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Abstract: This paper discusses the application of the plantwide control design procedure of Skogestad (2004a) to the ammonia synthesis process. Three modes of operation are considered: (I) Given feed rate, (IIa) Maximum throughput, and (IIb) "Optimized" throughput. Two control structures, one for Mode I and another for Mode IIb, are proposed. In Mode I, it is proposed to keep constant purge rate and compressor powers. There is no bottleneck in the process, and thus there is no Mode IIa of operation. In Mode IIb, the compressors are at their maximum capacity and it is proposed to adjust the feed rate such that the inert concentration is constant. The final control structures result in good dynamic performance.

To: Editorial office, Computers and Chemical Engineering

From: Sigurd Skogestad Dept. of Chemical Engineering Norwegian University of Science and Technology N-7491 Trondheim, Norway Email: skoge@chemeng.ntnu.no

February 28, 2008

Dear Sirs:

We would like to thank the reviewers for many useful comments. Most of them have been implemented and have markedly improved the quality of the revised paper.

The paper has been revised based on the reviewers' comments and our answers are given below.

Reply to reviewer #1:

Reviewer #1 has made two very nice points. However, in order to limit the scope of the paper, we have chosen to study the synthesis section separately. Moreover, we agree with the reviewer that the inclusion of a more detailed reactor model, which is open-loop unstable, would have been nice, but this would not change the main results in this paper on selection of controlled variables, because they are based on steady-state economics.

In addition, the entire manuscript was grammatically revised to ensure a typo-free text.

Reply to reviewer #2:

Reactor model information: This a very appropriate comment from reviewer #2 and we added an Appendix with more details on the Aspen PlusTM implementation of the reactor model. Moreover, the reader now can have the Aspen PlusTM by accessing Sigurd's home page at http://www.nt.ntnu.no/users/skoge/, as pointed in the Appendix.

Reactor inlet/outlet temperature responses and time unit in the plots: The reactor temperature responses are not shown, but they perform nicely with a maximum change of about 8°C. We decided not to include these plots and instead comment on the temperature responses. Furthermore, the time unit used in the plots is now properly stated.

Reply to reviewer #3:

References on optimization of ammonia plants: The reviewer has put it wisely that there should be references correlating our findings with results from other papers. This could be possible, but we have not found any such references.

Source of Figure 1 and Table 1: Figure 1 is indeed a simplified version of the process currently in operation at Norsk Hydro, Norway. The reactor configuration is due to Morud and Skogestad, 1998. The stream table results corresponding to the nominally optimal operating point are calculated in the Optimization section of the paper. Those very nice points are now clear in the text.

Unused manipulated variables in Table 2: As nicely pointed by the reviewer, there is a misreading in Table 2. When it says that the status is "steady-state" the reader may think it is not changed dynamically. Actually, these variables are varied to keep the selected controlled variables at their steady-state optimum values. Table 2 is now corrected to reflect this change.

Minimum singular value formula: The motivation for the minimum singular value formula is now given as well as a more clear definition of the Hessian matrix J_{uu} .

Range of the minimum singular value in Table 7: This is indeed a good point. We included in the text some comments on this respect, and added an instance of a typical set of candidates that one might think is a good one, namely, the reactor inlet pressure, the feed compressor power, and the mole fraction of methane in the purge. However, such a set would likely give a large loss since its minimum singular value is 10 times smaller than the values in Table 7.

Controller tuning tables: Although we mentioned that Table 13 was sorted by the time constant of the loops in ascending order, we did not show the values of these time constants. Indeed, they are not part of the table and we decided not to show them in the text.

Is multiloop control "easy" or "hard"?: This is actually a very good question. We included in the text that although multivariable control would improve the performance, we find that the dynamic performance with our decentralized control configuration is pretty much acceptable, as seen from Figures 9 to 15.

Additional comments from the authors:

We made some additional changes on the paper. More specifically, we added the following comments on the manuscript:

- In the of Controller Tuning section we emphasized that there is no need for supervisory control in Mode 1 (given feed) because the purge flow (Y6) and the two compressor powers (Y3 and Y4) are simply set constant.
- In Table 14 the column corresponding to Mode I was deleted since there is no supervisory control for this case.
- In the Identification of Candidate Controlled Variables for Mode IIb section we made a remark that that the purge flow rate (Y6) is not included in any of the ten best sets, whereas it was included in all the ten best sets in mode I (with given feed).
- As for the steady-state optimization degrees of freedom for both Modes I and IIb we include in the text that the steady-state optimization was performed with all 8 (Mode I) or 9 (Mode IIb)

steady-state degrees of freedom. However, during implementation we fixed the inlet temperature to the reactor and the split fractions to the three interstage cooling flows at their nominally optimal value (3 variables). This is in accordance with industrial practice, but could be reconsidered if the resulting economic loss is not acceptable. Furthermore, we found that the two cooling duties were optimally at their upper constraints in both cases, so these should be implemented as active constraints (2 variables). In case II, the two compressors were also optimally at their maximum values (2 variables). We were then left with 3 (Mode I) or 2 (Mode IIb) degrees of freedom for which we had to find associated controlled variables.

Control structure design for the ammonia synthesis process

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Abstract

This paper discusses the application of the plantwide control design procedure of Skogestad (2004*a*) to the ammonia synthesis process. Three modes of operation are considered: (I) Given feed rate, (IIa) Maximum throughput, and (IIb) "Optimized" throughput. Two control structures, one for Mode I and another for Mode IIb, are proposed. In Mode I, it is proposed to keep constant purge rate and compressor powers. There is no bottleneck in the process, and thus there is no Mode IIa of operation. In Mode IIb, the compressors are at their maximum capacity and it is proposed to adjust the feed rate such that the inert concentration is constant. The final control structures result in good dynamic performance.

Key words:

Ammonia plant, control structure, top-down analysis, bottom-up design, bottleneck, throughput, primary controlled variable, secondary controlled variables, manipulable variables.

1 Introduction

There are hundreds of references on the ammonia synthesis process that discuss the various aspects of its operation and design but none addresses the issue of control structure design in a systematic manner. In this paper, we consider the application of the plantwide control structure design procedure of Skogestad (2004a) to an ammonia synthesis process. We start with a top-down analysis of the process where we define the operational objectives (identification of a scalar cost function and operational constraints) and identify the dynamic and steady-state (economic) degrees

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of freedom. This is followed by the identification of the most important disturbances to the process. Based on all of this information, we proceed by selecting the controlled variables that gives optimal operation [variables that are active at their constraints, (Maarleveld and Rijnsdorp, 1970)] and use the self-optimizing control technique (Skogestad, 2000) to decide for the remaining unconstrained controlled variables so that near-optimal operation is achieved without the need to re-optimize when disturbances occur.

One important issue in the plantwide control procedure is the definition on where in the plant the production rate should be set. We distinguish between 3 modes of operation:

- **Mode I: Given throughput**. This mode of operation occurs when (a) the feed rate is given (or limited) or (b) the production rate is given (or limited, e.g. by market conditions). The operational goal is then to minimize utility (energy) consumption, that is, to maximize efficiency.
- Mode II: Throughput as a degree of freedom. We here have two cases:
 - Mode IIa: Maximum throughput. This mode encompasses feasibility issues and the maximum throughput does not depend on cost data. It occurs when the product prices are sufficiently high and feed is available.
 - **Mode IIb: "Optimized" throughput**. In some cases, it is not optimal economically to maximize throughput, even if feed is available. This happens if the profit reaches a maximum, for example, because purge streams increase sharply at high feed rates.

The mode in which a given process will operate depends on market conditions and in which way the plant responds to increasing production rate.

The bottom-up design aims at defining the structure of the regulatory and supervisory control layers. The optimization (RTO) layer is not considered in this paper since we assume that near-optimal operation is satisfactory as long as the loss between the truly optimal and the near-optimal (with constant set point policy for the unconstrained variables) is acceptable. The main purpose of the regulatory control layer is "stabilization" such that the plant does not drift too far away from its nominal operating point and it also should make the operation of the supervisory control layer smooth such that disturbances on the primary outputs can be handle effectively. The most important issue in the design of the regulatory layer is the selection of good secondary controlled variables and the pairing of these with the inputs at this layer.

With the regulatory layer in place, we then proceed to the design of the supervisory control layer. The purpose of this layer is to keep the primary (economic) controlled variables at their optimal set points using as degrees of freedom (inputs) the set points for the regulatory layer and any unused input at the supervisory layer. The main decisions involved in this layer are related to configuration of the control system, that is, the use of decentralized or multivariable (MPC) control.

A validation step is also included in the procedure in order to evaluate the effectiveness of the proposed control structure against disturbances using dynamic simulation.

For the ammonia plant, we will apply this procedure from a practical perspective in order to illustrate its applicability to actual industrial plants.

To limit the scope of the paper, we have chosen to study the synthesis section separately and do not consider the reaction section of the process. However, for Modes IIa and IIb (feed rate is a degree of freedom), we assume that there is available capacity in the synthesis gas section.

2 The ammonia synthesis process

We here consider the ammonia synthesis process given in Figure 1 which is a simplified version of an actual industrial plant. The reactor configuration is from Morud and Skogestad (1998). The stream table results corresponding to the nominally optimal operating point computed using AspenTM are given in Table 1.



Fig. 1. Ammonia synthesis flowsheet.

table for the nomi	inally o	ptimal	operat	ing po	oint for	r the a	mmon	ia synt	thesis	proces	s. See	Figure	e 1 for	the st	ream n	lames.		
Stream	1	2	3	4	5	9	7	8	6	10	11	12	13	14	15	16	17	18
Temperature (°C)	231.7	231.8	340.1	231.7	231.7	231.7	231.8	231.8	231.8	306.3	456.2	420.1	452.1	423.9	449.3	394.4	296.9	107.6
Pressure (bar)	203.194	204.957	203.96	206.957	206.957	206.957	203.957	202.957	201.857	203.957	202.957	202.957	201.857	201.857	200.757	199.76	198.76	197.76
Vapor Frac	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
Mole Flow (kmol/h)	40573.8	20449.2	20449.2	5152.87	5639.75	9331.97	9331.97	5639.75	5152.87	29781.2	27046.4	32686.1	32002	37154.8	36531.7	36531.6	36531.6	36531.6
Mass Flow (kg/h)	412598	207950	207950	52400	57351.2	94897.6	94897.6	57351.2	52400	302848	302848	360199	360199	412599	412599	412598	412598	412598
Enthalpy (Mkcal/h)	-22.911	-11.547	5.95	-2.91	-3.185	-5.27	-5.27	-3.185	-2.91	0.68	0.68	-2.504	-2.504	-5.414	-5.414	-22.912	-53.546	-112.78
Mole Flow (kmol/h)																		
Hydrogen	25329.8	12766.2	12766.2	3216.88	3520.84	5825.84	5825.84	3520.84	3216.88	18592	14489.8	18010.7	16984.4	20201.3	19266.5	19266.5	19266.5	19266.5
Nitrogen	7432.32	3745.89	3745.89	943.904	1033.09	1709.43	1709.43	1033.09	943.904	5455.32	4087.92	5121.01	4778.92	5722.82	5411.25	5411.23	5411.23	5411.23
Methane	1341.71	676.221	676.219	170.397	186.497	308.593	308.593	186.497	170.397	984.812	984.812	1171.31	1171.31	1341.71	1341.71	1341.7	1341.7	1341.7
Argon	943.356	475.452	475.45	119.806	131.127	216.972	216.972	131.127	119.806	692.422	692.422	823.549	823.549	943.355	943.355	943.351	943.351	943.351
Ammonia	5526.63	2785.42	2785.48	701.882	768.202	1271.13	1271.13	768.202	701.882	4056.61	6791.41	7559.61	8243.79	8945.68	9568.82	9568.82	9568.82	9568.82
Water	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Mole Frac																		
Hydrogen	0.624	0.624	0.624	0.624	0.624	0.624	0.624	0.624	0.624	0.624	0.536	0.551	0.531	0.544	0.527	0.527	0.527	0.527
Nitrogen	0.183	0.183	0.183	0.183	0.183	0.183	0.183	0.183	0.183	0.183	0.151	0.157	0.149	0.154	0.148	0.148	0.148	0.148
Methane	0.033	0.033	0.033	0.033	0.033	0.033	0.033	0.033	0.033	0.033	0.036	0.036	0.037	0.036	0.037	0.037	0.037	0.037
Argon	0.023	0.023	0.023	0.023	0.023	0.023	0.023	0.023	0.023	0.023	0.026	0.025	0.026	0.025	0.026	0.026	0.026	0.026
Ammonia	0.136	0.136	0.136	0.136	0.136	0.136	0.136	0.136	0.136	0.136	0.251	0.231	0.258	0.241	0.262	0.262	0.262	0.262
Water	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Stream	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	FEED]	PURGE
Temperature (°C)	27.1	40.5	40.4	40.4	48	40.4	40.4	40.5	17	304.2	15	15.1	144.7	15	15.1	82.9	17	40.2
Pressure (bar)	196.76	196.284	195.284	195.284	207.957	195.284	195.284	190.284	23.1	196.284	10	S	4	10	5	4	23.1	190.284
Vapor Frac	0.81	0.907	1	1	1	1	0	0.001	1	1	0	0	0.456	0	0	0	1	1
Mole Flow (kmol/h)	36531.6	44750.2	40578	40573.8	40573.8	4.257	4172.14	4172.14	8218.57	8218.57	4440.68	4440.68	4440.68	38855.9	38855.9	38855.9	8218.57	4.257
Mass Flow (kg/h)	412598	483598	412641	412598	412598	43.294	70956.9	70956.9	71000	71000	80000	80000	80000	700000	700000	700000	71000	43.294
Enthalpy (Mkcal/h)	-164.1	-148.04	-84.485	-84.477	-82.14	-0.009	-63.552	-63.552	-0.961	16.065	-306.04	-306.04	-275.4	-2677.8	-2677.8	-2626.5	-0.96	-0.009
Mole Flow (kmol/h)																		
Hydrogen	19266.5	25390.2	25332.4	25329.8	25329.8	2.658	57.707	57.707	6123.66	6123.66	0	0	0	0	0	0	6123.66	2.658
Nitrogen	5411.23	7454.37	7433.11	7432.33	7432.32	0.78	21.261	21.261	2043.14	2043.14	0	0	0	0	0	0	2043.14	0.78
Methane	1341.7	1368.82	1341.85	1341.71	1341.71	0.141	26.97	26.97	27.121	27.121	0	0	0	0	0	0	27.121	0.141
Argon	943.351	968.007	943.46	943.361	943.356	0.099	24.547	24.547	24.656	24.656	0	0	0	0	0	0	24.656	0.099
Ammonia	9568.82	9568.82	5527.16	5526.58	5526.63	0.58	4041.66	4041.66	0	0	0	0	0	0	0	0	0	0.58
Water	0	0	0	0	0	0	0	0	0	0	4440.68	4440.68	4440.68	38855.9	38855.9	38855.9	0	0
Mole Frac																		
Hydrogen	0.527	0.567	0.624	0.624	0.624	0.624	0.014	0.014	0.745	0.745	0	0	0	0	0	0	0.745	0.624
Nitrogen	0.148	0.167	0.183	0.183	0.183	0.183	0.005	0.005	0.249	0.249	0	0	0	0	0	0	0.249	0.183
Methane	0.037	0.031	0.033	0.033	0.033	0.033	0.006	0.006	0.003	0.003	0	0	0	0	0	0	0.003	0.033
Argon	0.026	0.022	0.023	0.023	0.023	0.023	0.006	0.006	0.003	0.003	0	0	0	0	0	0	0.003	0.023
Ammonia	0.262	0.214	0.136	0.136	0.136	0.136	0.969	0.969	0	0	0	0	0	0	0	0	0	0.136
Water	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	0	0

Table 1 Stream ta

Hydrogen and nitrogen are fed to the process at the molar ratio of 3:1 along with a small concentration of inerts (methane and argon). In the synthesis reactor, the following exothermic equilibrium reaction (1) take place:

$$N_2 + 3H_2 \rightleftharpoons 2NH_3 \tag{1}$$

We assume that the reaction kinetics are described by the Temkin-Pyzhev kinetics (Froment and Bischoff, 1990, p. 433) in (2):

$$r_{NH_3} = \frac{2f}{\rho_{cat}} \left(k_1 \frac{p_{N_2} p_{H_2}^{1.5}}{p_{NH_3}} - k_{-1} \frac{p_{NH_3}}{p_{H_2}^{1.5}} \right) \left[\frac{kmol \ NH_3}{kg \ cat \cdot h} \right]$$
(2)

with the partial pressure p_i in [bar] and the catalyst bulk density ρ_{cat} in [kg/m³]. The pre-exponential factors of the forward and reverse paths are, respectively:

$$k_1 = 1.79 \cdot 10^4 e^{-\frac{87,090}{RT}}, \quad k_{-1} = 2.75 \cdot 10^{16} e^{-\frac{198,464}{RT}}$$
 (3)

where T is the temperature in [K]. The multiplier factor f is used to correct for the catalyst activity, and we use the value of f = 4.75 as given in Morud and Skogestad (1998).

The simplified reactor model is shown in Figure 1. It consists of three adiabatic catalytic reactors (beds) in series with interstage cooling and preheating of the feed with the reactor effluent. The interstage cooling is provided by direct mixing of cold reactor feed with the respective inlet flow to each bed. The beds are modeled in Aspen $Plus^{TM}$ by means of its built-in catalytic plug-flow reactor model (see the Appendix for more details in the reactor model). This is clearly a simplified model as, e.g. no radial distribution is assumed. However, it is believed to be acceptable for our purposes.

The reactor effluent is quenched in a series of three heat exchangers where the first one (H-501) uses the hot gases from the reactor to generate low pressure steam. The second heat exchanger (H-502) pre-heats the reactor feed, while the third one (H-583) provides cooling for the condensation of ammonia in the separator (V-502).

The ammonia product, which is about 97%w/w ammonia, leaves the process as a liquid stream through the separator bottom. A small flow is purged from the separator to prevent accumulation of inerts (methane and argon) in the system.

Our reactor model did not produce the oscillations found, for example, by Morud and Skogestad (1998). It would have be proper to include a more detailed reactor model, which is open-loop unstable, but this would not change the main results in this paper on selection of controlled variables, because they are based on the steady-state economics.

Next, we apply the control structure design procedure of Skogestad (2004a) to the ammonia synthesis process just described, starting with the degree of freedom analysis.

3 Top-down analysis

3.1 Degree of freedom (DOF) analysis

The ammonia synthesis in Figure 1 has 10 manipulated variables (Table 2) and 11 candidate measurements (Table 4).

Table 2

List of manipulable variables.

	1	
	Manipulated variable	Status in this work
U1	Gas feed rate F_{gas} [kg/h]	
U2	Purge flow rate F_{purge} [kg/h]	
U3	Feed compressor power W_{K-401} [kW]	
U4	Recycle compressor power W_{K-402} [kW]	
U5	Interstage cooling flow rate to first bed F_{bed1} [kg/h]	Not used
U6	Interstage cooling flow rate to second bed F_{bed2} [kg/h]	Not used
U7	Interstage cooling flow rate to third bed F_{bed3} [kg/h]	Not used
U8	Condensate flow rate to H-501 F_{cond} [kg/h]	Not used (at maximum)
U9	Cooling water flow rate to H-583 F_{cool} [kg/h]	Not used (at maximum)
U10	Product flow rate F_{prod} [kg/h]	Dynamic (level control)

Based on the steady-state degree of freedom analysis described in (Skogestad, 2002), we consider nine steady-state degrees of freedom for optimization as given in Table 3. This is in accordance with Table 2, because U10 only has a dynamic effect.

Note that we later, in the selection of controlled variables, do not consider the interstage cooling flow rates to the beds as steady-state degrees of freedom and thus manipulated variables U5 to U7 are not used. More precisely, we adjust U5 to keep the reactor inlet temperature at its nominal optimum, and we fix the split fractions U5 and U6 at their nominal optimum values (found from the optimization). This is

·	5	1	
Process unit	No. of units	DOF/unit	DOF
External feed streams	1	1	1
Splitters (Purge) ^(*)	1	1	1
Splitters (cold shots reactor)	3	1	3
Compressors (K-401 and K-402)	2	1	2
Adiabatic flashes ^(*) (V-502)	1	0	0
Gas phase reactors ^(*)	3	0	0
Heat exchangers ^(**) (H-501 and H-583)	2	1	2
Total			9

 Table 3

 Steady-state degrees of freedom analysis for the ammonia synthesis plant.

^(*) Assuming no adjustable valves for pressure control (assume fully open valve before separator).

^(**) We will see later that its is optimal to keep maximum cooling.

in accordance with the industrial practice. Moreover, we can anticipate that maximum cooling is optimal in heat exchangers H-501 and H-583 (active constraints) since a small temperature in the separator (V-502) favors more ammonia recovery and less power consumption in the recycle compressor (K-402). Thus we have 4 remaining steady-state degrees of freedom (U1-U4) for which we need to find an associated controlled variable. Note that for case I with a given feedrate (U1 given), we only need to find 3 controlled variables.

Table 4 lists the 11 candidate controlled variables considered in this study. With 4 steady-state degrees of freedom and 11 candidate measurements, there are $\binom{11}{4} = \frac{11!}{4!7!} = 660$ possible ways of selecting the control structure. This shows that we need a simple tool to pre-screen and identify good candidate structures. An effective tool, used in this paper, for the case with unconstrained degrees of freedom is to consider the minimum singular value of the steady-state gain matrix. A large value means that controlling the associated controlled variables has good "self-optimizing" properties.

3.2 Definition of optimal operation

The operational objective to be maximized is given by the profit P below:

$$P = \$_{prod}(x_{NH_3}F_{prod}) + \$_{purge}F_{purge} + \$_{steam}F_{steam} - \\ \$_{gas}F_{gas} - \$_{ws}(W_{K-401} + W_{K-402})$$
(4)

Table 4 Selected candidate controlled variables.

Y1	Gas feed rate F_{gas} [kg/h]
Y2	Reactor inlet pressure P_{rin} [bar]
Y3	Feed compressor power W_{K-401} [kW]
Y4	Recycle compressor power W_{K-402} [kW]
Y5	Product purity x_{NH_3}
Y6	Purge flow rate F_{purge} [kg/h]
Y7	Mole fraction of hydrogen $y_{H_2,purge}$ in the purge stream
Y8	Mole fraction of nitrogen $y_{N_2,purge}$ in the purge stream
Y9	Mole fraction of ammonia $y_{NH_3,purge}$ in the purge stream
Y10	Mole fraction of argon $y_{Ar,purge}$ in the purge stream
Y11	Mole fraction of methane $y_{CH_{A}, purge}$ in the purge stream

where x_{NH_3} is the product purity and F_{steam} is the steam generation in [kg/h]. Note that P is the operational profit and does not include other fixed costs or capital costs.

The prices are $p_{prod} = 0.200 / kg$, $p_{purge} = 0.010 / kg$, $s_{steam} = 0.017 / kg$, $g_{as} = 0.080$ /kg, and $g_{ws} = 0.040$ /kJ.

The constraints on operation are:

 $P_{rin} \leq 250 \ bar$ (5)

 $W_{K-401} \le 25000 \ kW$ (6)

$$W_{K-402} \le 3500 \ kW \tag{7}$$

 $F_{cond} \leq 80000 \ kg/h$ (8)

$$F_{cool} \le 700000 \ kg/h \tag{9}$$

Nominally, we have $F_{gas} = 71000 \text{ kg/h}$, $P_{rin} = 203 \text{ bar}$, $W_{K-401} = 19800 \text{ kW}$, $W_{K-402} = 2718$ kW, and the molar feed compositions $y_{H_2} = 0.7450, y_{N_2} =$ $0.2486, y_{CH_4} = 0.0033$, and $y_{AR} = 0.0030$, as given in Table 1.

We now proceed the self-optimizing control analysis for the cases with given feed rate and variable feed rate, separately.

3.3 Operation with given feed rate

3.3.1 Identification of important disturbances

For the case with given gas feed rate F_{gas} , we consider the disturbances listed in Table 5.

Table 5			
Disturbances to	the process	operation	for Mode I

No.	Description	Nominal	Disturbance
D1	Gas feed rate [kg/h]	71000	+15%
D2	Gas feed rate [kg/h]	71000	-15%
D3	Split fraction to the first bed	0.230	+0.1*
D4	Split fraction to the second bed	0.139	+0.1*
D5	Split fraction to the third bed	0.127	+0.1*
D6	Mole fraction of CH_4 in the gas feed	0.0033	+0.0030**
D7	Mole fraction of Ar in the gas feed	0.0030	+0.0030**

 $^{(*)}$ The split fraction to the feed effluent heat exchanger is reduced by the same amount. $^{(**)}$ Mole fraction of H₂ in the gas feed is reduced by the same amount.

3.3.2 Optimization

With a given gas feed rate F_{gas} , there are 8 steady-state degrees of freedom for optimization, namely F_{purge} , W_{K-401} , W_{K-402} , F_{cond} , and F_{cool} , plus the three split fractions in the reactor. Figure 2 gives the results of the optimizations conducted in Aspen PlusTM for the nominal operating point and for the 7 disturbances described in Table 5. As it can be seen, the profit P is weakly dependent on the disturbances, except for disturbances D1 and D2 that have a large effect on P. However, note that the fact that a disturbance has a small effect on the profit does *not* means it can be discarded when selecting the controlled variables.

As mentioned, during operating we fix the inlet reactor temperature plus the two splits for the reactor cooling at their nominal values. Furthermore, we found that the two colling duties (F_{cond} and F_{cool}) are optimal at their upper constraints, so these should be implemented as active constraints (2 variables). This leaves 5 - 2 = 3 unconstrained degrees of freedom (W_{K-401} , W_{K-402} , and F_{purge}) for which we need to identify associated controlled variables.



Fig. 2. Effect of disturbances (see Table 5) on optimal operation for Mode I. Percentages in parentheses are the changes with respect to the nominally optimum.

3.3.3 Identification of candidate controlled variables - local analysis

Because of the large number of candidate structures, we first pre-screen using a local (linear) analysis as described in Skogestad and Postlethwaite (2005). The objective is to find the set of 3 unconstrained controlled variables that maximizes the minimum singular value $\underline{\sigma}(S_1GJ_{uu}^{-1/2})$. *G* is the steady-state gain matrix of the process from the three unconstrained degrees of freedom *u* to the candidate controlled variables in Table 4 (variables Y2 to Y11); J_{uu} is the Hessian (second-order derivative) of the profit function (4) with respect to the three steady-state degrees of freedom *u*. The motivation behind this expression is that it gives a measure of the loss when a set of candidate controlled variables is fixed at the nominal setpoint in a neighborhood around the nominal optimum. S_1 is the wariation of each candidate measurements $S_1 = diag\{\frac{1}{span(Y_i)}\}$. $span(Y_i)$ is the variation of each candidate controlled variable Y_i due to variation in disturbances and implementation error n_i :

$$span(Y_i) = \Delta Y_{i,opt} + n_i = \sum_j \left| \frac{\partial Y_i}{\partial d_j} \right| \Delta d_j + n_i$$
 (10)

In Table 6, we give the optimal variation and implementation error for the candidate controlled variables in Table 4. A branch-and-bound algorithm (Cao *et al.*, 1998) is used to obtain the candidate sets of controlled variables. The results for the ten sets with largest $\underline{\sigma}(S_1GJ_{uu}^{-1/2})$ are shown in Table 7. One candidate set that one may expect is good is to control reactor inlet pressure P_{rin} , feed compressor power W_{K-401} , and mole fraction of methane in the purge $y_{CH_4,purge}$. However, for this set $\underline{\sigma}(S_1G_{3\times 3}J_{uu}^{-1/2}) = 0.0075$ which is about 10 times smaller than set S_9^I , and we expect the loss be about $10^2 = 100$ times larger.

Table 6
Optimal variation for the candidate controlled variables for Mode I.

	Description	Nominal	$\Delta Y_{i,opt}(d)$	n_i	$span(Y_i)$
Y2	Reactor inlet pressure P_{rin} [bar]	203	35	5	40
Y3	Feed compressor power W_{K-401} [kW]	19800	5200	1000	6200
Y4	Recycle compressor power W_{K-402} [kW]	2718	782	100	882
Y5	Product purity x_{NH_3}	0.969	0.015	0.01	0.025
Y6	Purge flow rate F_{purge} [kg/h]	43.29	673	5	678
Y7	Mole fraction of hy- drogen $y_{H_2,purge}$ in the purge stream	0.624	0.069	0.05	0.119
Y8	Mole fraction of ni- trogen $y_{N_2,purge}$ in the purge stream	0.183	0.044	0.03	0.074
¥9	Mole fraction of ammo- nia $y_{NH_3,purge}$ in the purge stream	0.136	0.016	0.03	0.046
Y10	Mole fraction of argon $y_{Ar,purge}$ in the purge stream	0.023	0.023	0.002	0.025
Y11	Mole fraction of methane $y_{CH_4,purge}$ in the purge stream	0.033	0.028	0.003	0.031

As we can see from Table 7, it is desirable to keep the purge flow rate (candidate controlled variable Y6) fixed at its nominally optimal set point. The other 2 controlled variables may be "freely" chosen among any of the 10 sets in Table 7 because $\underline{\sigma}(S_1G_{3\times3}J_{uu}^{-1/2})$ is essentially the same. As an attractive option, we choose to keep the variables in Set S^I₉ (feed compressor power W_{K-401} , recycle compressor power W_{K-402} , and purge flow rate F_{purge}) at their nominally optimal set point since this reduces significantly the complexity of the control structure.

3.3.4 Evaluation of loss

We now evaluate in more detail the loss caused by keeping each controlled variable in Set S_9^I , corresponding to Mode I of operation, at its nominally optimal set point. The results are shown in Table 8.

Table 7

Set	1	Variabl	es	$\underline{\sigma}(S_1 G_{3\times 3} J_{uu}^{-1/2})$
\mathbf{S}_1^I	Y6	Y8	Y2	0.07652
\mathbf{S}_2^I	Y6	Y11	Y4	0.07534
\mathbf{S}_3^I	Y6	Y3	Y10	0.07512
\mathbf{S}_4^I	Y6	Y3	Y2	0.07502
\mathbf{S}_5^I	Y6	Y3	Y7	0.07501
\mathbf{S}_6^I	Y6	Y3	Y9	0.07491
\mathbf{S}_7^I	Y6	Y8	Y3	0.07490
\mathbf{S}_8^I	Y6	Y3	Y5	0.07489
\mathbf{S}_9^I	Y6	Y3	Y4	0.07485
\mathbf{S}_{10}^{I}	Y6	Y2	Y9	0.07478

Local analysis (Mode I): Minimum singular values for the ten best sets of unconstrained controlled variables.

Table 8

Loss by keeping the variables in Set S_9^I in Table 7 at their nominally optimal set points for Mode I.

Disturbance	Optimal profit	Profit with S_9^I	Loss
	[k\$/year]	[k\$/year]	[k\$/year]
D1	71616	71228	388
D2	54631	53734	897
D3	63437	63203	234
D4	63450	63198	252
D5	63458	63191	267
D6	61886	61400	485
D7	61723	61603	120
Average			378

As the average loss is considered acceptable, we confirm that Set S_9^I an acceptable set of primary controlled variables for the case with given gas feed rate (Mode I).

3.4 Operation with variable feed rate

3.4.1 Maximum throughput

From an economic point of view, it is optimal to increase the production rate F_{prod} . With the given feed rate as a parameter, we optimize the profit P in (4) with the same constraints (5) - (9). The results are given in Figure 3. As per Mode I, the steady-state optimization was performed with all 9 steady-state degrees of freedom, including here the inlet temperature to the reactor (F_{bed1}) and the split fractions to the three interstage cooling flows $(F_{bed2} \text{ and } F_{bed3})$, but we then fix F_{bed1} to F_{bed3} at their nominally optimal values.



Fig. 3. Optimization of the ammonia plant with variable gas feed rate F_{gas} .

When $F_{gas} = 71850$ kg/h, the constraint (7) on the recycle compressor power (W_{K-402}) becomes active and remains active as the feed is increased. When $F_{gas} = 80400$ kg/h, constraint (6) on the feed compressor power (W_{K-401}) becomes active and also remains active. Around $F_{gas} = 87250$ kg/h, the profit reaches its maximum and then it starts falling sharply. The reason for the drop is the reduction in pressure which reduces the conversion and results in a sharp increase in the purge flow rate (see Figure 4). Note that the degrees of freedom corresponding to condensate flow rate to H-501 F_{cond} and cooling water flow rate to H-583 F_{cool} were found to be active throughout the optimizations.

Note that there is no bottleneck and thus no maximum throughput (Mode IIa) for this case study. The reason is that the feed may be purged and there is no limit on the purge rate.

On the other hand, there is an "optimized" throughput (Mode IIb) corresponding to an "economic" bottleneck where $\frac{\partial P}{\partial F_{gas}} = 0$ and further increase in F_{gas} leads to non-optimal economic operation.



Fig. 4. Optimal reactor inlet pressure P_{rin} and purge flow rate F_{purge} as a function of gas feed rate F_{gas} .

3.4.2 **Optimization** (Mode IIb)

We now evaluate the optimal operation with the gas feed rate as a degree of freedom and the two compressors at their constraints, i.e. $W_{K-401} = 25000$ kW and $W_{K-401} = 3500$ kW, respectively. There are two remaining unconstrained degrees of freedom for which we need to identify controlled variables, namely the gas feed rate F_{gas} and the purge flow rate F_{purge} . We thus perform optimization runs for the disturbances listed in Table 9 below. The results are shown in Figure 5.

Table 9

stui	Dances	s to the process operation for Mode no.		
	No.	Description	Nominal	Disturbance
	D3	Split fraction to the first bed	0.230	+0.1*
	D4	Split fraction to the second bed	0.139	+0.1*
	D5	Split fraction to the third bed	0.127	+0.1*
	D6	Mole fraction of CH ₄ in the gas feed	0.0033	+0.003**
	D7	Mole fraction of Ar in the gas feed	0.0030	+0.003**
	D8	Feed compressor power W_{K-401} [kW]	25000	+1000
	D9	Recycle compressor power W_{K-402} [kW]	3500	+100

^(*) The split fraction to the feed effluent heat exchanger is reduced by the same amount.

(**) Mole fraction of H₂ in the gas feed is reduced by the same amount.



Fig. 5. Effect of disturbances (see Table 9) on optimal operation for Mode IIb. Percentages in parentheses are the changes with respect to the nominally optimum.

3.4.3 Identification of candidate controlled variables - local analysis

We use a linear analysis, similar to the one conducted in the Section 3.3.3, to prescreen the candidate controlled variables in Table 4.

The optimal variation and implementation error are given in Table 10 and the ten best sets with largest $\underline{\sigma}(S_1GJ_{uu}^{-1/2})$ are shown in Table 11.

From Table 11, we see that the five best sets involve control of reactor pressure (Y2), which is easy to control. The other controlled variable (Y7 - Y11) is a composition. The lowest minimum singular value is for methane (Y11) and we consider this in more detail in the following.

Note that the purge flow rate (Y6) is not included in any of the ten best sets, whereas it was included in all the ten best sets in mode I (with given feed).

3.4.4 Evaluation of loss (Mode IIb)

The loss is calculated is calculated for set S_1^{IIb} and given in Table 12 for various disturbances.

As the average loss for Mode IIb is acceptable, we confirm Set S_1^{IIb} in Table 11 as the selected set of primary controlled variables.

-		Description	Nominal	$\Delta Y_{i,opt}(d)$	n_i	$span(Y_i)$
-	Y1	Gas feed rate F_{gas} [kg/h]	87250	1570	1700	3315
	Y2	Reactor inlet pressure P_{rin} [bar]	226	68	5	73
	Y5	Product purity x_{NH_3}	0.968	0.019	0.01	0.029
	Y6	Purge flow rate F_{purge} [kg/h]	366	22348	36.6	22384.5
	Y7	Mole fraction of hy- drogen $y_{H_2,purge}$ in the purge stream	0.603	0.068	0.05	0.118
	Y8	Mole fraction of ni- trogen $y_{N_2,purge}$ in the purge stream	0.174	0.040	0.03	0.070
	Y9	Mole fraction of ammo- nia $y_{NH_3,purge}$ in the purge stream	0.172	0.019	0.03	0.049
	Y10	Mole fraction of argon $y_{Ar,purge}$ in the purge stream	0.022	0.027	0.002	0.029
	Y11	Molefractionofmethane $y_{CH_4,purge}$ in the purge stream	0.029	0.025	0.003	0.028

Table 10Total span summary for the candidate controlled variables for Mode IIb.

4 Bottom-up design

4.1 Structure of the regulatory control layer (Modes I and IIb)

The unstable mode associated with the separator level is stabilized using its outlet liquid flow rate with a P-controller. Moreover, as discussed in Morud and Skogestad (1998), the reactor is normally open-loop unstable and sustained oscillations in the reactor outlet temperature may appear as a consequence of a reduction in reactor inlet pressure or temperature. They suggested to control the temperature at the inlet of the first bed using the quench flow rate before the first bed to overcome this instability. Although our model does not seem to have this feature, probably because of no radial variation of dispersion, we here follow this suggestion and close a temperature loop at this location.

To reduce drift caused by pressure changes, and also to avoid nonlinearity in control

Table 11

Set	Varia	ables	$\underline{\sigma}(S_1 G_{2 \times 2} J_{uu}^{-1/2})$	
\mathbf{S}_1^{IIb}	Y2	Y11	0.07011	
\mathbf{S}_2^{IIb}	Y2	Y10	0.06809	
\mathbf{S}_3^{IIb}	Y2	Y8	0.06510	
\mathbf{S}_4^{IIb}	Y2	Y9	0.06391	
\mathbf{S}_5^{IIb}	Y2	Y7	0.05913	
\mathbf{S}_{6}^{IIb}	Y7	Y8	0.05022	
\mathbf{S}_7^{IIb}	Y7	Y10	0.04599	
\mathbf{S}_8^{IIb}	Y7	Y11	0.04172	
\mathbf{S}_{9}^{IIb}	Y9	Y5	0.03987	
\mathbf{S}_{10}^{IIb}	Y10	Y11	0.03429	

Local analysis (Mode IIb): Minimum singular values for the ten best sets of unconstrained controlled variables.

Table 12

Loss by keeping the variables in Set S_1^{IIb} in Table 11 at their nominal optimal set points for Mode II<u>b</u>.

Disturbance	Optimal		With S_1^{IIb}		Loss
	Feed rate	Profit	Feed rate	Profit	
	[kg/h]	[k\$/year]	[kg/h]	[k\$/year]	[k\$/year]
D3	87595	75955	87759	75421	534
D4	87502	75986	87832	75410	576
D5	87663	75887	87715	75334	553
D6	89490	74216	91563	73564	652
D7	89114	74583	90892	73971	612
D8	89529	78675	88263	77990	685
D9	90752	79258	89536	78627	631
Average					606

values, we use flow controllers for the gas feed rate F_{gas} and purge flow rate F_{purge} .

The regulatory control layer is then designed as follows:

- 1. Flow control of gas feed rate F_{gas} .
- 2. Flow control of purge flow rate F_{purge} .
- 3. First-bed inlet temperature T_{bed1} with quench flow rate before the first bed F_{bed1} .

4. Separator level L_{sep} using its liquid outlet flow rate F_{prod} .

4.2 Structure of the supervisory control layer

Mode I: Keep the following at constant (optimal) values: feed compressor power W_{K-401} , recycle compressor power W_{K-402} , and purge flow rate $F_{purge,sp}$. These are all manipulated variables, so no additional control loops are needed.

Mode IIb: Keep the compressors (K-401 and K-402) at maximum power. With the two remaining inputs $u = \{F_{gas,sp}, F_{purge,sp}\}$ we control $y = \{P_{rin}, y_{CH_4,purge}\}$ at constant optimal set points. Suggested pairings are $F_{gas,sp} - P_{rin}$ and $F_{purge,sp} - y_{CH_4,purge}$.

4.3 Switching between Mode I and Mode IIb

The transition between Modes I and IIb involves changing the set points for W_{K-401} , W_{K-402} , and T_{bed1} from the nominally optimal for Mode I to the maximum throughput set point in Mode IIb. In addition, we need to close two loops: $F_{gas,sp}$ - P_{rin} and $F_{purge,sp}$ - $y_{CH_4,purge}$.

4.4 Controller tuning

The regulatory loops selected above are closed and tuned one at the time in a sequential manner (starting with the fastest loops). Aspen DynamicsTM has an open loop test capability that was used to determine a first-order plus delay model from u to y. Based on the model parameters, we used the SIMC tuning rules (Skogestad, 2004*b*) to design the PI-controllers:

$$K_c = \frac{1}{k} \frac{\tau}{\tau_c + \theta}, \quad \tau_I = \min[\tau, 4(\tau_c + \theta)]$$
(11)

where k, τ , and θ are the gain, time constant, and effective time delay, respectively. In our case, we choose $\tau_c = \theta$ to ensure robustness and small input variation.

The gain K_c and integral time τ_I for the regulatory controllers (Modes I and IIb) are given in Table 13, and for supervisory controllers (Mode IIb) in Table 14. There is no need for supervisory control in Mode I (given feed) because the purge flow (F_{purge}) and the two compressor powers $(W_{K-401} \text{ and } W_{K-402})$ are simply set constant.



Fig. 6. Ammonia synthesis process flowsheet with controllers installed (Mode I).



Fig. 7. Ammonia synthesis process flowsheet with controllers installed (Mode IIb).

Tag ^(*)	Input	Output	Set point		PI-controller parameters	
			Mode I	Mode IIb	$K_{c}(\%/\%)$	τ_I (min)
FC1	V_1	F_{gas} [kg/h]	71000	87250 ^(**)	6.75	0.39
FC2	V_2	F_{purge} [kg/h]	43	366 ^(**)	5.05	0.60
TC1	V_4	T_{bed1} [^o C]	306	293	8.05	1.60
LC1	V_3	L_{sep} [m]	2.5	2.5	2.00	-

Table 13Tuning parameters for the regulatory loops (Modes I and IIb).

^(*) See tags in Figure 6.

(**) Nominal value. Set point set by outer loop.

Table 14

Tuning parameters for supervisory loops (Mode IIb).

Tag ^(*)	Input	Output	Set point	PI-controller parameters	
				$K_c (\% / \%)$	τ_I (min)
PC1	$F_{gas,sp}$	P _{rin} [bar]	226	5.55	4.99
CC1	$F_{purge,sp}$	$y_{CH_4,purge}$	0.029	93.39	72.88

(*) See tags in Figure 7.

4.5 Dynamic simulations

In this section, we conduct dynamic simulation to evaluate the performance of the selected control structure. We will consider the disturbances listed in Table 15 for both Modes I and IIb. The responses are shown in Figures 8 to 15. Note that the disturbances are applied 1 hour after the beginning of each simulation run.

Table 15

Disturbances to the effect of dynamic simulations for Modes I and IIb.

No.	Description	Nominal		Disturbance
		Mode I	Mode IIb	
Dyn1	Mole fraction of CH ₄ in the gas feed	0.0033	0.0033	+0.0010 ^(*)
Dyn2	Cooling water temperature in H-583 [°C]	15	15	+5
Dyn3	Compressor power W_{K-401} [kW]	19800	25000	+5%
Dyn4	Gas feed rate F_{gas} [kg/h]	71000	87250 ^(**)	+5%

(*) Mole fraction of H_2 in the gas feed is reduced by the same amount.

(**) Gas feed rate disturbance for Mode IIb considered as measurement error.



Fig. 8. Mode I - Dynamic response of selected variables for disturbance Dyn1.



Fig. 9. Mode IIb - Dynamic response of selected variables for disturbance Dyn1.



Fig. 10. Mode I - Dynamic response of selected variables for disturbance Dyn2.



Fig. 11. Mode IIb - Dynamic response of selected variables for disturbance Dyn2.



Fig. 12. Mode I - Dynamic response of selected variables for disturbance Dyn3.



Fig. 13. Mode IIb - Dynamic response of selected variables for disturbance Dyn3.



Fig. 14. Mode I - Dynamic response of selected variables for disturbance Dyn4.



Fig. 15. Mode IIb - Dynamic response of selected variables for disturbance Dyn4.

It can be seen from Figures 8 and 15 that the product purity does not change significantly in both modes of operation. The reason for this is that ammonia is satisfactorily separated from the other components at all conditions. Moreover, as discussed before, in Mode I the pressure of the system is allowed to fluctuate without causing the process to drift away from its nominally optimal operating condition. In Mode IIb, the pressure is tightly controlled. In general, the dynamic responses for both modes are satisfactory with settling time of about 4 hours, except for disturbance Dyn1 which seems to be the most difficult disturbance. But this was expected since composition is usually slower than other variables, e.g., flow, pressure, and temperature. The reactor inlet/outlet temperature responses are not shown, but they perform very nicely with a maximum change of about 8° C.

Multivariable control would improve the performance of this system, but we find that the dynamic performance with decentralized control is acceptable.

5 Conclusion

This paper discussed the application of the plantwide design procedure of Skogestad (2004*a*) to the ammonia synthesis process. It has been found that is not economically attractive to operate the process beyond the production rate determined by the "economic" bottleneck corresponding to the maximum gas feed rate. By applying the self-optimizing technique of Skogestad (2000), we also found that it is (near) optimal to operate the supervisory control layer by keeping constant set point policy for the feed compressor power, recycle compressor power, and purge flow rate when the gas feed rate is given (Mode I), which corresponds to the practice currently adopted in industrial ammonia synthesis plants. In case of optimized throughput (Mode IIb), the pressure of the system and the mole fraction of CH_4 should be controlled to achieve (near) optimal operation. The regulatory layer is enhanced by controlling the reactor temperature so to avoid the deteriorating effects of oscillations caused by variations in the reactor inlet conditions (temperature and/or pressure) (Morud and Skogestad, 1998).

6 Appendix

We here give more details for the Aspen $Plus^{TM}$ reactor model. The more detailed Aspen $Plus^{TM}$.bkp file is also available at http://www.nt.ntnu.no/users/skoge/.

Table 16 shows the main options and parameters used for modeling the ammonia reactor in Aspen $Plus^{TM}$.

Specification	Bed 1	Bed 2	Bed 3
Reactor type	Adiabatic	Adiabatic	Adiabatic
Length [m]	2.13	3.07	4.84
Diameter [m]	2.00	2.00	2.00
Bed voidage	0.33	0.33	0.33
Particle density [kg/m ³]	2200	2200	2200
Heat transfer between catalyst and process $fluid^{(*)}$	Neglected	Neglected	Neglected
Equipment heat capacity [kJ/kg-K] ^(**)	0.50	0.50	0.50

Table 16 Specifications for the ammonia reactor model in Aspen $Plus^{TM}$.

^(*) Simulations showed the heat transfer between catalyst and process fluid could be neglected.

(**) We assumed the default values given in the model dynamic specification tab.

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