

## Adaptive Control of Three – Tank – System Using Polynomial Methods

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**Abstract:** Adaptive control of a three – tank - system laboratory model is presented. The objective laboratory model is a two input – two output (TITO) nonlinear system. It is based on experience with authentic industrial control applications. Two control algorithms utilizing polynomial theory and pole – placement were applied and compared. The first one is based on the traditional 1DOF (one – degree of freedom) configuration of the closed loop, the second one applies a decoupling method to suppress undesired cross – coupling. The algorithms implemented as self – tuning controllers are then used for control of the model. Results of real-time experiments are also included. Quality of control achieved by both methods is compared and discussed.

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### 1. INTRODUCTION

Many technological processes require a simultaneous control of several variables related to one system. Each input may influence all system outputs. The three – tank – system in Fig. 1 is a typical multivariable nonlinear system with significant cross – coupling. The design of a controller able to cope with such a system must be quite sophisticated. There are many different methods of controlling MIMO (multi input – multi output) systems. One possibility is the serial insertion of a compensator ahead of the system to transform the multivariable system into a series of independent SISO loops (Wittenmark *et al.*, 1987, Chien *et al.*, 1990, Peng, 1990, Krishnawamy *et al.*, 1991).

Here polynomial theory approach (Kučera, 1980, Kučera, 1991) is used for the design of multivariable controllers. Two controllers are presented. The first one is based on traditional 1DOF (one degree of freedom) configuration of the closed loop, the second one applies a decoupling method using a compensator to suppress undesired cross – coupling. Application of the designed methods for adaptive control of the three – tank – system is then presented. The algorithms were applied as self – tuning controllers. It was assumed, that the dynamic behaviour of the system could be described in the neighbourhood of a steady state by a discrete linear model. The recursive least squares method with the directional forgetting was used for the identification part of the self – tuning controllers.

The paper is organised as follows: Section 2 contains description of the three – tank - system; Section 3 presents a mathematical model of the system which was used for the controllers design; Sections 4 and 5 describes designs of the 1DOF and decoupling controllers; Section 6 describes the system identification method; Section 7 contains the experimental results; finally, Section 8 concludes the paper.

### 2. THREE – TANK – SYSTEM

The three – tank – system laboratory model can be viewed as a prototype of many industrial applications in process industry, such as chemical and petrochemical plants, oil and gas systems. The typical control issue involved in the system is how to keep the desired liquid level in each tank. The principle scheme of the model is shown in Fig 1. The basic apparatus consists of three plexiglass tanks numbered from left to right as T1, T3 and T2. These are connected serially with each other by cylindrical pipes. Liquid, which is collected in a reservoir, is pumped into the first and the third tanks to maintain their levels. The level in the tank T3 is a response which is uncontrollable. It affects the level in the two end tanks. Each tank is equipped with a static pressure sensor, which gives a voltage output proportional to the level of liquid in the tank.

Hmax denotes the highest possible liquid level. In case the liquid level of T1 and T2 exceeds this value the corresponding pump will be switched off automatically.  $Q_1$  and  $Q_2$  are the flow rates of the pumps 1 and 2. Two variable speed pumps driven by DC motor are used in this apparatus. These pumps are designed to give an accurate well defined flow per rotation. Thus, the flow rate provided by each pump is proportional to the voltage applied to its DC motor.

There are six manual valves  $v_1, v_2 \dots v_6$  that can be used to vary the configuration of the process or to introduce disturbances or faults.

The pump flow rates  $Q_1$  and  $Q_2$  denote the input signals, the liquid levels of T1 and T2 are the output signals.

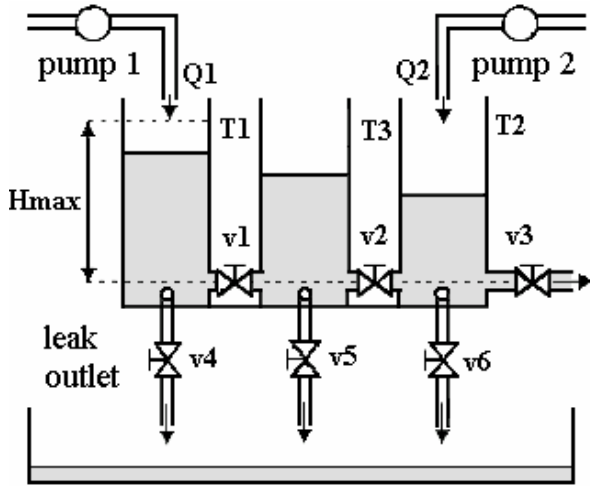


Fig. 1. Principal scheme of three – tank - system

### 3. MATHEMATICAL MODEL OF THE APPARATUS

An analytical model of the three – tank - system based on physics and the equipment construction is presented in (AMIRA, 1996). All the parameters in this model have a particular physical denotation. The apparatus is a nonlinear system, as it was mentioned above. A possible method for control of nonlinear systems is using of self – tuning controllers. A suitable model for adaptive control of the real object is an input – output model (“black box model”). This is a standard approach in self tuning controller area. Instead of often tedious construction of a model from first principles and then calculating its parameters from plant dimensions and physical constants, general type of model is chosen (here it is in fact transfer function (1)) and its parameters are identified from data. It is a model of the system behaviour and its parameters do not have a particular physical denotation. Of course, not all properties of the plant can be extracted from the data in this way but as a rule dominant properties are modelled, which is sufficient for a controller design. Advantages of this kind of model are its simplicity and accuracy in an operational range in which the input – output dependence is measured. In the framework of adaptive controllers it was chosen this kind of model. It was necessary to determine its structure in advance. The aim here was to find experimentally as simple structure of the model as possible, as it is mentioned below. The parameters are identified during the process of the recursive identification in virtue of the measured input and output signals.

A general transfer matrix of a two inputs – two outputs system with cross coupling is expressed as

$$G(z) = \begin{bmatrix} G_{11}(z) & G_{12}(z) \\ G_{21}(z) & G_{22}(z) \end{bmatrix} \quad (1)$$

$$Y(z) = G(z)U(z) \quad (2)$$

Where  $U(z)$  and  $Y(z)$  are vectors of the manipulated variables (flow rates of liquid into tanks T1 and T2) and the controlled variables (liquid levels of T1 and T2).

$$U(z) = [u_1(z), u_2(z)]^T \quad Y(z) = [y_1(z), y_2(z)]^T \quad (3)$$

It is possible to assume that the dynamic behaviour of the system can be described in the neighbourhood of a steady state by a discrete linear model in the following form of the matrix fraction

$$G(z) = A^{-1}(z^{-1})B(z^{-1}) = B_1(z^{-1})A_1^{-1}(z^{-1}) \quad (4)$$

Where polynomial matrices  $A \in R_{22}[z^{-1}]$ ,  $B \in R_{22}[z^{-1}]$  are the left coprime factorization of matrix  $G(z)$  and matrices  $A_1 \in R_{22}[z^{-1}]$ ,  $B_1 \in R_{22}[z^{-1}]$  are the right coprime factorization of  $G(z)$ .

At first, the algorithms described below were designed for a model with polynomials of the first order. This model proved to be unsuitable for the process and the control algorithms failed. Consequently, the polynomial orders were increased and the algorithms were designed for a model with second order polynomials. This model proved to be effective. In case of the simple 1DOF controller a model with nondiagonal matrix  $A(z^{-1})$  was used.

The model has sixteen parameters:

$$A(z^{-1}) = \begin{bmatrix} 1 + a_1z^{-1} + a_2z^{-2} & a_3z^{-1} + a_4z^{-2} \\ a_5z^{-1} + a_6z^{-2} & 1 + a_7z^{-1} + a_8z^{-2} \end{bmatrix} \quad (5)$$

$$B(z^{-1}) = \begin{bmatrix} b_1z^{-1} + b_2z^{-2} & b_3z^{-1} + b_4z^{-2} \\ b_5z^{-1} + b_6z^{-2} & b_7z^{-1} + b_8z^{-2} \end{bmatrix} \quad (6)$$

In case of decoupling control using the compensator the model was simplified by considering the matrix  $A(z^{-1})$  to be a diagonal type.

$$A(z^{-1}) = \begin{bmatrix} 1 + a_1z^{-1} + a_2z^{-2} & 0 \\ 0 & 1 + a_3z^{-1} + a_4z^{-2} \end{bmatrix} \quad (7)$$

The reason for the simplification is explained in section 5. This assumption causes reduction of number of parameters. This model has twelve parameters.

### 4. DESIGN OF 1DOF CONTROLLER

The 1DOF configuration of the closed loop system is depicted in Fig. 2.

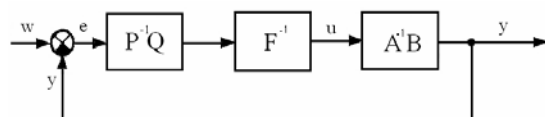


Fig. 2. Block diagram of 1DOF configuration

Similarly as it was for the controlled system, the transfer matrix of the controller takes the form of the following matrix fraction

$$G_R(z) = P^{-1}(z^{-1})Q(z^{-1}) = Q_1(z^{-1})P_1^{-1}(z^{-1}) \quad (8)$$

Generally, the vector  $W(z^{-1})$  of input reference signals is specified as

$$W(z) = F_w^{-1}(z^{-1})h(z^{-1}) \quad (9)$$

In case of control of the three – tank - system, the reference signals were considered as a class of step functions. In this case  $h(z^{-1})$  is a vector of constants and  $F_w(z^{-1})$  is expressed as

$$F_w(z^{-1}) = \begin{bmatrix} 1-z^{-1} & 0 \\ 0 & 1-z^{-1} \end{bmatrix} \quad (10)$$

The compensator  $F(z^{-1})$  is a component formally separated from the controller. It has to be included in the controller to fulfil the requirement on the asymptotic tracking. If the reference signals are step functions, then  $F(z^{-1})$  is an integrator.

The control law (operator  $z^{-1}$  will be omitted from some operations for the purpose of simplification) is defined as

$$U = F^{-1}Q_1P_1^{-1}E \quad (11)$$

where  $E$  is a vector of control errors. Using matrix operations it is possible to modify this vector as

$$E = W - Y = P_1(AFP_1 + BQ_1)^{-1}AW \quad (12)$$

Asymptotic tracking of the reference signals is then fulfilled if  $FP_1$  is divisible by  $F_w$ .

It is possible to derive the following equation for the system output

$$Y = A^{-1}BF^{-1}P^{-1}QE = A^{-1}BF^{-1}P^{-1}Q(W - Y) \quad (13)$$

and this can be modified

$$Y = P_1(AFP_1 + BQ_1)^{-1}BQ_1P_1^{-1}W \quad (14)$$

It is apparent, that the elements of the vector of the output signal have in their denominators the determinant of the matrix  $AFP_1 + BQ_1$ . This determinant is the characteristic polynomial of a MIMO system. The roots of this polynomial matrix are the ruling factors for the behaviour of a closed loop system. The roots must be inside the unit circle (of the Gauss complex plain), in order for the system to be stable. The conditions for BIBO (bounded input bounded output) stability can be defined by the following diophantine equation

$$AF P_1 + BQ_1 = M \quad (15)$$

Where  $M \in R_{22}[z^{-1}]$  is a stable diagonal polynomial matrix. If the system has the same number of inputs and outputs,

matrix  $M$  can be chosen as diagonal. This choice enables easier computation of controller parameters.

$$M(z^{-1}) = \begin{bmatrix} 1 + m_1z^{-1} + m_2z^{-2} + & & 0 \\ + m_3z^{-3} + m_4z^{-4} & & \\ & & 1 + m_1z^{-1} + m_2z^{-2} + \\ 0 & & + m_3z^{-3} + m_4z^{-4} \end{bmatrix} \quad (16)$$

The degree of the controller polynomial matrices depends on the internal properness of the closed loop. The structure of matrices  $P_1$  and  $Q_1$  was chosen so that the number of unknown controller parameters equals the number of algebraic equations resulting from the solution of the diophantine equation. The method of the uncertain coefficients was used to solve the diophantine equation.

$$P_1(z^{-1}) = \begin{bmatrix} 1 + p_1z^{-1} & p_2z^{-1} \\ p_3z^{-1} & 1 + p_4z^{-1} \end{bmatrix} \quad (17)$$

$$Q_1(z^{-1}) = \begin{bmatrix} q_1 + q_2z^{-1} + q_3z^{-2} & q_4 + q_5z^{-1} + q_6z^{-2} \\ q_7 + q_8z^{-1} + q_9z^{-2} & q_{10} + q_{11}z^{-1} + q_{12}z^{-2} \end{bmatrix} \quad (18)$$

The solution of the diophantine equation results in a set of sixteen algebraic equations with unknown controller parameters. Using matrix notation the algebraic equations can be expressed in the following form

$$\begin{bmatrix} -a_2 & -a_4 & 0 & 0 & b_2 & 0 & 0 & b_4 \\ a_2 - a_1 & a_4 - a_3 & 0 & b_2 & b_1 & 0 & b_4 & b_3 \\ a_1 - 1 & a_3 & b_2 & b_1 & 0 & b_4 & b_3 & 0 \\ 1 & 0 & b_1 & 0 & 0 & b_3 & 0 & 0 \\ -a_6 & -a_8 & 0 & 0 & b_6 & 0 & 0 & b_8 \\ a_6 - a_5 & a_8 - a_7 & 0 & b_6 & b_5 & 0 & b_8 & b_7 \\ a_5 & a_7 - 1 & b_6 & b_5 & 0 & b_8 & b_7 & 0 \\ 0 & 1 & b_5 & 0 & 0 & b_7 & 0 & 0 \end{bmatrix} \begin{bmatrix} p_1 \\ p_2 \\ p_3 \\ p_4 \\ p_5 \\ p_6 \\ p_7 \\ p_8 \\ p_9 \\ p_{10} \\ p_{11} \\ p_{12} \end{bmatrix} = \begin{bmatrix} m_4 \\ m_3 + a_2 \\ m_2 - a_2 + a_1 \\ m_1 - a_1 + 1 \\ 0 \\ a_6 \\ a_5 - a_6 \\ -a_5 \end{bmatrix} \quad (19)$$

The controller parameters are obtained by solving these equations.

## 5. DESIGN OF DECOUPLING CONTROLLER

There are several ways to control multivariable systems with internal interactions. One possibility is a serial insertion of a compensator ahead of the system (Wittenmark *et al.*, 1987, Chien *et al.*, 1990, Peng, 1990, Krishnawamy *et al.*, 1991). The objective, in this case, is to suppress undesirable interactions between the input and output variables so that each input affects only one controlled variable. The block diagram for this kind of system is shown in Fig. 3 ( $R$  is a transfer matrix of a controller and  $C$  is a decoupling compensator).

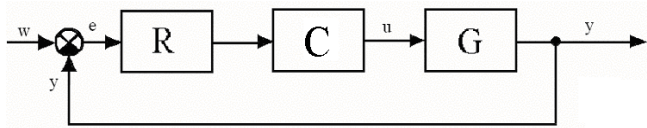


Fig. 3. Closed loop with general decoupling compensator

The resulting transfer matrix  $H$  is then determined by

$$H = GC \quad (20)$$

The decoupling conditions are fulfilled when the matrix  $H$  is diagonal.

The matrix  $B$  can be written as

$$B = z^{-1} \begin{bmatrix} b_1 + b_2 z^{-1} & b_3 + b_4 z^{-1} \\ b_5 + b_6 z^{-1} & b_7 + b_8 z^{-1} \end{bmatrix} = z^{-1} B_x \quad (21)$$

and then the matrix  $H$  as

$$H = A^{-1} z^{-1} B_x C = A^{-1} H_1 \quad (22)$$

As it was mentioned above, the matrix  $A$  was chosen to be diagonal. The objective of this simplification is apparent from the equation (22). If the matrix  $A$  was assumed to be non-diagonal, it would have to be included into the compensator ( $AA^{-1}=I$ ) to obtain a diagonal matrix  $H$ . Then, the order of the controller and sophistication of the closed loop system would be increased. According to this assumption, the compensator  $C$  must be chosen so that multiplication of the matrix  $B_x$  and the compensator leads to a diagonal matrix  $H_1$ . The compensator, which was applied for our algorithm, is the adjoint matrix  $B_x$ .

$$C = adj(B_x) \quad (23)$$

The multiplication of the matrix  $B_x$  and the adjoint matrix  $B_x$  results in a diagonal matrix  $H_1$ . The determinants of the matrix  $B_x$  represent the diagonal elements.

$$H_1 = z^{-1} B_x adj(B_x) = z^{-1} \begin{bmatrix} det(B_x) & 0 \\ 0 & det(B_x) \end{bmatrix} \quad (24)$$

The closed loop system is shown in Fig. 4.

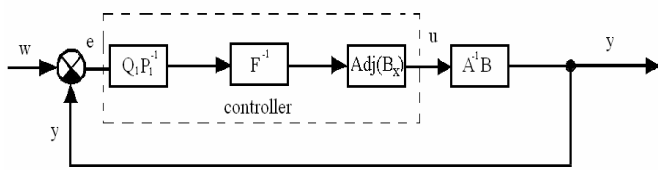


Fig. 4. Closed loop with chosen decoupling compensator

The compensator  $F$  is the integrator which must be included into the controller to fulfil the requirement on the asymptotic tracking as in the previous case with the simple 1DOF controller.

It is possible to derive an equation for the system output, which can be modified by matrix operations to the form

$$Y = P_1 (AFP_1 + H_1 Q_1)^{-1} H_1 Q_1 P_1 W \quad (25)$$

To achieve stability in the closed loop system the following diophantine equation must be fulfilled

$$AFP_1 + H_1 Q_1 = M \quad (26)$$

The controller polynomial matrices were chosen in the following form

$$P_1(z^{-1}) = \begin{bmatrix} 1 + p_1 z^{-1} + p_2 z^{-2} & 0 \\ 0 & 1 + p_3 z^{-1} + p_4 z^{-2} \end{bmatrix} \quad (27)$$

$$Q_1(z^{-1}) = \begin{bmatrix} q_1 + q_2 z^{-1} + q_3 z^{-2} & 0 \\ 0 & q_4 + q_5 z^{-1} + q_6 z^{-2} \end{bmatrix} \quad (28)$$

and the matrix  $M$  is

$$M(z^{-1}) = \begin{bmatrix} 1 + m_1 z^{-1} + & & & & \\ + m_2 z^{-2} + m_3 z^{-3} + & 0 & & & \\ + m_4 z^{-4} + m_5 z^{-5} & & & & \\ & 1 + m_6 z^{-1} + & & & \\ 0 & m_7 z^{-2} + m_8 z^{-3} + & & & \\ & + m_9 z^{-4} + m_{10} z^{-5} & & & \end{bmatrix} \quad (29)$$

The solution of the diophantine equation defines a set of algebraic equations which were used to obtain the unknown controller parameters.

For the purpose of a simplification, the  $det(B_x(z^{-1}))$  is defined as follows:

$$\begin{aligned} det(B_x(z^{-1})) &= db_3 + db_2 z^{-1} + db_1 z^{-2} \\ det(B_x(z^{-1})) &= (b_1 b_7 - b_5 b_3) + z^{-1} (b_1 b_8 + b_2 b_7 - b_5 b_4 - b_6 b_3) + \\ &+ z^{-2} (b_2 b_8 - b_4 b_6) \end{aligned} \quad (30)$$

The algebraic equations have the form

$$\begin{bmatrix} 1 & 0 & db_3 & 0 & 0 \\ a_1 - 1 & 1 & db_2 & db_3 & 0 \\ a_2 - a_1 & a_1 - 1 & db_1 & db_2 & db_3 \\ -a_2 & a_2 - a_1 & 0 & db_1 & db_2 \\ 0 & -a_2 & 0 & 0 & db_1 \end{bmatrix} \begin{bmatrix} p_1 \\ p_2 \\ q_1 \\ q_2 \\ q_3 \end{bmatrix} = \begin{bmatrix} m_1 - a_1 + 1 \\ m_2 - a_2 + a_1 \\ m_3 + a_2 \\ m_4 \\ m_5 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & db_3 & 0 & 0 \\ a_3 - 1 & 1 & db_2 & db_3 & 0 \\ a_4 - a_3 & a_3 - 1 & db_1 & db_2 & db_3 \\ -a_4 & a_4 - a_3 & 0 & db_1 & db_2 \\ 0 & -a_4 & 0 & 0 & db_1 \end{bmatrix} \begin{bmatrix} p_3 \\ p_4 \\ q_4 \\ q_5 \\ q_6 \end{bmatrix} = \begin{bmatrix} m_6 - a_3 + 1 \\ m_7 - a_4 + a_3 \\ m_8 + a_4 \\ m_9 \\ m_{10} \end{bmatrix} \quad (31)$$

The control law is described by the following matrix equation

$$FU = adj(B_x) Q_1 P_1^{-1} E \quad (32)$$

## 6. SYSTEM IDENTIFICATION

For control of the three – tank – system, the control algorithms were applied as self tuning controllers. They were incorporated into an adaptive control system with recursive identification. The recursive least square method proved to be effective for self-tuning controllers (Kulhavý, 1987; Bittanti et al., 1990) and was used as the basis for our algorithm. For our two-variable example it was considered the disintegration of the identification into two independent parts.

For the simple 1DOF controller with nondiagonal matrix  $A$  the parameter vectors are specified as shown below:

$$\theta_1^T(k) = [a_1, a_2, a_3, a_4, b_1, b_2, b_3, b_4] \quad (33)$$

$$\theta_2^T(k) = [a_5, a_6, a_7, a_8, b_5, b_6, b_7, b_8]$$

and the data vector is

$$\phi_{1,2}^T(k-1) = [-y_1(k-1), -y_1(k-2), -y_2(k-1), -y_2(k-2), u_1(k-1), u_1(k-2), u_2(k-1), u_2(k-2)] \quad (34)$$

For the configuration with the compensator the vectors have the following forms:

$$\theta_1^T(k) = [a_1, a_2, b_1, b_2, b_3, b_4] \quad (35)$$

$$\theta_2^T(k) = [a_3, a_4, b_5, b_6, b_7, b_8]$$

$$\phi_1^T(k-1) = [-y_1(k-1), -y_1(k-2), u_1(k-1), u_1(k-2), u_2(k-1), u_2(k-2)] \quad (36)$$

$$\phi_2^T(k-1) = [-y_2(k-1), -y_2(k-2), u_1(k-1), u_1(k-2), u_2(k-1), u_2(k-2)] \quad (37)$$

The parameter estimates are updated using the recursive least square method with adaptive directional forgetting.

## 7. EXPERIMENTAL EXAMPLES

The model was connected with a PC equipped with a control and measurement PC card. The Matlab and the Real Time Toolbox were used to control the system.

For the experiments presented in this paper, the three – tank – system was configured in such a way that the valves v3 and v5 were closed and the remaining valves were open.

The best sampling period  $T_0=5$  s was found in virtue of many experiments. Another problem was finding of suitable poles of the characteristic polynomial. In comparison with controllers for SISO control loops, where it is often possible to assume influence of particular poles to behaviour of the closed loop, pole – placement of multivariable controllers is much more complicated. The right side matrices, obtained from a number of experiments, are denoted as follows: the right side matrix for the case without the compensator -  $M_1$  and the right side matrix for controller with the compensator -  $M_2$

$$M_1(z^{-1}) = \begin{bmatrix} 1 - 0,9z^{-1} + 0,19z^{-2} - & 0 \\ -0,009z^{-3} - 0,002z^{-4} & 1 - 0,9z^{-1} + 0,19z^{-2} - \\ 0 & -0,009z^{-3} - 0,002z^{-4} \end{bmatrix} \quad (38)$$

$$M_2(z^{-1}) = \begin{bmatrix} 1 - 0,7z^{-1} + 0,01z^{-2} - & 0 \\ -0,1z^{-3} - 0,05z^{-4} + 0,0001z^{-5} & 1 - 0,7z^{-1} + 0,01z^{-2} - \\ 0 & -0,1z^{-3} - 0,05z^{-4} + 0,0001z^{-5} \end{bmatrix} \quad (39)$$

In Fig. 4 and Fig. 5 are shown time responses of the control when the initial parameter estimates were chosen without any a-priori information:

$$\theta_1^T(0) = [0.1, 0.2, 0.3, 0.4, 0.1, 0.2, 0.3, 0.4] \quad (40)$$

$$\theta_2^T(0) = [0.5, 0.6, 0.7, 0.8, 0.5, 0.6, 0.7, 0.8]$$

and

$$\theta_1^T(0) = [0.1, 0.2, 0.1, 0.2, 0.3, 0.4] \quad (41)$$

$$\theta_2^T(0) = [0.2, 0.3, 0.5, 0.6, 0.7, 0.8]$$

The reference signals contain frequent step changes in the beginning of experiments to activate input and output signals and improve the identification. The controlled variables  $y_1$  and  $y_2$  are liquid levels of tanks T1 and T2. The manipulated variables  $u_1$  and  $u_2$  are flow rates of liquid into the tanks. As  $w_1$  and  $w_2$  are denoted desired liquid levels in particular tanks (reference signals).

Subsequent experiments were carried out in such a way that initial parameter estimates were set as the last parameter estimates obtained in the ends of the previous experiments.

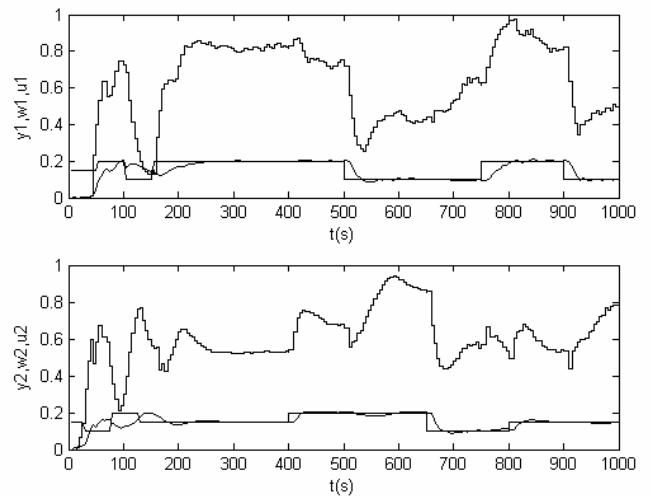


Fig. 5. Control of the laboratory model using 1DOF controller

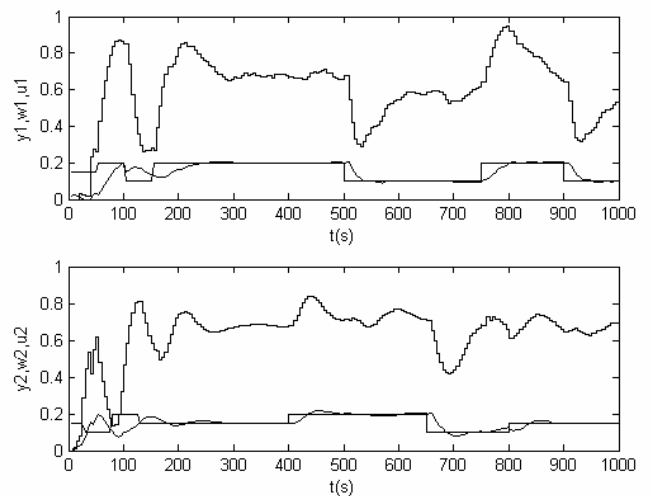


Fig. 6. Control of the laboratory model using 2DOF controller

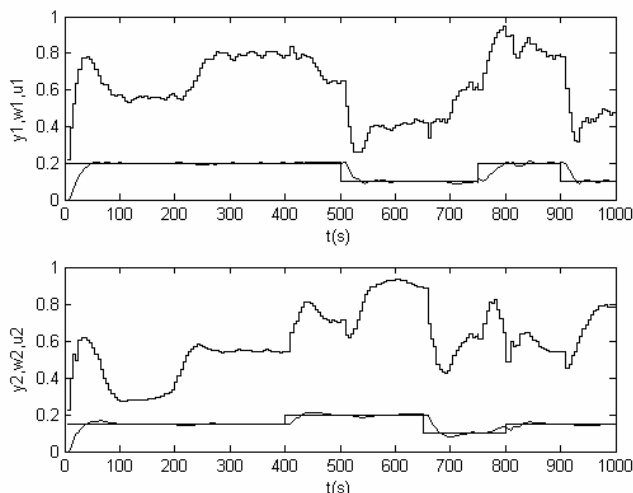


Fig. 7. Control of the laboratory model using 1DOF controller – experiment with steady parameters

The initial conditions of the recursive identification were also modified by reducing of diagonal elements of the square covariance matrix, which represent variances of the identified parameters, from 1000 to 10. Because the system is nonlinear and the identified parameters were valid only for particular steady states, the reference signals were set to the same values as it was in the ends of the previous experiments. Time responses of these experiments are shown in Fig. 6 and Fig. 7.

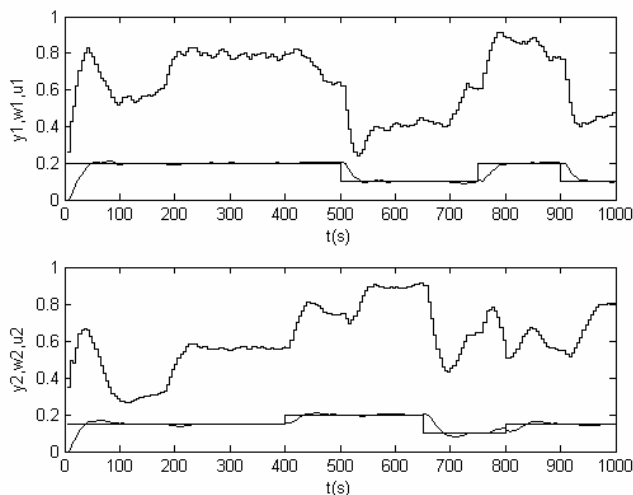


Fig. 8. Control of the laboratory model using 2DOF controller – experiment with steady parameters

## 8. CONCLUSIONS

According to the theoretical assumptions, the controller with the compensator should reduce interactions between the control loops. From the results in Fig. 5 - Fig. 8 it is obvious that similar results were achieved with both controllers from this point of view (overshoots of one controlled variable caused by step changes of the reference signal of the other one were comparable). This is caused by fact that the

decoupling controller is based on inversion of the controlled plant. Such controllers are sensitive to differences between the model and the plant. According to the achieved experimental results the main merit of the decoupling controller lies in much better courses of manipulated variables. Increments of manipulated variables between individual sampling intervals are smaller.

The control tests executed on the laboratory model provide very satisfactory results, despite of the fact, that the non-linear dynamics was described by a linear model. The objective laboratory model simulates technological processes, which frequently occur in industry. The laboratory tests proved that the examined methods could be implemented and used successfully to control such processes.

## ACKNOWLEDGEMENTS

This work was supported in part by the Grant Agency of the Czech Republic under grant No.102/05/0271 and in part by the Ministry of Education of the Czech Republic under grant MSM 7088352101.

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