimal Profiles in Kaibel Arrangement

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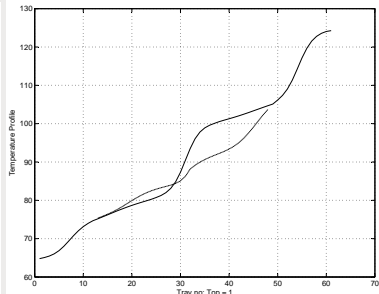
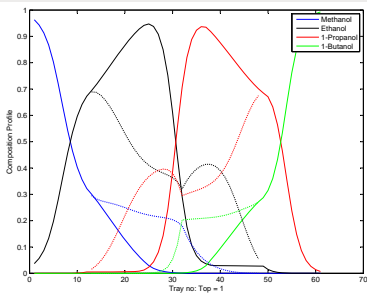
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Optimal composition (left) and temperature (right) profiles



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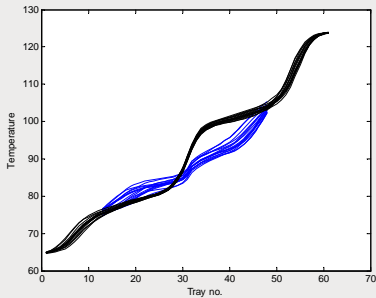
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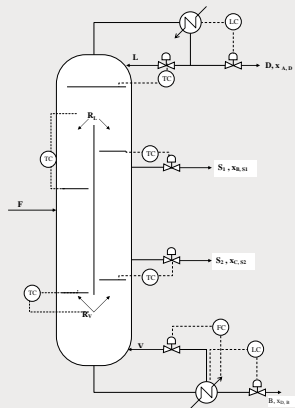
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**Figure:** Optimal temperature profiles  
for disturbances in feed compositions,  
liquid fraction and boilup flow setpoint



# Pairings

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- Avoid pairing on negative steady-state RGA
- Choose pairings corresponding to RGA-elements close to 1
- Prefer pairing on variables with good controllability (=small effective delay).

$$RGA(\mathbf{G}) = \mathbf{G} \times (\mathbf{G}^{-1})^T$$

	$R_l$	$R_v$	$RR$	$Side_1$	$Side_2$
T15	0.31	0.72	0.49	-0.06	-0.47
T36	-0.74	0.42	10.37	0.33	-9.38
T39	2.18	-0.78	4.16	-1.50	-3.07
T54	-1.13	0.77	-4.22	2.31	3.27
T75	0.38	-0.13	-9.81	-0.08	10.64



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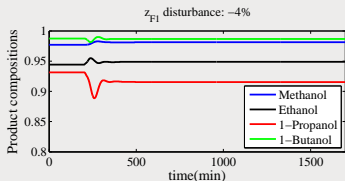
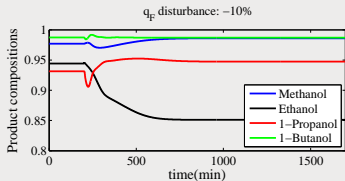
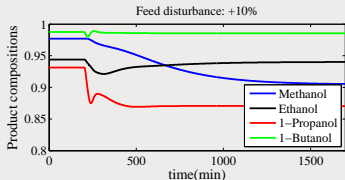
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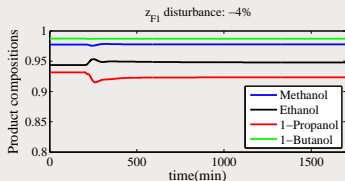
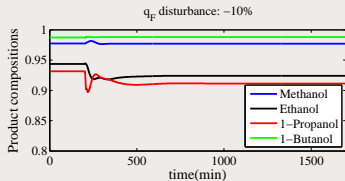
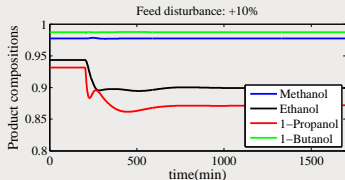
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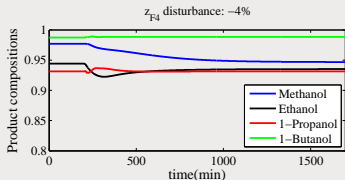
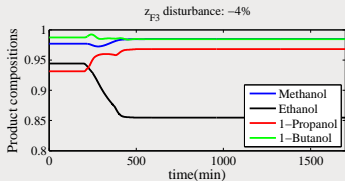
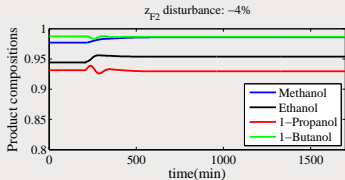
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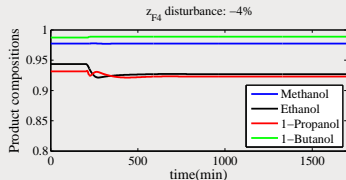
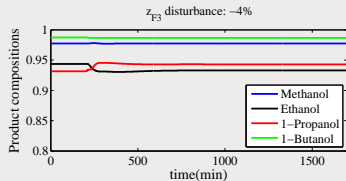
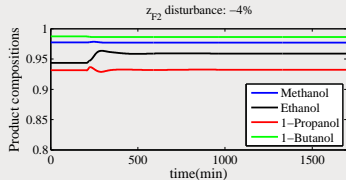
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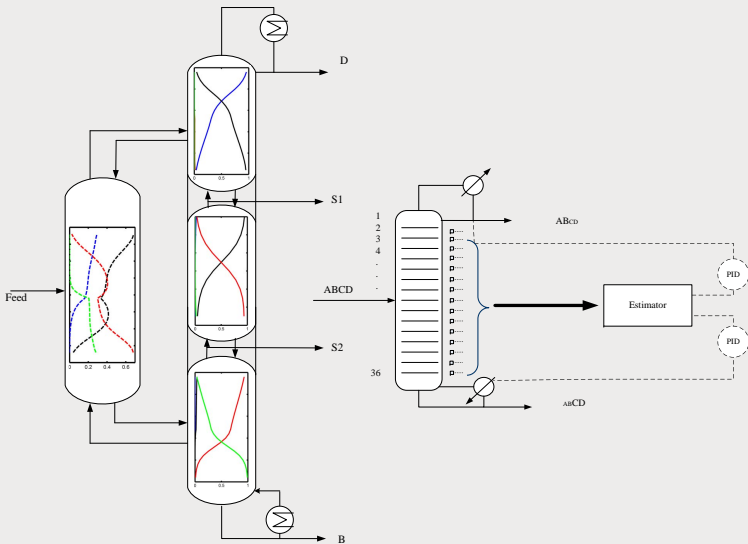
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## OBJECTIVE

The main objective is to find a linear combination of measurements such that keeping these constant indirectly leads to nearly accurate estimation with a small loss  $L$  in spite of unknown disturbances,  $d$ , and measurement noise,  $n^X$ .

$$\min_H \|e\|_2 = \|y - \hat{y}\|_2$$



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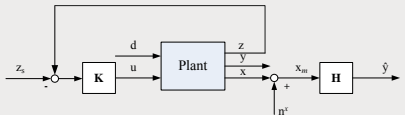
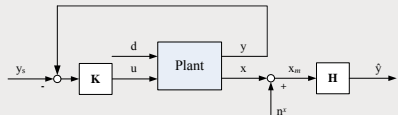
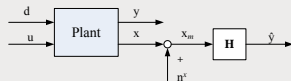
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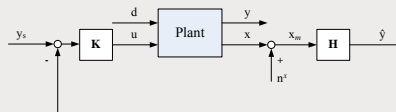
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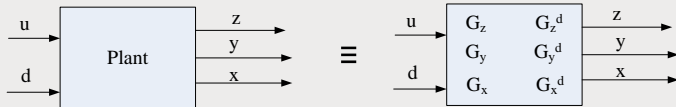
- "Open-loop" (for Monitoring of  $\hat{y}$ )
  - 1 No control ( $u$  is a free variable)
  - 2 Primary variables  $y$  are controlled ( $u$  is used to keep  $y = y_s$ ).
  - 3 Secondary variables  $z$  are controlled ( $u$  is used to keep  $z = z_s$ ).



- "Closed-loop" (for Control of  $\hat{y}$ )



# Our Static Estimator



- 1 Assumption: Linear models for the primary variables  $y$ , measurements  $x$ , and secondary variables  $z$

$$y = \mathbf{G}_y u + \mathbf{G}_y^d d \quad x = \mathbf{G}_x u + \mathbf{G}_x^d d \quad z = \mathbf{G}_z u + \mathbf{G}_z^d d$$

$$\mathbf{G}_y = \left( \frac{\partial y}{\partial u} \right)_d, \mathbf{G}_y^d = \left( \frac{\partial y}{\partial d} \right)_u, \dots$$

- 2 The actual measurements  $x_m$ , containing measurement noise  $\mathbf{n}^x$  is  $x_m = x + \mathbf{n}^x$
- 3 The linear estimator is of the form  $\hat{y} = \mathbf{H}x_m$



# Optimal estimators for different scenarios

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"Open-loop" 1

$$H_1 = Y_1 X_1^\dagger$$

$$Y_1 = \begin{bmatrix} G_y W_u & G_y^d W_d & 0 \end{bmatrix}$$

$$X_1 = \begin{bmatrix} G_x W_u & G_x^d W_d & W_{n^x} \end{bmatrix}$$

"Open-loop" 2

$$H_2 = Y_2 X_2^\dagger$$

$$Y_2 = \begin{bmatrix} W_{y_s} & 0 & 0 \end{bmatrix}$$

$$X_2 = \begin{bmatrix} G_x^{cl} W_{y_s} & F W_d & W_{n^x} \end{bmatrix}$$

"Open-loop" 3

$$H_3 = Y_3 X_3^\dagger$$

$$Y_3 = \begin{bmatrix} G_y^{cl} W_{z_s} & F'_y W_d & 0 \end{bmatrix}$$

$$X_3 = \begin{bmatrix} G_x^{cl} W_{z_s} & F'_x W_d & W_{n^x} \end{bmatrix}$$

"Closed-loop"

$$\min_H \left\| H \begin{bmatrix} F W_d & W_{n^x} \end{bmatrix} \right\|_F$$

$$\text{s.t. } H G_x = G_y$$



# H values

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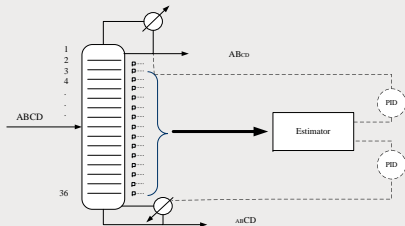
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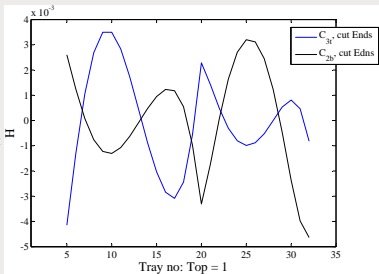
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$$\begin{bmatrix} \Delta \hat{y}_1 \\ \Delta \hat{y}_2 \end{bmatrix} = H$$



$\times$

$$\begin{bmatrix} \Delta T_5 \\ \Delta T_6 \\ \Delta T_7 \\ \Delta T_8 \\ \vdots \\ \Delta T_{32} \end{bmatrix}$$



# Open-loop estimation (S1)

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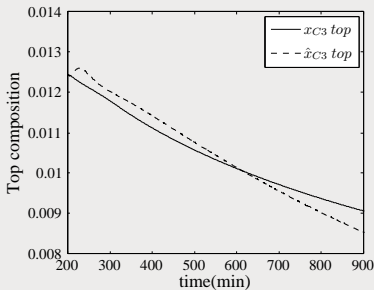


Figure: Top estimate with -1 percent change in boilup

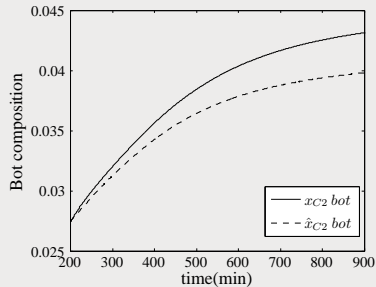


Figure: Bot estimate with -1 percent change in boilup



# Open-loop estimation (S3)

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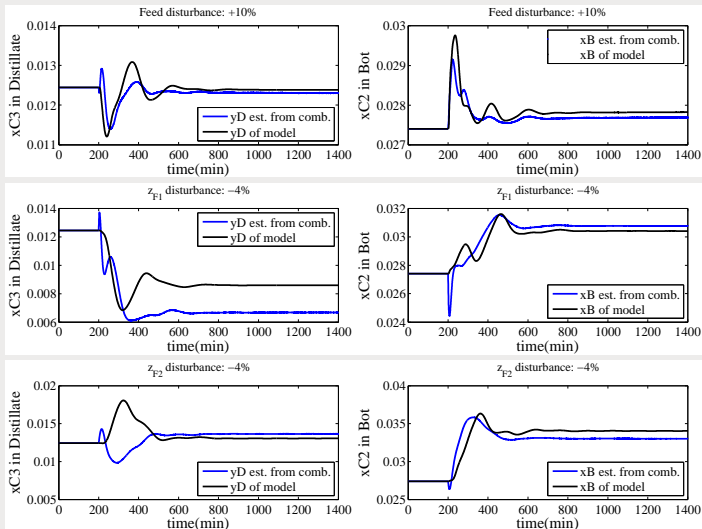
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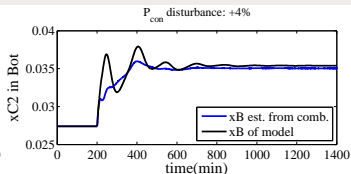
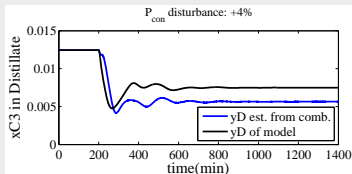
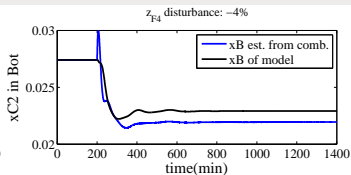
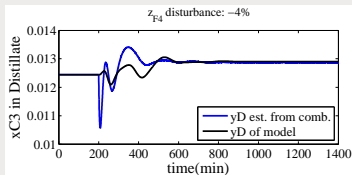
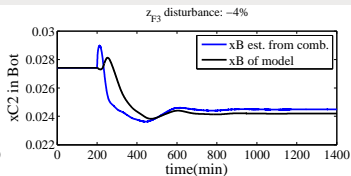
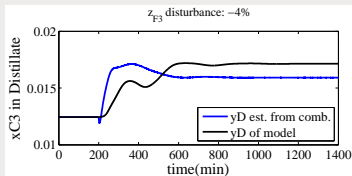
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# OL estimation (S3) (contd.)



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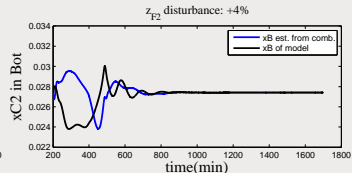
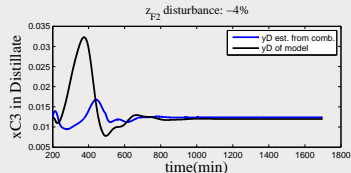
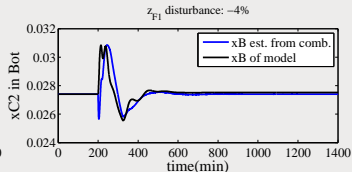
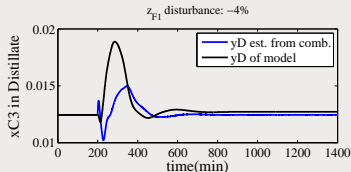
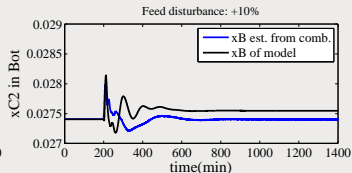
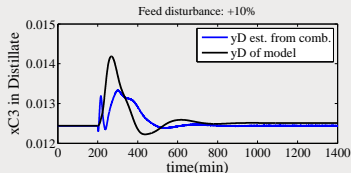
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# Closed-loop estimation (S4)



# Closed-loop estimation (S4)

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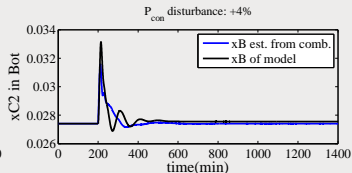
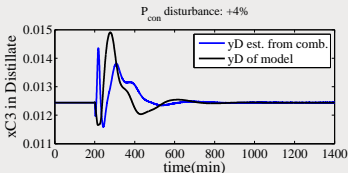
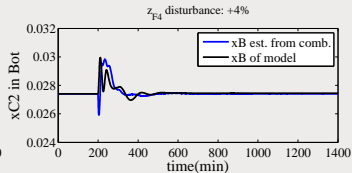
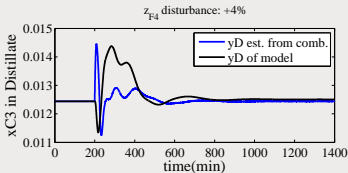
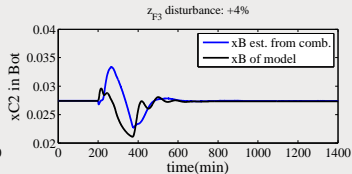
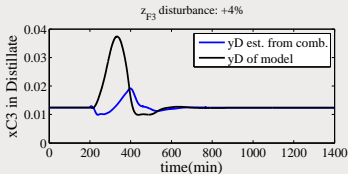
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# Improving dynamic performance

The fast dynamics of measurements with negative contributions may lead to inverse response (RHP zero in the transfer function from  $u$  to  $CV$ )

- Cascade Control:  
Close a fast inner loop and adjust the setpoint on a time scale which is slower than the RHP-zero.
- Use of measurements from the same section of the process:  
Selected measurements are similar, then it is less likely to get RHP-zero. However, this gives a larger steady-state error.
- Filters:  
The Low-pass filters will keep the system optimal at steady state.

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## Example

$$\mathbf{G}_x = \begin{bmatrix} \frac{1}{3s+1} \\ \frac{1}{s+1} \end{bmatrix}$$

and the optimal matrix  $\mathbf{H}$  is

$$\mathbf{H} = \begin{bmatrix} 2 & -1 \end{bmatrix}$$

the transfer function from  $u$  to  $\hat{y}$  is

$$\mathbf{G} = \mathbf{H}\mathbf{G}_x = \frac{2}{3s+1} - \frac{1}{s+1} = \frac{1-s}{(3s+1)(s+1)} \approx \frac{e^{-1.5s}}{3.5s+1}$$

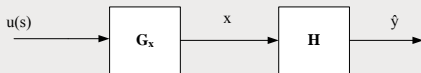


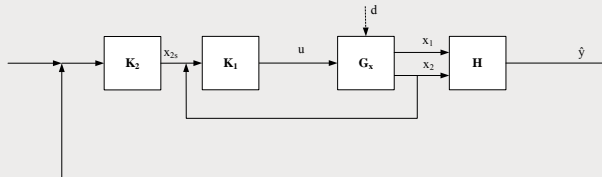
Figure: Block diagram of the estimation



## Theorem

*Cascade (inner-loop) can not move the zero of  $HG_x$*

**Proof.**



By performing the loop calculations, the transfer function from  $x_{2s}$  to  $\hat{y}$  is

$$\hat{y} = \left( h_2 + h_1 \frac{g_1}{g_2} \right) \frac{kg_2}{1 + kg_2} x_{2s} \quad (1)$$

The term  $(h_1 g_1 + h_2 g_2)$ , which includes the RHP zero, is unchanged.



# Filtering

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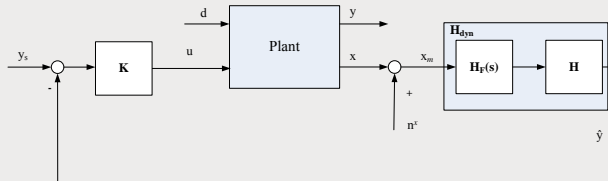
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**Figure:** Block diagram of the estimation system including filter ( $H_F$ )

$$H_F = \begin{bmatrix} \frac{1}{\tau_{F1}s+1} & 0 \\ 0 & \frac{1}{\tau_{F2}s+1} \end{bmatrix}$$

$$H_F(0) = I$$



Some Filters:

$$\mathbf{H}_{F1} = \begin{bmatrix} \frac{1}{s+1} & 0 \\ 0 & \frac{1}{3s+1} \end{bmatrix}$$

$$\mathbf{H}_{F2} = \begin{bmatrix} 1 & 0 \\ 0 & \frac{s+1}{3s+1} \end{bmatrix}$$

$$\mathbf{H}_{F3} = \begin{bmatrix} \frac{3s+1}{s+1} & 0 \\ 0 & 1 \end{bmatrix}$$

$$\mathbf{H}_{F4} = \begin{bmatrix} 1 & 0 \\ 0 & \frac{1}{3s+1} \end{bmatrix}$$

The filtered transfer function will  
be

$$\mathbf{H}_{dyn1} \mathbf{G}_x = \frac{1}{(3s+1)(s+1)}$$

$$\mathbf{H}_{dyn2} \mathbf{G}_x = \frac{1}{3s+1}$$

$$\mathbf{H}_{dyn3} \mathbf{G}_x = \frac{1}{s+1}$$

$$\mathbf{H}_{dyn4} \mathbf{G}_x = \frac{2s+1}{(3s+1)(s+1)}$$

Using Lead-lag compensators, we can make the response as fast as we want.





# Distillation case-study

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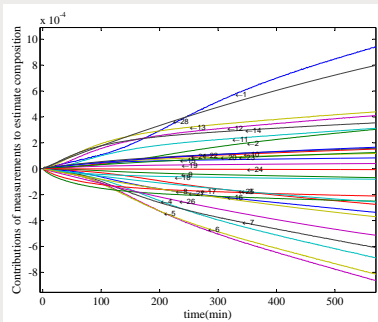
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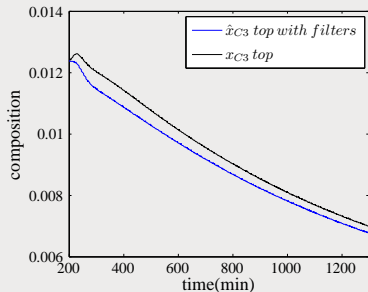
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**Figure:**  $HG_X(t)$  with -1% change in boilup and constant Reflux ratio



**Figure:** Estimated composition (tf =  $HG_X$ ) and filtered estimated composition (tf =  $HH_F G_X$ ) where there are filters only on 6th, 16th and 17th measurements



# Optimizing filters

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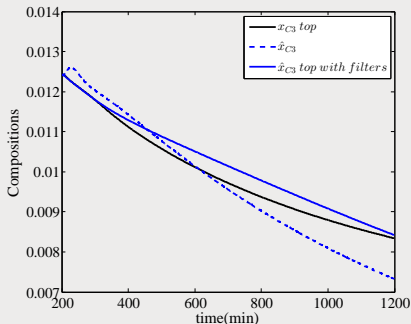
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$$\min_{\mathbf{H}_F} \|\mathbf{H}\mathbf{H}_F \mathbf{G}_X - \mathbf{G}_{ref}\|$$



**Figure:** Real composition, Estimated composition ( $tf = \mathbf{H}\mathbf{G}_X$ ) and filtered estimated composition ( $tf = \mathbf{H}\mathbf{H}_F \mathbf{G}_X$ ) where filters are optimized for first 100 min. assuming  $G_{ref} = G_{u \rightarrow y_1}$



# Explicit solution for the filter problem

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## Approach:

Convert the model matching problem to Nehari problem

$$\|T_1 - T_2 Q T_3\|_\infty \Rightarrow \|R - X\|_\infty = \|\Gamma_R\|$$

- In our case we have  $T_3 = I$
- An optimal  $Q$  exists if the ranks of the two matrices  $T_2(j\omega)$  and  $T_3(j\omega)$  are constant for all  $0 < \omega < \infty^3$ .

---

<sup>3</sup>Francis1987.



# Scalar-valued case

**Step 1** Perform inner-outer factorization for  $T_2$

**Step 2**  $R = [A, B, C, 0]$  ( $A$  antistable) +  $R_2$  (in  $RH_\infty$ )

**Step 3** The controllability and observability grammians are the solutions of

$$AL_c + L_c A^T = BB^T$$

$$A^T L_o + L_o A = C^T C$$

**Step 4** Having  $\lambda^2 =$ largest eigenvalue of  $L_c L_o$  and the corresponding eigenvector ( $\omega$ ), define

$$f(s) := [A, \omega, C, 0]$$

$$g(s) := [-A^T, \lambda^{-1} L_o \omega, B^T, 0]$$

**Step 5**  $X = R - \lambda \frac{f}{g}$

**Step 6**  $Q = T_{2o}^{-1} X$

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## Example

In our example, we have the following inputs:

$$T_1 = \frac{1}{0.5s + 1} : \text{Desired transfer function } (\mathbf{G}_{ref})$$

$$T_2 = \frac{-s + 1}{3s^2 + 4s + 1} \text{Current transfer function } (\mathbf{HG}_x)$$

Since the rank of  $T_2$  is not constant for all  $0 \leq \omega \leq \infty$ , a transfer function

$$\mathbf{V} = (s + 1)^l$$
$$\mathbf{Q} = \frac{19.82s^2 + 2042s + 678.5}{s^2 + 1002s + 2000}$$



# Matrix-valued case

The general algorithm to obtain  $\mathbf{Q}$  is as follows

**Step 1** Find a minimal realization of  $\mathbf{R}$ :  $\mathbf{R}(s) = [\mathbf{A}, \mathbf{B}, \mathbf{C}, 0]$

**Step 2** Solve the Lyapunov equations to find controllability and observability gramians and set  $\mathbf{N} = (\mathbf{I} - \mathbf{L}_o \mathbf{L}_c)^{-1}$

**Step 3** Set

$$\mathbf{L}_1(s) = \begin{bmatrix} \mathbf{A} & -\mathbf{L}_c \mathbf{N} \mathbf{C}^T & \mathbf{C} & \mathbf{I} \end{bmatrix}$$

$$\mathbf{L}_2(s) = \begin{bmatrix} \mathbf{A} & \mathbf{N}^T \mathbf{B} & \mathbf{C} & \mathbf{0} \end{bmatrix}$$

$$\mathbf{L}_3(s) = \begin{bmatrix} -\mathbf{A}^T & \mathbf{N} \mathbf{C}^T & -\mathbf{B}^T & \mathbf{0} \end{bmatrix}$$

$$\mathbf{L}_4(s) = \begin{bmatrix} -\mathbf{A}^T & \mathbf{N} \mathbf{L}_o \mathbf{B}^T & \mathbf{B}^T & \mathbf{I} \end{bmatrix}$$

**Step 4** Select  $\mathbf{Y}$  in  $RH_\infty$  with  $\|\mathbf{Y}\|_\infty \leq 1$  (for example  $\mathbf{Y} = 0$ ) and set  $\mathbf{X} = \mathbf{R} - (\mathbf{L}_1 \mathbf{Y} + \mathbf{L}_2)(\mathbf{L}_3 \mathbf{Y} + \mathbf{L}_4)$



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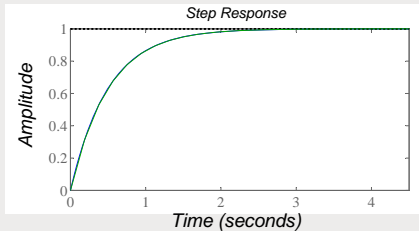
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# Example

$$T_1 = \frac{1}{0.5s + 1}, T_2 = \begin{bmatrix} 2 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} \frac{1}{3s+1} \\ \frac{1}{s+1} \end{bmatrix}$$

$$Q = \begin{bmatrix} \frac{0.92308(s+2)^2(s+0.67)(s+0.3333)(s-0.9431)^2(s-1)}{(s+2)^3(s+0.67)(s+0.6202)(s-0.6202)(s-0.9431)^2} \\ \frac{-1.3846(s+2)^2(s+0.67)(s+0.3333)(s-0.3333)(s-0.9431)^2}{(s+2)^3(s+0.67)(s+0.6202)(s-0.6202)(s-0.9431)^2} \end{bmatrix}$$



# Kaibel column control

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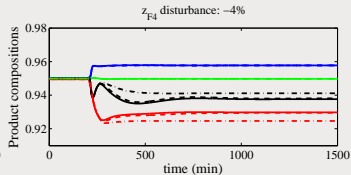
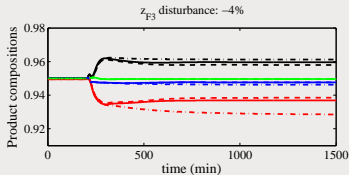
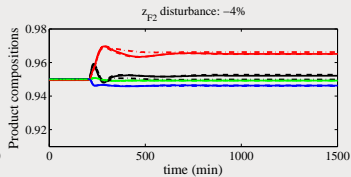
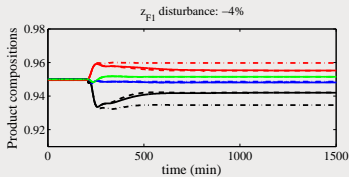
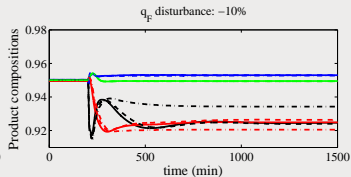
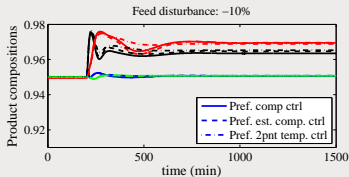
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# Concluding Remarks

- Kaibel distillation columns can save operational costs if operated optimally
- $V_{min}$  diagrams are very useful tools for design, analysis and operation of columns
- It's important to control the key component flows out of the prefractionator
- Combination of measurement will result in lower estimation error compared to using single measurements
- It's possible to have dynamic issues in the estimators which stems from combining measurements from different sections
- Dynamic issues can be alleviated by cascade control, combining subset of measurements or applying filters

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# Optimal Operation of Kaibel Columns

Maryam GHADRAN

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Thanks for your attention