

# Process control – Exercise 1

## 1 Control of mixer and reactor process

The process flowsheet is shown in Figure 1. Before feeding to the reactor, reactant A needs to be diluted with water to a specified concentration. The mixing with water releases a lot of heat. The main dilution is done in the mixing tank which is also cooled. The conditions in the mixing tank make it difficult to install a concentration sensor here. The mixture is further cooled in a heat exchanger before the concentration is “fine tuned” (and measured) before entering the reactor. The reactor temperature should be kept constant. The flowrate of reactant A is measured.

- Classify the variables (CVs, MVs and important DV)
- Suggest a control structure, which includes use of two ratio controllers

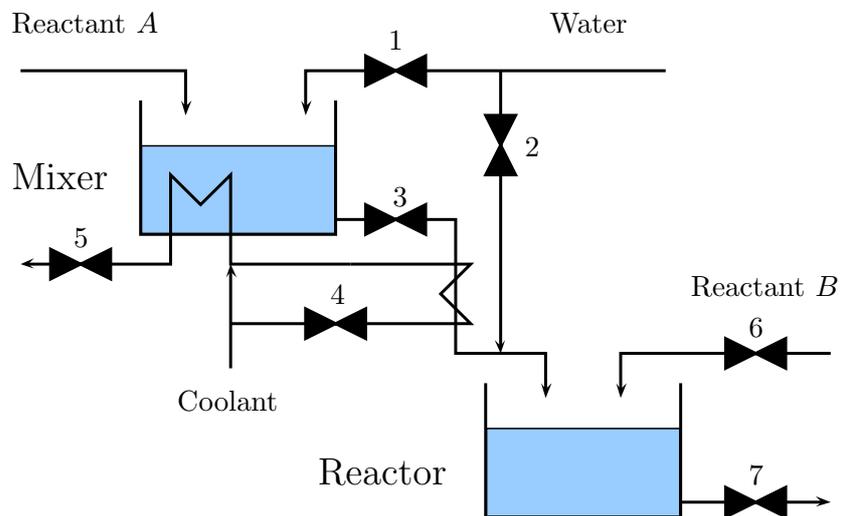


Figure 1: Control of mixer/reactor process

## 2 Temperature control in a tank (similar to control of shower)

The feed to a continuous process enters through a long pipeline, see Figure 2. We assume perfect mixing and constant volume in the tank. The heat loss is neglected. We want to consider how the tank temperature ( $T$ ) changes when the inlet temperature  $T_0$  varies. *Note: Green line means that you should also plot your result by hand by extending the green line in the figures below.*

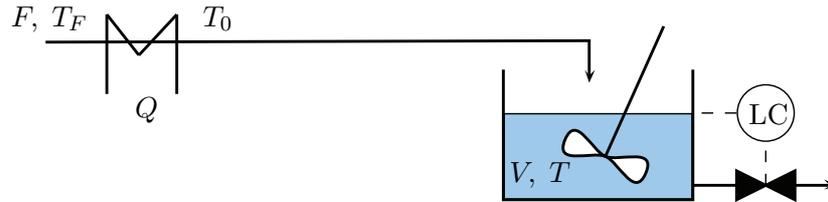


Figure 2: Pipe and tank process

### 2.1 Dynamics

1. Formulate the (dynamic) energy balance for the tank (without the pipeline).
2. Sketch the time response in  $T$  to a step change in  $T_0$  (including the pipeline). *Complete the green line in Figure 3a.*
3. Find the gain ( $k$ ), time constant ( $\tau$ ) and delay ( $\theta$ ) for this process (with  $T_0$  as input and  $T$  as output).

Table 1: Data

parameter	symbol	value	unit
mass flow	( $F$ )	10	$\text{kg s}^{-1}$
water density	( $\rho$ )	1000	$\text{kg m}^{-3}$
pipe area	( $A$ )	0.01	$\text{m}^2$
pipe length	( $L$ )	100	m
tank volume	( $V$ )	0.2	$\text{m}^3$

### 2.2 Control

4. In practice, we can adjust  $T$  by use of an electrical heater ( $Q$ ). Make a flow sheet and show how to control the temperature in the tank ( $y = T$ ) using the heater with a single feedback controller.
5. The time delay due to the long pipe can be a problem for good control of  $T$ . Suggest an improved control structure (with cascade) based on measuring also  $T_0$ . (Comment: The outer cascade is intended, for example, to correct for possible heat loss in the pipe and in the tank).

6. Consider a step disturbance in  $T_F$  (at  $t=100$  s for example).
  - What is the best possible control (ideal control) one can get for  $T$  for this system using feedback based on measuring  $T$ ? **Complete the green line in Figure 3b.**
  - What if we can measure  $T_0$ ?
7. What if we can measure  $T_F(d)$  and use feedforward control; what is the best possible?

### 2.3 Simulation (Extra: will be demonstrated in class in week 2)

Simulate case 4 with  $y = T$  for a step disturbance ( $d$ ) in  $T_F$  using a PI controller with gain  $K_c$  and integral time  $\tau_I$  [s]. The input is the scaled heat input,  $u = \Delta Q/(FC_p)$ .

Use the Simulink file `tunepid1_ex1` (see example code at the bottom):

- Note that we consider deviation variables and we can write  $\Delta T_0 = u + d$ , where  $d = \Delta T_F$  and  $u = \Delta Q/(FC_p)$  (derived from energy balance for the heater).
- Some dynamics have been added for the heater (first-order response with time constant 1 s).
- Disturbances.  $d$  at  $t=100$  s:  $T_F$  goes up by 1 K.

Consider the following cases:

8. No control ( $K_c=0$  which gives  $u = 0$ ). Note: Should be the same as in Task 2. **Complete the green line in Figure 3a.**
9. P-control (keep `taui=99999` at a large value so the I-action is off). Use  $K_c=0.5$ . **Complete the green line in Figure 3c.**
10. P-control. Try increasing  $K_c$ . At what value of  $K_c$  does the system go unstable? Can you explain this?
11. PI-control. Use SIMC rule with `tauc=delay`. **Complete the green line in Figure 3d.**

Start Simulink by writing the following in the Matlab command window:

```
>> tunepid1_ex1 %Alternatively double click the Simulink (.mdl) file
>> Kc=0;taui=99999;taud=0; %This sets the PI controller parameters
>> sim('tunepid1_ex1') % Alternatively press the start button
>> plot(time,Tf,'red',time,u,'blue',time,T,'green')
```

To change the step disturbance settings open the Simulink file and double click Step disturbance ( $d$ ) block. In the pop-up window you can define the time and magnitude of the step.

## 2.4 Figures

In the plots below (Figure 3), the input  $u$  (scaled heat input; blue line) and the disturbance  $T_f$  (red line) are given for the whole simulation, but the output  $T$  (green line) is given up to 300 s. Please sketch by hand the behavior of output  $T$  (green line) for the remaining time.

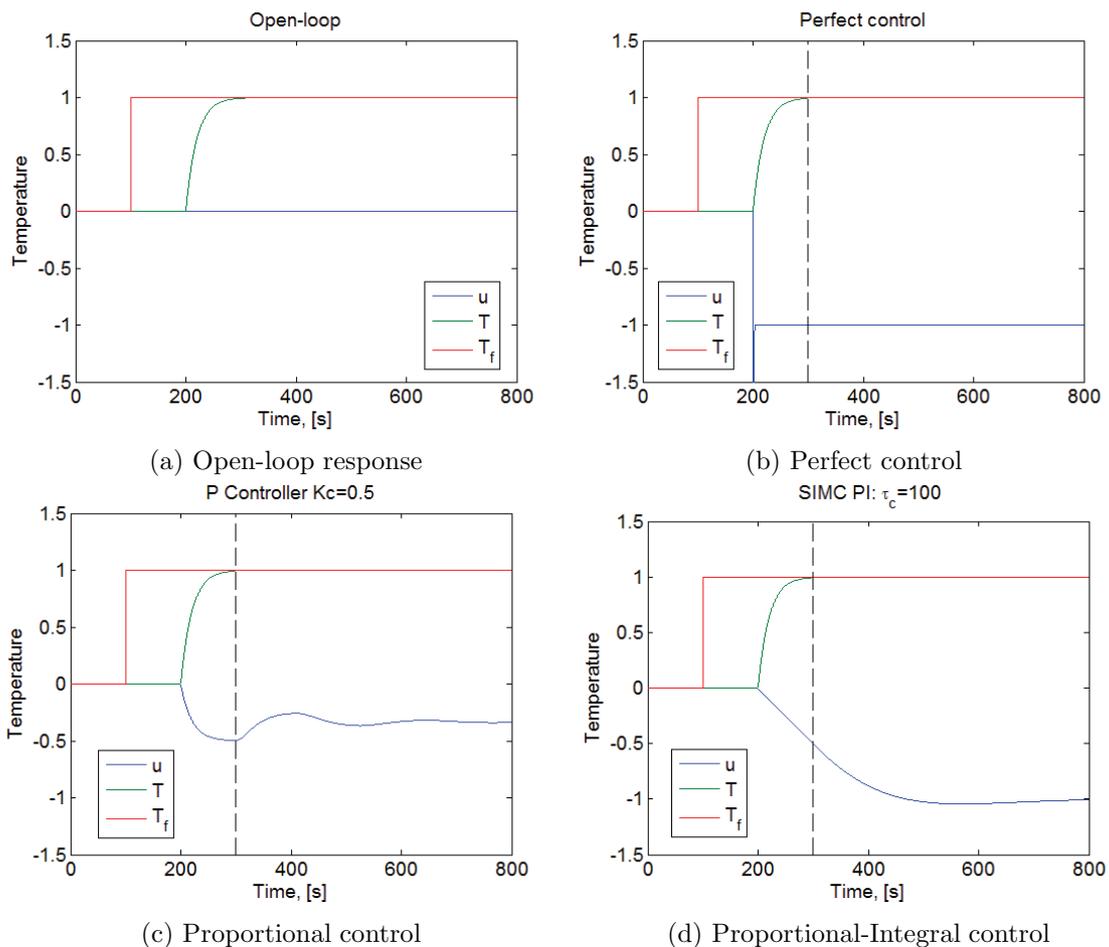


Figure 3: Step response plots