

Multivessel Batch Distillation

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The multivessel batch column consists of a reboiler, several column sections, intermediate vessels and a condenser vessel. This configuration provides a generalization of previously proposed batch-distillation schemes, including the inverted column and the middle-vessel column. The total reflux operation of the multivessel batch-distillation column was presented recently, and the main contribution of this article is to propose a simple feedback control strategy for its operation. We propose to adjust the vessel holdups indirectly by manipulating the reflux flow out of each vessel to control the temperature at some location in the column section below. The feasibility of this strategy is demonstrated by simulations.

Introduction

Although batch distillation generally is less energy efficient than continuous distillation, it has received increased attention in the last few years because of its simplicity of operation, flexibility, and lower capital cost. For many years academic research on batch distillation was focused primarily on optimizing the reflux policy for the conventional batch-distillation column (also called the batch rectifier) where the feed is charged to the reboiler and the products are drawn from the top of the column. More recently, however, there has been renewed interest in reexamining the operation of batch distillation as a whole.

A total reflux strategy, where two final products are collected in the condenser drum and in the reboiler, was suggested independently by Treybal (1970) and Bortolini and Guarise (1971). Sørensen and Skogestad (1994) found the total reflux operation to be better for separations with a small amount of light component. A generalization of the total reflux strategy is the cyclic operation described by Sørensen and Skogestad (1994). Here, the operation is switched between total reflux operation and dumping of the product (i.e., the condenser holdup is introduced as an additional degree of freedom).

Robinson and Gilliland (1950) proposed an inverted batch column, also called the batch stripper, where the feed is charged to the top and the heavy products are drawn from

the bottom of the column. Sørensen and Skogestad (1996) found that, also in this case, the inverted column is better than the conventional column for separations with a small amount of light component. Bernot et al. (1991) studied the use of this column for separating azeotropic mixtures.

A further generalization of the inverted column is the middle-vessel column, which has both a rectifying and a stripping section. This configuration was first mentioned by Robinson and Gilliland (1950, p. 388).

Bortolini and Guarise (1971) proposed to charge a *binary* feed mixture to the middle vessel and draw products from both the top and the bottom, such that the composition in the middle vessel was approximately constant during the operation. The operation stops when the middle vessel is empty. This mode of operation is found to be optimal in some cases (Meski and Morari, 1995).

Davidyan et al. (1991, 1994) and Hasebe et al. (1992) proposed to charge a *ternary* mixture to the middle vessel, and let the light and heavy impurities be drawn from the top and the bottom of the column. In this case the operation stops when the intermediate component in the middle vessel has reached its desired purity. Hasebe et al. (1992) studied the separation of ideal mixtures whereas Davidyan et al. (1991, 1994) studied azeotropic mixtures. Mujtaba and Macchietto (1992, 1994) studied the case where a chemical reaction takes place in the middle vessel, and conversion can be increased by removing the products.

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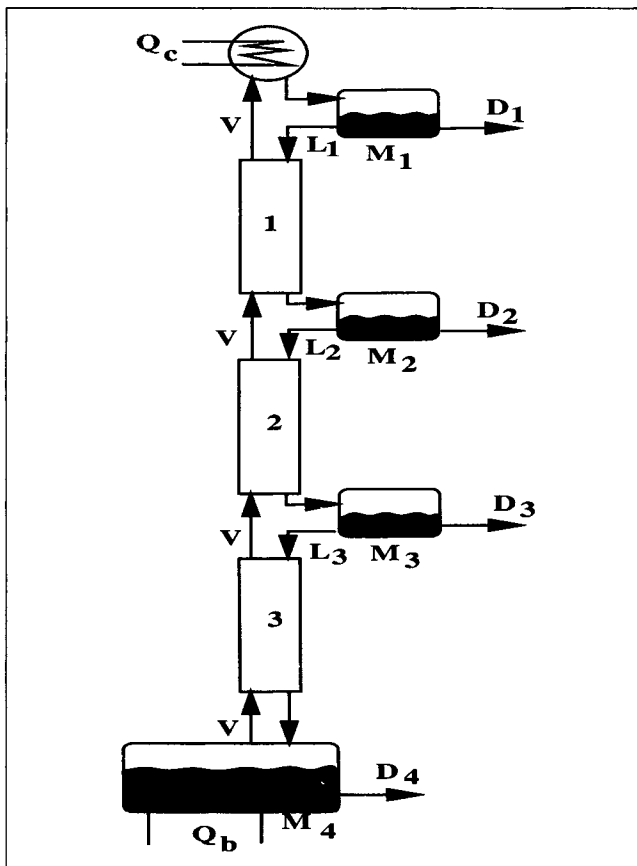


Figure 1. General multivessel batch-distillation column for a case with 4 vessels.

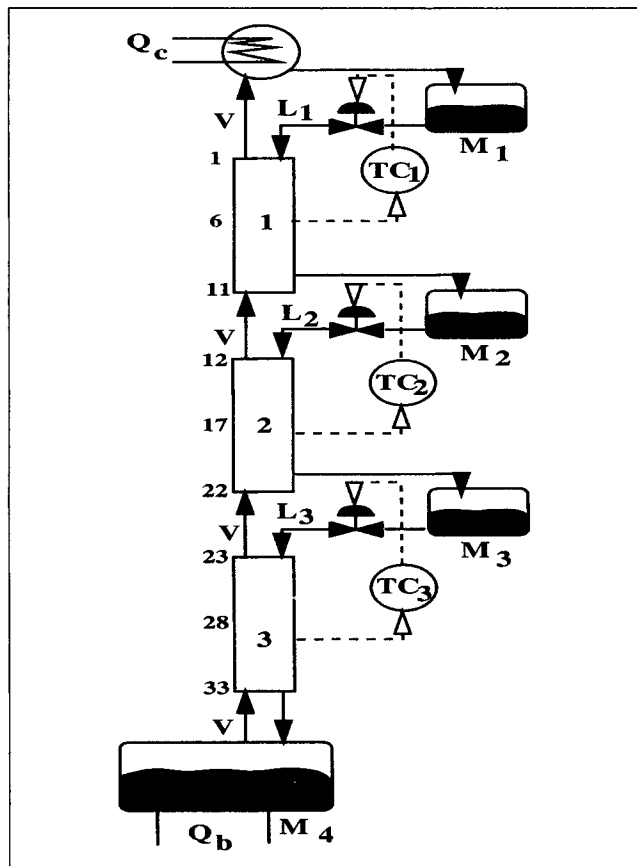


Figure 2. Feedback control structure for multivessel batch-distillation column under total reflux.

A further generalization is the multivessel column suggested by Hasebe et al. (1995). They proposed a total reflux operation where the products are collected in vessels along the column. Because this column can be seen as a stacking of several columns on top of each other, they call this process a "multieffect batch distillation system" (MEBAD).

All of the preceding designs and strategies can be realized in the *multivessel batch-distillation column* shown in Figure 1, where both the holdups, $M_i(t)$, and product flows, $D_i(t)$, are degrees of freedom. With N_c vessels along the column and with the given pressure and heat input, this column has $2N_c - 1$ degrees of freedom for optimization; namely the $N_c - 1$ holdups $M_i(t)$ (e.g., controlled by the $N_c - 1$ reflux streams) and the N_c product rates $D_i(t)$.

Further generalizations are possible, for example, by adding feed streams (semibatch operation), by removing liquid or vapor streams from other places in the column, or by using intermediate heaters or coolers.

The simplest strategy for operating the multivessel column, which is the focus of this article, is the *total reflux operation* suggested by Hasebe et al. (1995) where the N_c product rates are set to zero ($D_i = 0$). This multivessel column has at least two advantages compared to conventional batch distillation where the products are drawn over the top, one at a time. First, the operation is simpler since no product changeovers are required during operation; and second, the energy requirement may be much less due to the multieffect nature of

the operation. In fact, Hasebe et al. (1995) found that for some separations with many components the energy requirement may be similar to that for continuous distillation using $N_c - 1$ columns.

Hasebe et al. (1995) proposed to "control" the total reflux multivessel batch-distillation column by calculating in advance the final holdup in each vessel and then using a level control system to keep the holdup in each vessel constant. For cases where the feed composition is not known exactly they propose, after a certain time, to adjust the holdup in each vessel according to composition measurements. Their scheme, involving the optimization of the vessel holdups and their adjustment based on composition measurement in these vessels, is rather complicated to implement, and requires an advanced control structure to implement the control law.

The main contribution of our article is to propose, for the total reflux operation of the multivessel column, a feedback control structure based on $N_c - 1$ temperature controllers (see Figure 2). The idea is to adjust the reflux flow out of each of the upper $N_c - 1$ vessels by controlling the temperature at some location in the column section below. There is no explicit level control; rather the holdup, M_i , in each vessel is adjusted indirectly by varying the reflux flow to meet the temperature specifications.

In addition to the dynamic simulations, which show the feasibility of the proposed scheme, we present the steady-state values that would be achieved if we were to let the batch

Table 1. Column Data and Initial Conditions

No. of components	$N_c = 4$
Relative volatility	$\alpha_j = [10.2, 4.5, 2.3, 1]$
Total no. of stages	$N_{tot} = 33$
No. of sections	3
No. of stages per section	$N_i = 11$
Vessel holdups	$M_{i,0} = 2.5$ kmol
Tray holdups (constant)	$M_k = 0.01$ kmol
Total initial charge	$M_{tot} = 10.33$ kmol
Reflux flows	$L_{i,0} = 10$ kmol/h
Vapor flow (constant)	$V = 10$ kmol/h

time approach infinity ($t \rightarrow \infty$). Of course, in practice we want the batch time to be as short as possible, and we would terminate the batch when the specifications are met or the improvement in purity is small. Nevertheless, the steady-state values are interesting because they give the achievable separation for a given case.

Simulation Model

All the results in this article are based on simulations using the dynamic model described in the Appendix. We have made a number of simplifying assumptions, such as constant molar flows, constant relative volatility, linear boiling point curve, constant stage holdup, and constant pressure. These assumptions are introduced to simplify the model. Similar results are obtained when the assumptions are relaxed. The dynamic model is implemented using the SPEEDUP software package. In all simulations we neglect the time to heat up the column and feed mixture to the boiling temperature (i.e., “hot” startup is assumed).

In the simulations we consider a four-component mixture, and use a column with three sections and four vessels (including reboiler and condenser). The data for the mixture and the column are summarized in Table 1. The numerical values of the relative volatility are chosen to be close to those of the system methanol–ethanol–propanol–butanol. As mentioned, we assume the mixture temperature, T_k , on stage k to be the molar average of the boiling temperatures of the pure components (the linear boiling point curve assumption may seem very crude; however, we have performed simulations where temperatures are computed from *Raoult’s* law for ideal mixtures, $p_{tot} = \sum_{j=1}^{N_c} x_j \cdot p_j^{sat}(T)$, and the *Clausius-Clapeyron* equation for the pure component vapor pressures, $p_j^{sat}(T) = \exp(-(\Delta H_{vap,j}/R)((1/T)-(1/T_{b,j})))$, and the results show only minor deviations)

$$T_k = \sum_{j=1}^{N_c} x_j \cdot T_{b,j} \tag{1}$$

where $T_{b,j} = [64.7, 78.3, 97.2, 117.7]^{\circ}\text{C}$.

In the simulations we consider two feed mixtures: one equimolar ($z_{F,1}$), and one with smaller amounts of components 2 and 4 ($z_{F,2}$). In all cases, except in Figure 6, the initial (at $t = 0$) vessel holdup is the same ($M_i = 2.5$ kmol) in all four vessels, and the initial composition in all vessels is equal to that of the feed mixture. In all simulations, the vapor flow is kept constant at $V = 10$ kmol/h.

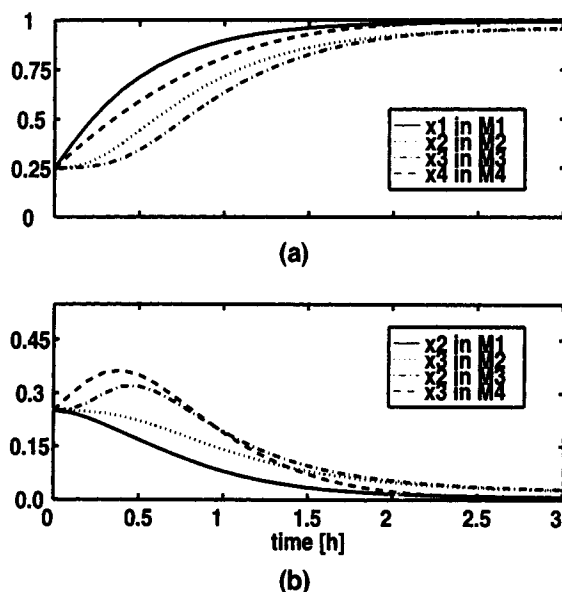


Figure 3. Constant vessel holdup for feed mixture $z_{F,1}$. Composition response in accumulator (1), vessel (2), vessel (3), and reboiler (4). (a) Composition profile, main component; (b) composition profile, main impurity.

Total Reflux Operation with Constant Vessel Holdups

In this section we follow Hasebe et al. (1995) and present simulations that demonstrate the feasibility of the multivessel batch distillation under total reflux. The holdup of each vessel is calculated in advance by taking the amount of feed, feed composition, and product specifications into account. After feeding the prescribed amount of raw material to the vessels, total reflux operation with constant vessel holdup is carried out until the product specifications are achieved, or until the improvement in product purity with time is too slow to justify further operation.

The simulated composition profiles as a function of time are shown in Figure 3 for the equimolar feed mixture

$$z_{F,1} = [0.25, 0.25, 0.25, 0.25]. \tag{2}$$

The holdup in each vessel is kept constant at $M_i = 2.5$ kmol during the simulation. The purity of the main component in each of the vessels is seen to improve nicely and levels off after about 2 hours. As time goes to infinity the steady-state compositions presented in Table 2 are achieved. The steady-state purity of the main component is better than 99% in the top and bottom vessels, and is about 96% in the two intermediate vessels.

Table 2. Constant Vessel Holdups for Feed Mixture $z_{F,1}$: Steady-State Compositions

	Vessel 1	Vessel 2	Vessel 3	Vessel 4
M_i [kmol]	2.5	2.5	2.5	2.5
x_1	0.993	0.017	0.0	0.0
x_2	0.007	0.959	0.025	0.0
x_3	0.0	0.024	0.963	0.004
x_4	0.0	0.0	0.012	0.996

Table 3. Constant Vessel Holdups for Feed Mixture $z_{F,2}$: Steady-State Compositions

	Vessel 1	Vessel 2	Vessel 3	Vessel 4
M_i [kmol]	2.5	2.5	2.5	2.5
x_1	0.999	0.203	0.0	0.0
x_2	0.001	0.404	0.001	0.0
x_3	0.0	0.393	0.999	0.180
x_4	0.0	0.0	0.0	0.820

In practice, however, it may be difficult to keep the vessel holdups constant, and the composition of the feed mixture may be uncertain. The results may be sensitive to holdup errors as is illustrated by considering a case where the actual feed composition is

$$z_{F,2} = [0.30, 0.10, 0.40, 0.20], \quad (3)$$

but the holdup of each vessel is kept constant at $M_i = 2.5$ kmol, which are the vessel holdups corresponding to the equimolar feed composition, $z_{F,1}$. This results in large changes in the final vessel compositions, as seen from Table 3. For example, the purity in vessel 2 is reduced from about 96% to 40%, whereas the purity in vessel 3 is improved from 96% to 99.9%.

To compensate for these feed variations Hasebe et al. (1995) proposed a rather complicated algorithm for adjusting the holdup, based on measuring the composition in the vessels. We propose a much simpler feedback scheme, which is discussed in the next section.

Feedback Control of Multivessel Column

We now present results for our proposed control structure for the total reflux operation (see Figure 2). The separation of a mixture containing N_c components requires N_c vessels and $N_c - 1$ temperature controllers. The i th temperature controller (TC_i) controls the temperature (T_i) in the middle of the i th column section, using as a manipulated input the reflux flow (L_i) out of the vessel above that column section. This enables an indirect control of the holdup (M_i) in that vessel. Note that there is no level controller or level measurement, although some minimum and maximum level sensors may be needed for safety reasons.

The simplest strategy is to set the setpoint for each temperature controller as the average boiling temperature of the two components being separated in that column section. This simple strategy is used in the simulations. Alternatively, to reduce the batch time for a specific separation, the setpoints may be obtained from steady-state calculations corresponding to the desired separation, or they may even be optimized as functions of time. However, it is believed that in most cases, except when the number of stages in the column is close to

Table 4. Data for Temperature Controllers

	$T_{s,i}$ [°C]	K_c [°C/kmol]	Location*
TC_1	71.5	-0.25	6
TC_2	87.75	-0.25	17
TC_3	107.2	-0.25	28

*Stage number from top of column.

Table 5. Temperature Control (Independent of Feed Composition): Steady-State Compositions

	Vessel 1	Vessel 2	Vessel 3	Vessel 4
x_1	0.993	0.016	0.0	0.0
x_2	0.007	0.967	0.034	0.0
x_3	0.0	0.017	0.960	0.007
x_4	0.0	0.0	0.006	0.993

the minimum for the desired separation, the simple strategy will be acceptable.

To demonstrate the feasibility of our proposed control scheme we consider the same column as studied in the previous section (Table 1). To prove that the scheme is insensitive to the initial feed composition, we consider two different initial feed compositions, $z_{F,1}$ (Eq. 2) and $z_{F,2}$ (Eq. 3).

We use simple proportional temperature controllers to manipulate the reflux flow

$$L_i = K_c \cdot (T_i - T_{s,i}) + L_{i,0}, \quad (4)$$

where we selected the controller bias as $L_{i,0} = V = 10$ kmol/h. The numerical values of the controller gain, K_c and temperature setpoints, $T_{s,i}$, are given in Table 4. The controller gains were selected such that an offset in the temperature of $\Delta T_i = 10^\circ\text{C}$ yields a change in the corresponding reflux flow of $\Delta L_i = 2.5$ kmol (25% of the nominal flow rate). The temperature sensors are located in the middle of each column section, and, as already mentioned, the setpoint, $T_{s,i}$, for each section is the average boiling temperature of the components being separated in that section.

With these temperature controllers (see Table 4), we achieve for *both* feed mixtures the same steady-state compositions ($t \rightarrow \infty$) given in Table 5. These steady-state compositions are very close to those found earlier for feed mixture $z_{F,1}$ with constant vessel holdups of $M_i = 2.5$ kmol (compare Tables 2 and 5).

As expected, the steady-state vessel holdups for feed mixture $z_{F,1}$ are close to 2.5 kmol (see the first row in Table 6), whereas those for mixture $z_{F,2}$ are quite different (second row). The composition time responses for feed mixture $z_{F,1}$ are shown in Figures 4a and 4b. The responses are similar to those with the constant vessel holdups shown in Figures 3a and 3b; the difference is that the approach to steady state is faster in vessels 1 and 4 and slower in vessels 2 and 3 for the control structure employing temperature control.

Figure 4 also shows, for feed mixture $z_{F,1}$, the time responses for the holdups in the vessels (Figure 4c), the reflux flows out of the vessels (Figure 4d), and the controlled temperatures (Figure 4e). The simulations demonstrate how the action of the temperature controllers adjust the reflux flows, which indirectly adjust the vessel holdups such that the final products are of high purity.

Table 6. Temperature Control for Feed Mixtures $z_{F,1}$ and $z_{F,2}$: Steady-State Vessel Holdups

	Vessel 1	Vessel 2	Vessel 3	Vessel 4
Feed	M_1 [kmol]	M_2 [kmol]	M_3 [kmol]	M_4 [kmol]
$z_{F,1}$	2.506	2.452	2.512	2.530
$z_{F,2}$	3.053	0.788	4.159	2.000

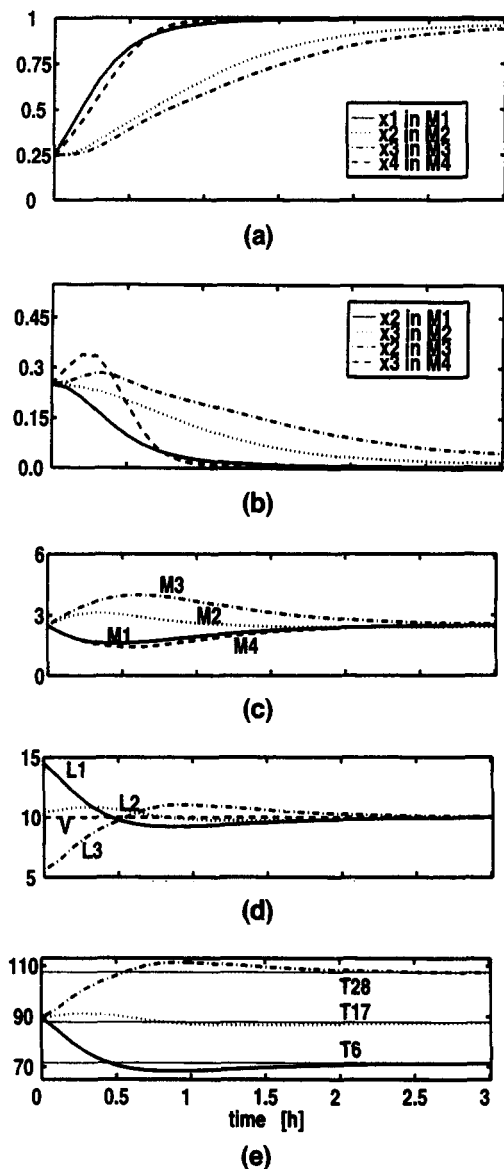


Figure 4. Temperature control for feed mixture $z_{F,1}$.

(a) Composition profile, main component; (b) composition profile, main impurity; (c) holdup, M_i (kmol); (d) reflux flow, L_i (kmol/h); and (e) tray temperature, T_i (°C), as a function of time.

Figure 5 shows similar results for feed mixture $z_{F,2}$. The initial vessel holdups are as for feed mixture $z_{F,1}$, and the simulations demonstrate how the temperature controllers indirectly adjust the vessel holdups such that the steady-state vessel compositions are the same as for feed mixture $z_{F,1}$. From the second row in Table 6 we see that the steady-state holdups with feed mixture $z_{F,2}$ vary from 0.788 kmol in vessel 2 to 4.159 kmol in vessel 3.

Two remarks about the results are in order:

1. From Figures 4e and 5e we observe that the controlled temperatures reach their setpoint with no offset ($T \rightarrow T_s$ as $t \rightarrow \infty$), even though only proportional controllers are used. The reason is that the model from L_i to T_i contains an integrating element, since the system is closed. More specifically,

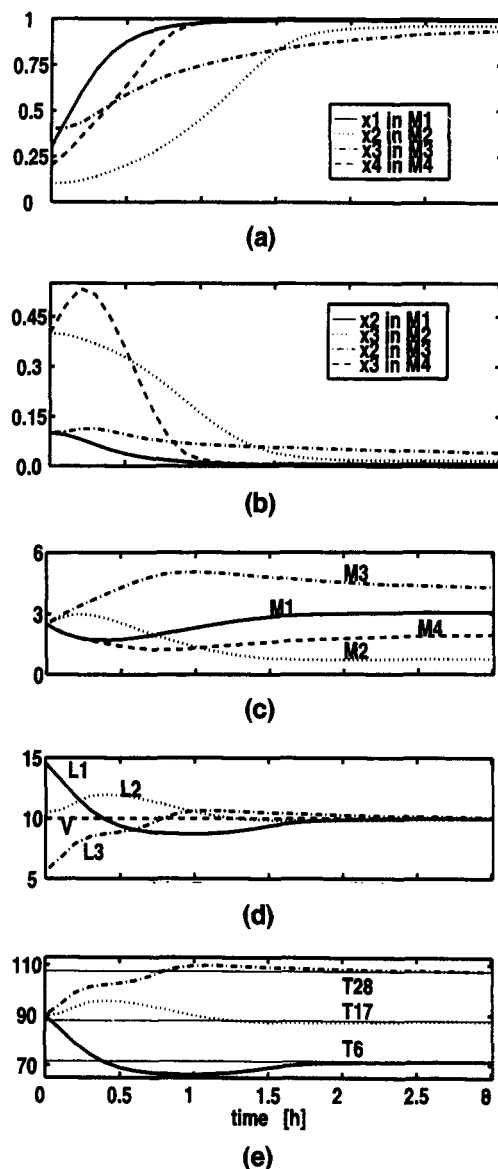


Figure 5. Temperature control for feed mixture $z_{F,2}$.

(a) Composition profile, main component; (b) composition profile, main impurity; (c) holdup, M_i (kmol); (d) reflux flow, L_i (kmol/h); and (e) tray temperature, T_i (°C), as a function of time.

consider the reflux L_i to a column section and the temperature T_i in that section. We know that we can change the steady-state value of T_i by changing L_i . We also know that a steady-state change in L_i is not allowed, since we must have $L_i \rightarrow V_i$ as $t \rightarrow \infty$ (total reflux operation). Thus the transfer function from L_i to T_i must contain an integrator.

2. With temperature control we achieve the same steady-state compositions in the vessels independent of the initial feed composition (only the vessel holdups differ at steady state). The reason is that the column has only three degrees of freedom at steady state, and if we fix three temperatures at three locations in the column, then the temperature profile over the column at total reflux is determined. (This assumes that we do not have multiple steady states. Multiple solutions are not likely when temperatures are specified, but

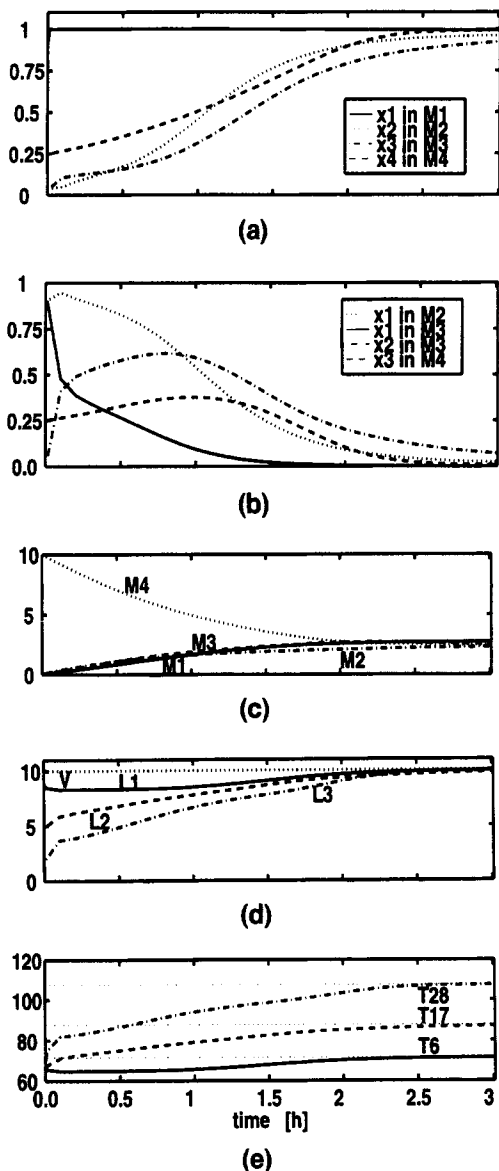


Figure 6. Temperature control for feed mixture $z_{F,1}$ with all liquid initially in the reboiler.

(a) Composition profile, main component; (b) composition profile, main impurity; (c) holdup, M_i (kmol); (d) reflux flow, L_i (kmol/h); and (e) tray temperature, T_i (°C), as a function of time.

may be encountered if we specify the composition of a given component.)

We also performed some simulations to study the startup for the case when the entire feed mixture is charged to the reboiler (and not distributed to the vessels as in Figure 4). The composition responses for feed mixture $z_{F,1}$ are presented in Figures 6a and 6b. The results indicate that the temperature controllers can be activated immediately after startup, possibly with some strategy to ensure that the vessels are not emptied. The vessels are then slowly filled by action of the temperature controllers, which reduce the reflux flows for a transient period (see Figures 6c and 6d). The simulations indicate that, except for the initial 2 to 3 hours, the required time to reach a desired separation is similar to that

in Figure 4 when the feed is initially distributed to the vessels.

Achievable Separation

The achievable separation is limited by the number of theoretical stages in the column sections. Or, stated in another way, if there are no thermodynamic limitations caused by azeotropes, and so forth, then we can achieve any desired purity in a multivessel column if we have a sufficient number of stages. This is demonstrated in Table 7 where we present the steady-state product compositions for different numbers of theoretical stages, N_i , in the three column sections. The total number of stages is $3 \cdot N_i$. We use the same components as before (the feed composition does not matter), and use temperature controllers with the setpoints given in Table 4. With 7 stages in each section we achieve a purity of about 86% in vessels 2 and 3, with 11 stages (base case used in rest of paper) about 96%, with 15 stages about 99%, and with 25 stages about 99.97%.

Discussion

One justification for using multivessel distillation instead of the conventional batch distillation is to save energy, or equivalently, for a given heat input the batch time may be significantly shorter. Another advantage is the simple operation of the multivessel column under total reflux. A third advantage is that it may be easier to operate the column close to optimum with the multivessel column. In conventional batch distillation the optimal operation may depend on the reflux policy and quite strongly on the use of off-cuts to achieve the desired product composition. On the other hand, in the multivessel batch column there are fewer degrees of freedom, which simplifies the operation considerably; the reflux flow is adjusted with simple temperature controllers such that the desired products are accumulated in the vessels.

One disadvantage with the multivessel column compared with conventional batch distillation is that the column itself is more complicated. Also, whereas in a conventional batch column one only has to decide on the length of one single column section, for a multivessel column one has to decide on the number of sections and their length. The design of the multivessel column is therefore more closely linked to a specific feed mixture, in particular the relative volatility and the product specifications. Thus, the design process of a multivessel column is similar to the design of a sequence of continuous distillation columns.

Table 7. Temperature Control (Independent of Feed Composition): Steady-State Vessel Compositions (Main Component) as a Function of Number of Stages N_i in Each Section

N_i	Vessel 1	Vessel 2	Vessel 3	Vessel 4
	x_1	x_2	x_3	x_4
7	0.965	0.864	0.856	0.965
9	0.984	0.932	0.923	0.984
11 (base case)	0.993	0.967	0.960	0.993
15	0.998	0.992	0.990	0.999
19	0.9997	0.9982	0.9974	0.9997
25	0.9999	0.9998	0.9997	0.9999

A simple practical implementation, which is used in our lab-scale column, is to place the sections and stages on top of each other, as shown in Figure 1. The liquid then flows by gravity and there is no need for pumps. However, this design is rather inflexible, and it cannot be used if a large number of stages is required. For an industrial multipurpose separation facility, it is probably better to place the column sections in series with the vessels at ground level as suggested by Hasebe et al. (1995). Reflux pumps are then needed to bring the liquid from the vessels to the column sections. In this case, one can quite easily put several column sections in series to meet the separation requirements for a given feed mixture.

Although the results of the temperature-controlled multi-vessel column presented in this article are most encouraging, a number of aspects are open for further research:

1. The simulations need to be verified experimentally. This work is in progress, and preliminary results (Wittgens et al., 1996) show very good agreement with the simulations.

2. The startup procedure needs to be studied in more detail, including the initial distribution of the feed mixture.

3. In this study the setpoints for the temperature controllers were set such that the temperature in the middle of the section would equal the average of the boiling points of the components separated in that section. In general, this is not optimal, especially if the requirements for product purities are very different.

4. The type of mixtures and conditions for which the new multivessel batch column is most suited should be established.

5. Reasonable criteria for aborting the total reflux operation should be established; that is, when is the improvement in product purity too slow to justify further operation, and how should this be detected?

6. The total reflux operation may be generalized by also allowing withdrawal of products (continuous or discontinuous) from the vessels. In this way the multivessel column forms a "super structure" that has as special case all the previously proposed batch schemes mentioned in the Introduction.

Conclusions

A general multivessel batch-distillation column is proposed, along with a new control strategy for its total reflux operation. It is shown that the proposed control scheme is easy to implement and operate, particularly for widely varying feed compositions.

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Appendix: Mathematical Model of the Multivessel Column

The model used in the simulations is based on the following assumptions:

- Constant relative volatility
- Constant molar liquid holdups on the stages (in which liquid flow dynamics are neglected)
- Constant molar vapor flows V_i (in which energy balance is neglected)
- Constant pressure
- Constant tray efficiency (100%)
- Negligible vapor holdup
- Perfect mixing on all trays and in all vessels
- Total condenser.

The distillation column is modeled as a stack of stages (counted from the top) as shown in Figure A1. Note that the vapor flow V does not pass through the intermediate vessels, so these are not counted as part of the theoretical stages. The model for stage k in section i consists of a material balance for each component j (M_k is assumed constant)

$$M_k \frac{dx_{j,k}}{dt} = L_i(x_{j,k-1} - x_{j,k}) + V(y_{j,k+1} - y_{j,k}) \quad (\text{A1})$$

and the vapor/liquid equilibrium

$$\alpha_j = \frac{y_{j,k}/x_{j,k}}{y_{H,k}/x_{H,k}}, \quad (\text{A2})$$

where H denotes the heaviest component in the mixture.

The material balance for the condenser ($i = 1$) is

$$\frac{d(M_1 x_{j,1})}{dt} = V y_{j+1,1} - L_1 x_{j,1}, \quad (\text{A3})$$

and its mass balance

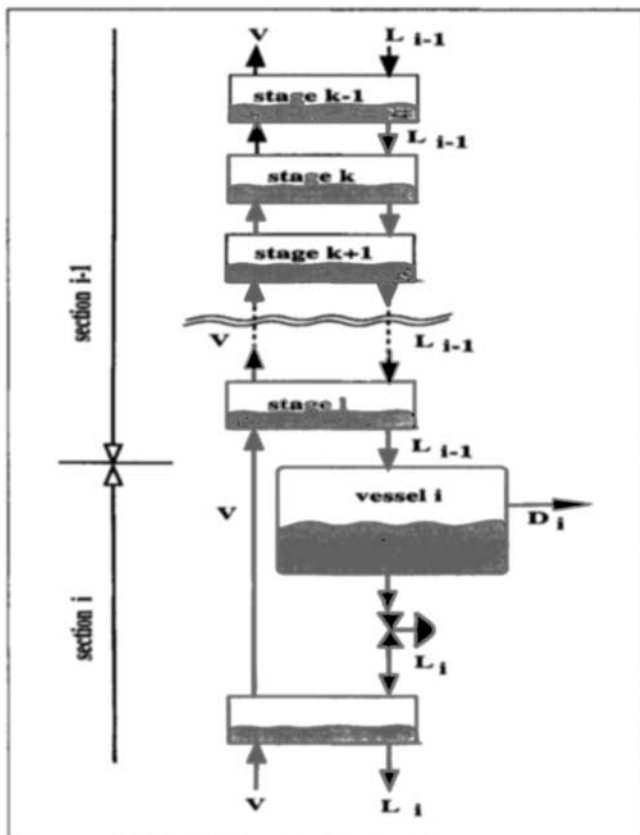


Figure A1. Connection of trays and vessels.

$$\frac{dM_i}{dt} = V - L_i \quad (\text{A4})$$

For intermediate vessels (i)

$$\frac{d(M_i x_{j,i})}{dt} = L_{i-1} x_{j-1,i} - L_i x_{j,i} \quad (\text{A5})$$

with

$$\frac{dM_i}{dt} = L_{i-1} - L_i \quad (\text{A6})$$

where x_i is the composition in vessel i and $x_{j-1,i}$ is the liquid composition at the bottom of the section above. The liquid flow L_i leaving vessel i is set by a control valve.

The reboiler ($i = R$)

$$\frac{d(M_i x_{j,i})}{dt} = L_{i-1} x_{j,i} - Vy_{j,i} \quad (\text{A7})$$

where

$$\frac{dM_i}{dt} = L_{i-1} - V \quad (\text{A8})$$

where again the vapor/liquid equilibrium is described by Eq. A2.

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