

# Selvoptimaliserende hierarkiske systemer

Prosessregulering, nasjonaløkonomi, hjerne og maratonløping

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# Oversikt

1. Mitt utgangspunkt
2. Styling av virkelige systemer
3. Sentralisert beslutningssystem
4. Hvordan fungerer virkelige styringssystemer?
5. Hvordan designe et hierarkisk system på en systematisk måte?
6. Hva skal vi regulere?
  1. Aktive begrensninger
  2. **Selvoptimaliserende variable**
7. Eksempler: Biologi, prosessregulering, økonomi, maraton

- Fokus: **Ikke** optimal beslutning
- Men: Hvordan **implementere** beslutning på en enkel måte i en usikker verden

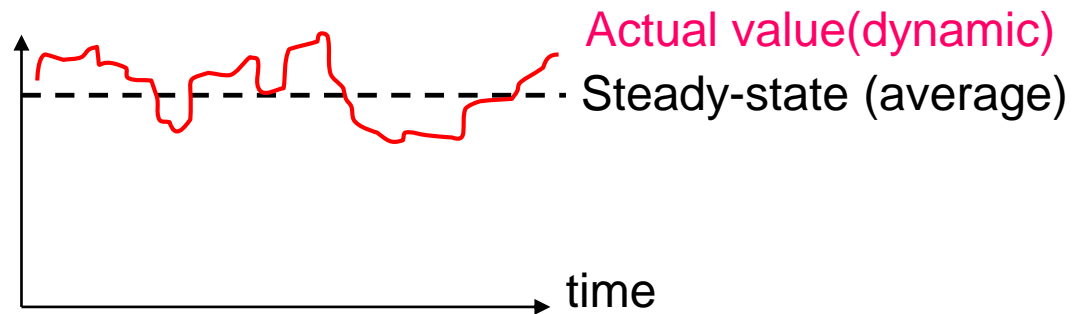
Mitt utgangspunkt: Hvordan skal man regulere et helt prosessanlegg?



Mer generelt: Hvordan designer man komplekse beslutningssystemer?

# Why control (*regulering*) ?

- *Operation*



In practice never steady-state:

- Feed changes
- Startup
- Operator changes
- Failures
- .....

“Disturbances” (d’s)

- Control is needed to reduce the effect of disturbances
- 30% of investment costs are typically for instrumentation and control

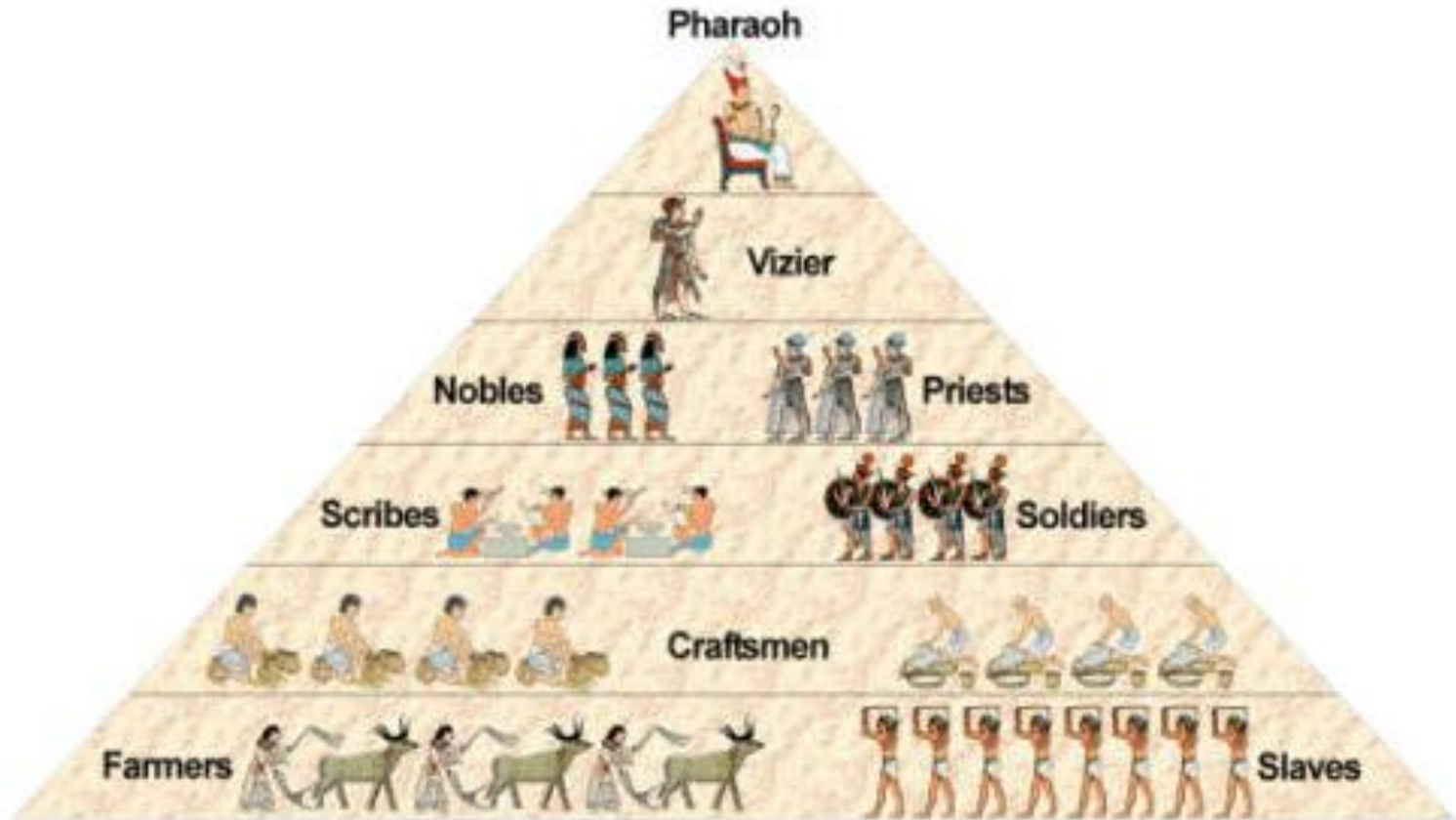
# Main objectives control system

1. Stabilization
2. Implementation of acceptable (near-optimal) operation

ARE THESE OBJECTIVES CONFLICTING?

- Usually NOT
  - Different time scales

# Alle virkelige beslutningssystemer: Hierarkisk pyramide



# Practice: Engineering systems

- Most (all?) large-scale engineering systems are controlled using hierarchies of quite simple controllers
  - Large-scale chemical plant (refinery)
  - Commercial aircraft
- 1000's of loops
- Simple elements

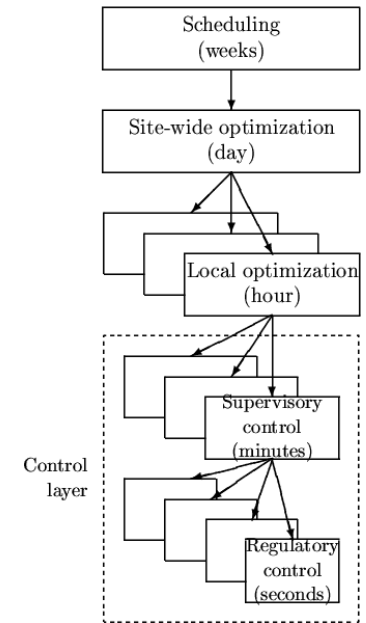
## Same in biological systems

- **Why are real decision systems hierchical and decentralized?**
- **How should such systems be designed?**

# Example: Bicycle riding

Note: design starts from the bottom

- **Stabilizing (regulatory) control:**
  - First need to learn to stabilize the bicycle
    - $CV = y_2 =$  tilt of bike
    - $MV =$  body position



- **Economic (supervisory) control:**
  - Then need to follow the road.
    - $CV = y_1 =$  distance from right hand side
    - $MV = y_{2s}$
  - Usually constant setpoint, e.g.  $y_{1s} = 0.5$  m

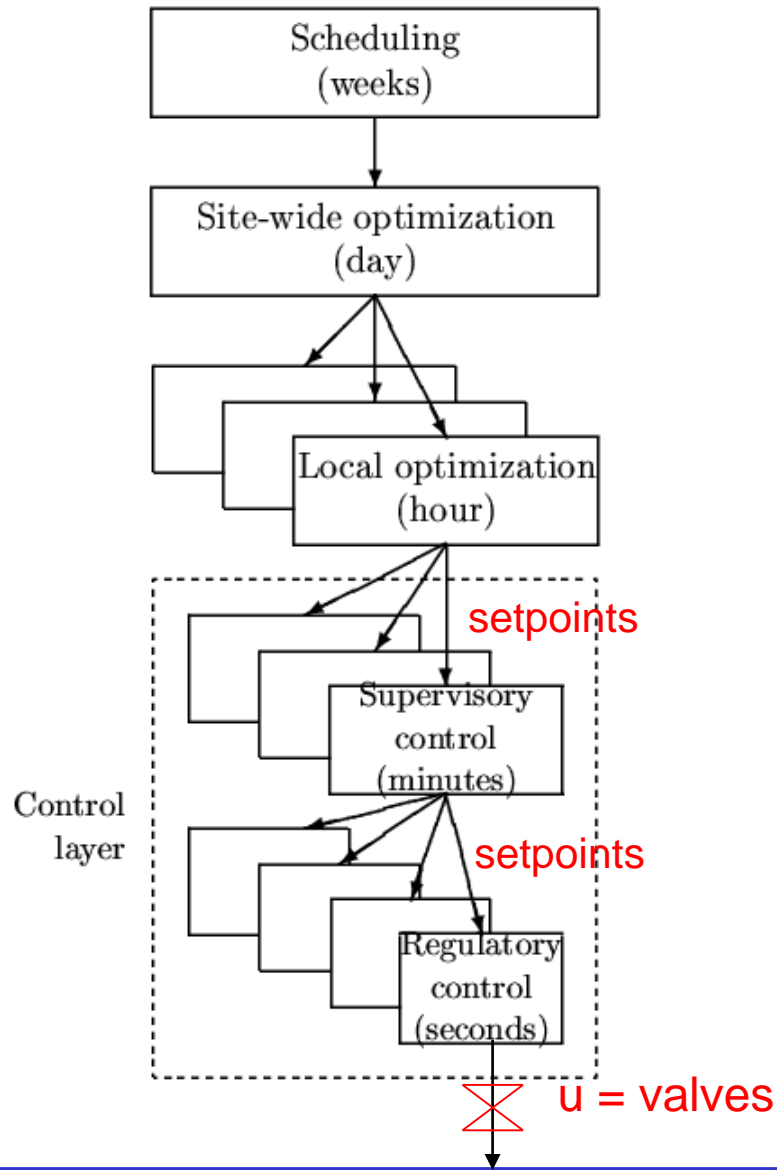


- **Optimization:**
  - Which road should we follow?





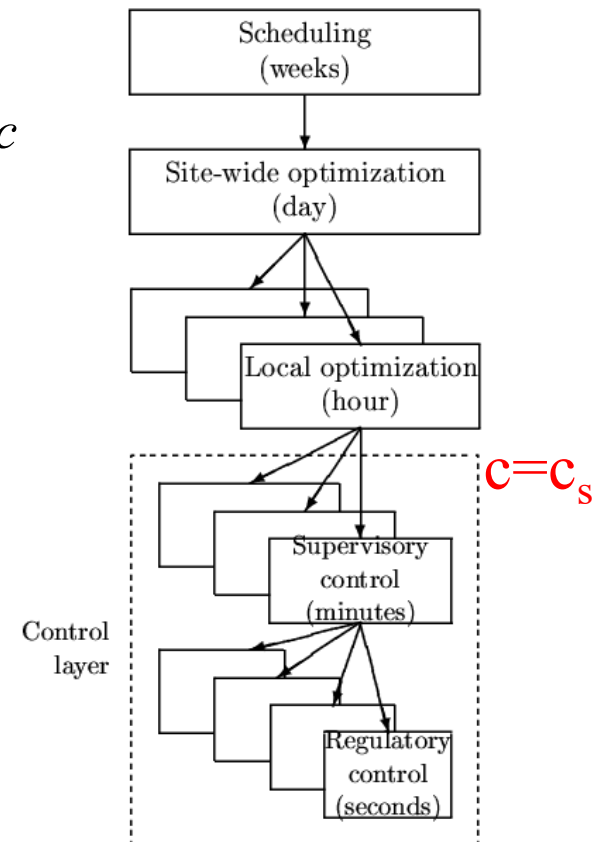
# Process control: Hierarchical structure (pyramid)



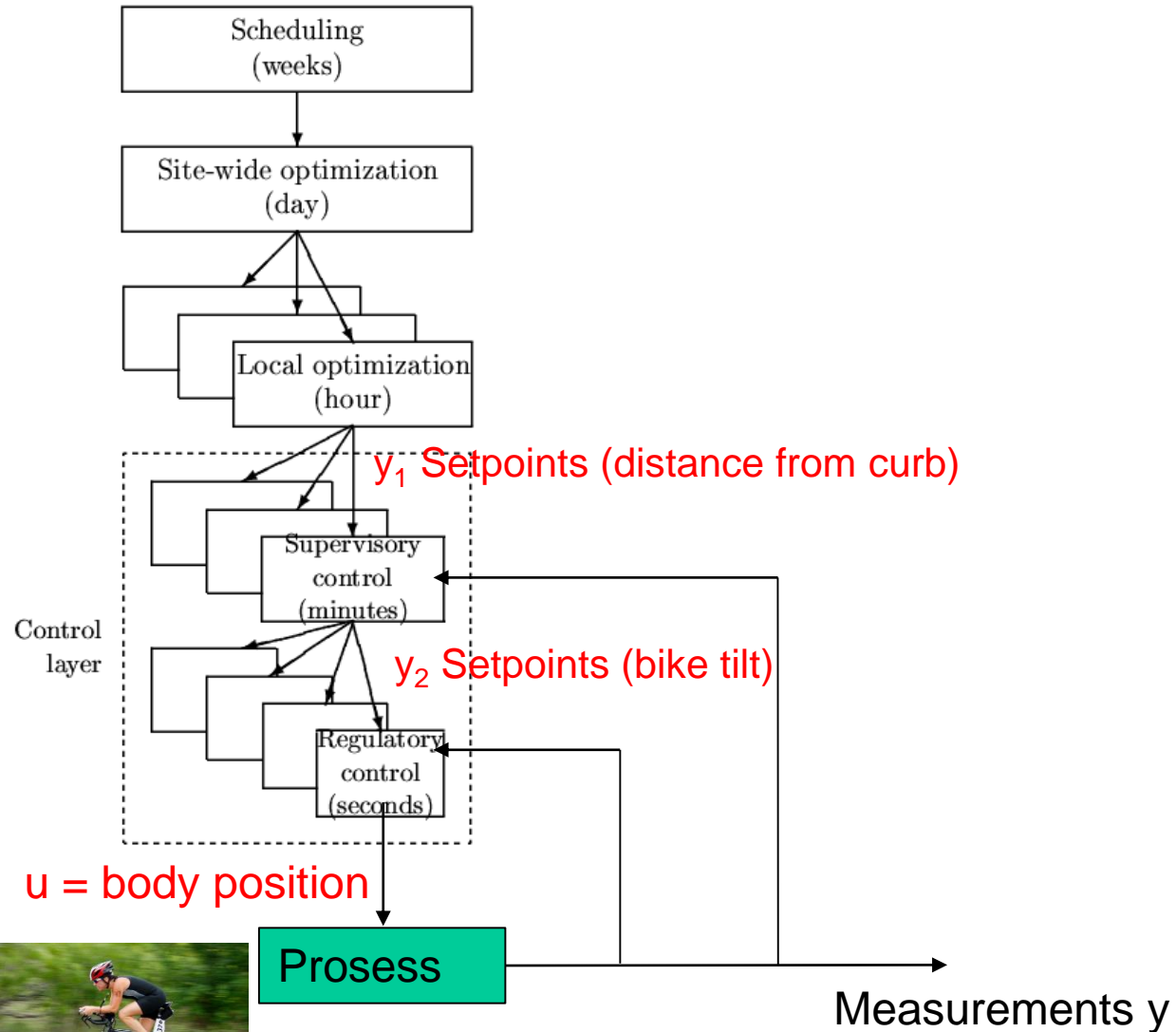
1. Tidsskalaseparasjon
2. Selvoptimaliserende variable
3. Lokal feedback

# Self-optimizing Control

Self-optimizing control is when *acceptable operation* can be achieved using *constant set points* ( $c_s$ ) for the controlled variables  $c$  (without re-optimizing when disturbances occur).

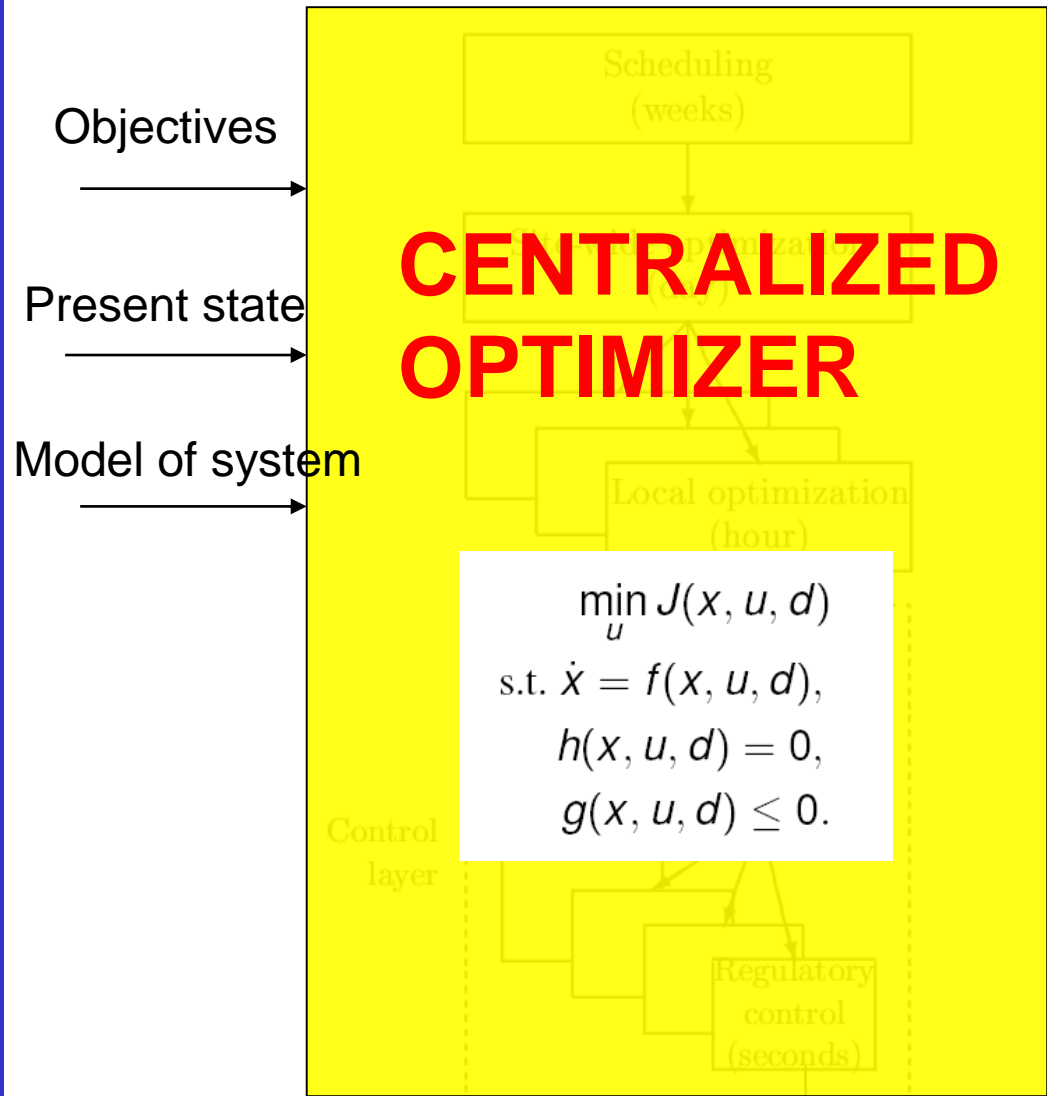


# Håndtere usikkerhet: Lokal feedback



# In theory: Optimal control and operation

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**CENTRALIZED OPTIMIZER**

$$\begin{aligned} & \min_u J(x, u, d) \\ & \text{s.t. } \dot{x} = f(x, u, d), \\ & \quad h(x, u, d) = 0, \\ & \quad g(x, u, d) \leq 0. \end{aligned}$$

Approach:

- Model of overall system
- Estimate present state
- Optimize all degrees of freedom

**Process control:**

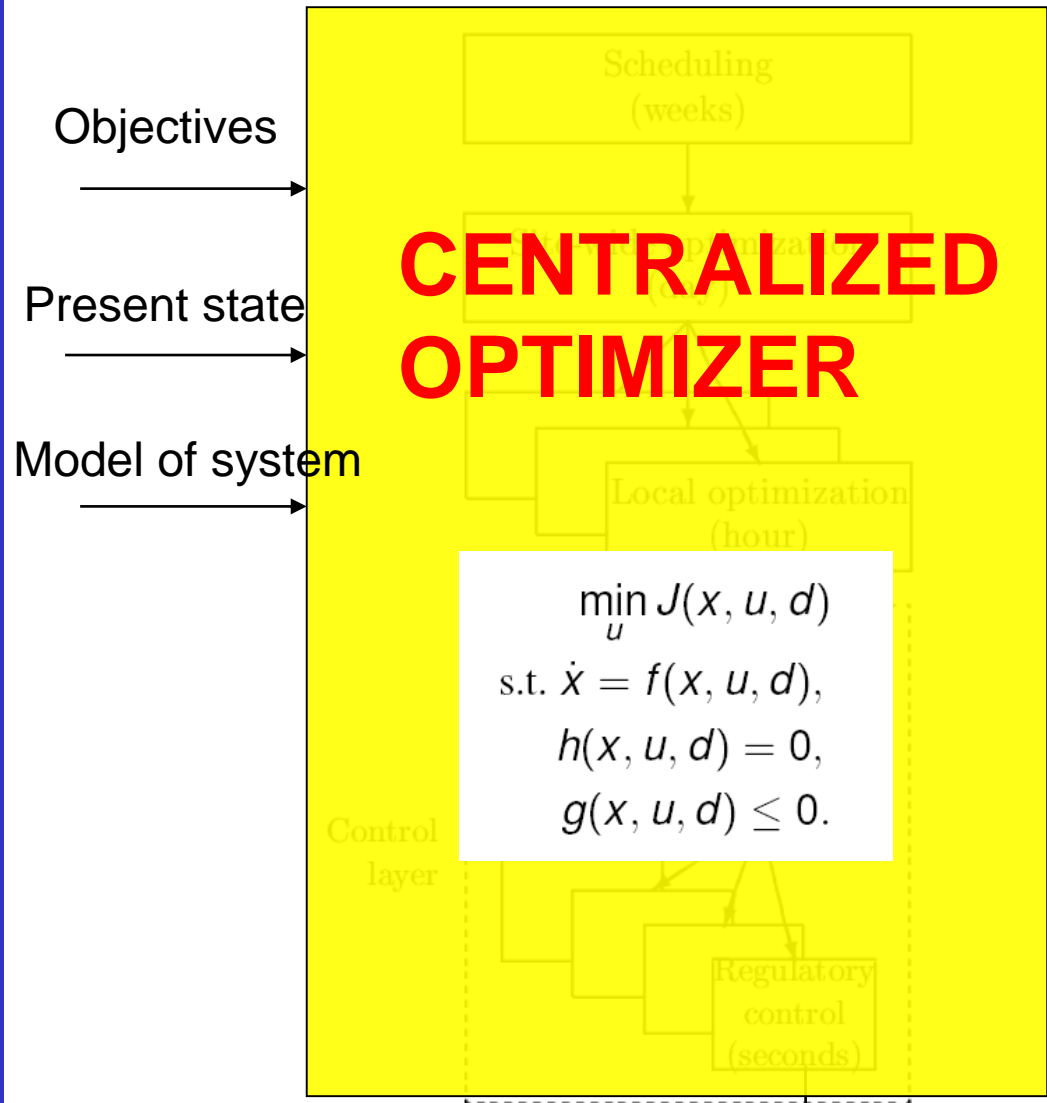
- Excellent candidate for centralized control

Problems:

- Model not available
- Objectives = ?
- Optimization complex
- Not robust (difficult to handle uncertainty)
- Slow response time

~~X~~ (Physical) Degrees of freedom

# In theory: Optimal control and operation



**Approach:**

- Model of overall system
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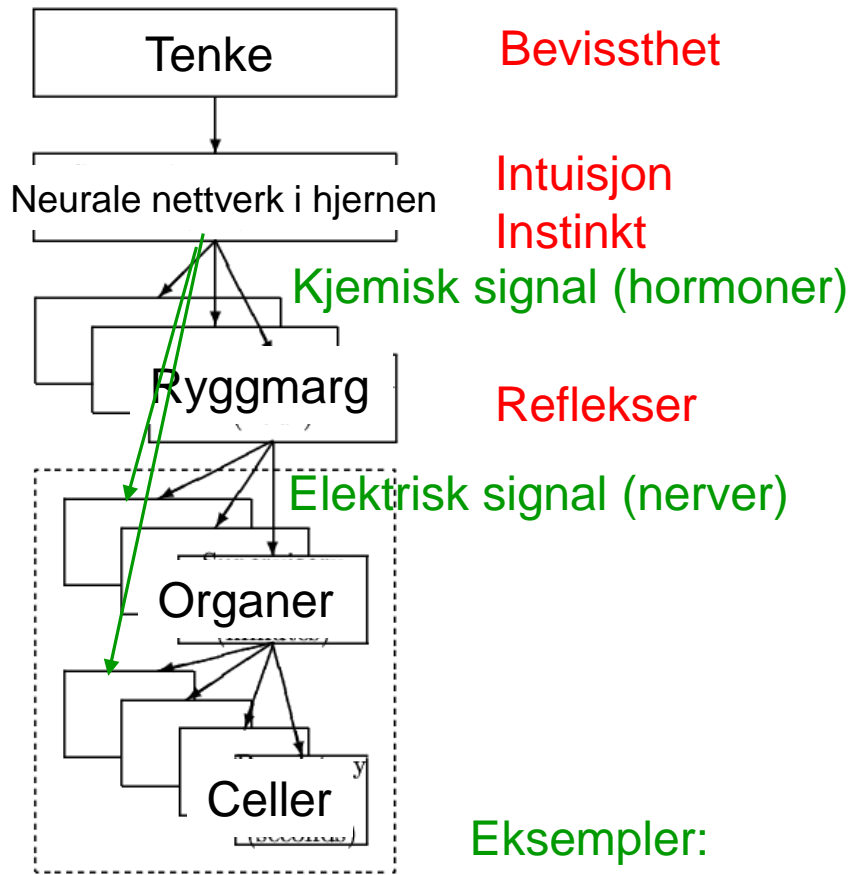
⊗ (Physical) Degrees of freedom

Academic process control community fish pond

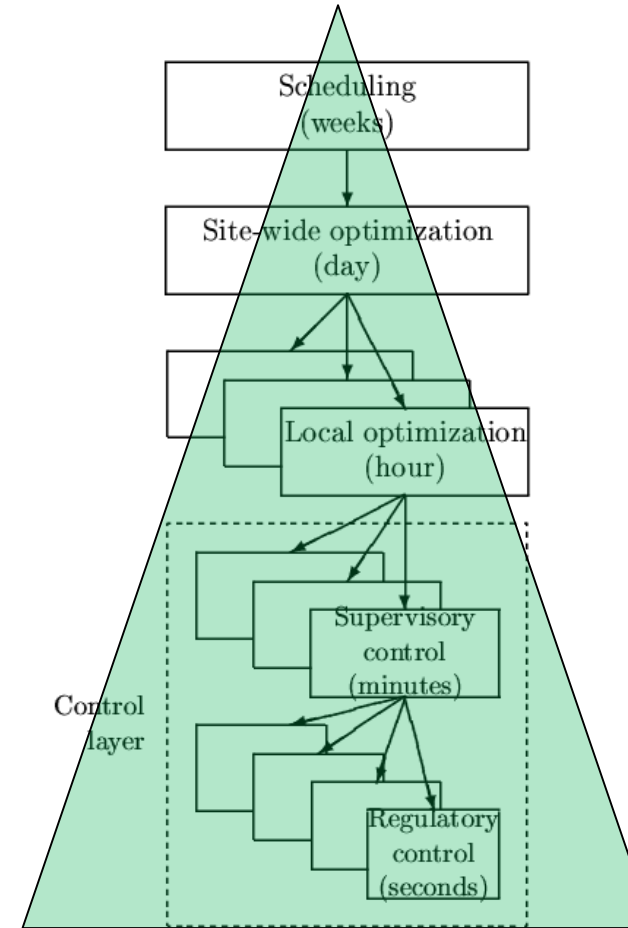
Optimal centralized Solution (EMPC)



# Menneskets beslutningssystem



Eksempler:  
 Temperatur-regulering  
 Puls-regulering  
 Puste-regulering





# To hovedprinsipper for oppdeling av beslutningssystemer (pyramide)

## 1. Tidsskala-separasjon (vertikal oppdeling)

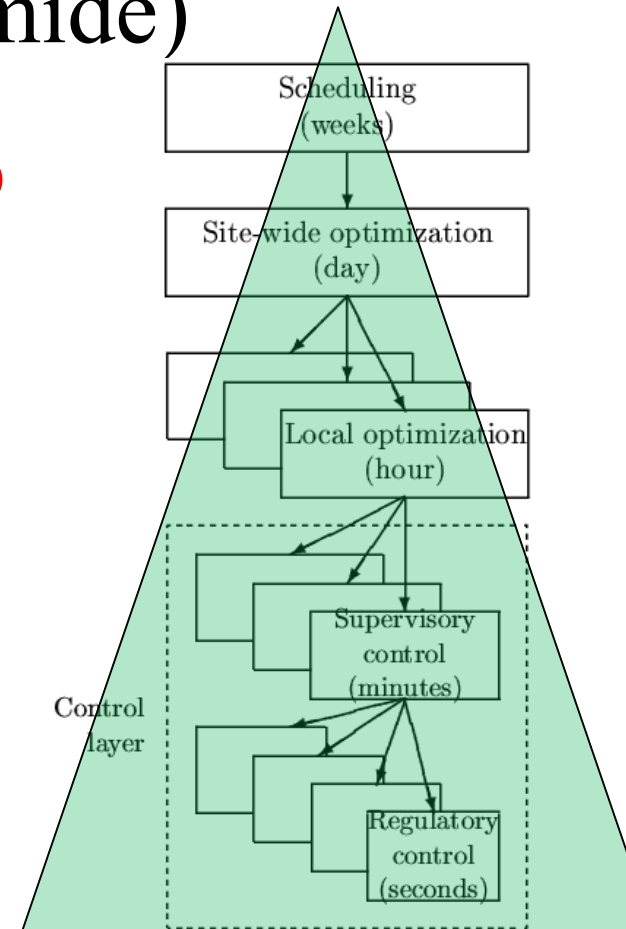
- Hierarkisk (Master-slave)
- Setpunkt sendes nedover
- Rapport om problemer sendes oppover

Intet tap dersom:

- tidsskalaene er separert og man har selvoptimaliserende regulering mellom oppdateringer

## 2. Romlig separasjon (horisontal)

- Desentralisert
- Intet tap dersom oppgaver kan utføres uavhengig av andre på samme nivå



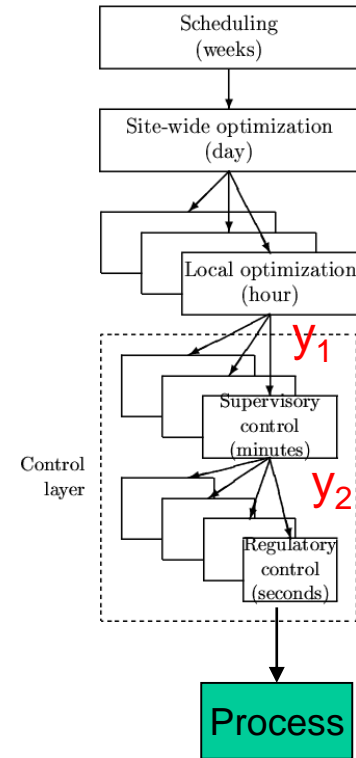
# Systematic approach: Control structure design

## I Top Down

- **Step 1:** Define optimal operation
  - Cost function  $J$  (to be minimized)
  - Operational constraints
- **Step 2:** Identify degrees of freedom and optimize for expected disturbances
  - Identify **Active constraints**
- **Step 3:** Select primary controlled variables  $y_1$ 
  - **Active constraints + Self-optimizing variables**
- **Step 4:** Locate throughput manipulator (process control only)

## II Bottom Up (dynamics, $y_2$ )

- **Step 5:** Regulatory / stabilizing control (PID layer)
  - What more to control ( $y_2$ )?
  - Pairing of inputs and outputs
- **Step 6:** Supervisory control
- **Step 7:** Real-time optimization (Do we need it?)



# Step 1. Define optimal operation (economics)

- What are we going to use our degrees of freedom  $\mathbf{u}$  for?
- Define cost function  $J$  and constraints

$$J = \text{cost feed} + \text{cost energy} - \text{value products}$$

## Step S2. Optimize

(a) Identify degrees of freedom

(b) Optimize for expected disturbances

- Need good model,
- Optimization is time consuming! But it is offline
- Main goal: Identify ACTIVE CONSTRAINTS
- A good engineer can often guess the active constraints

## Step S3: Implementation of optimal operation

- Have found the optimal way of operation.  
How should it be implemented?
- **What to control ?**
  1. Active constraints
  2. Self-optimizing variables (for unconstrained degrees of freedom)

# Optimal operation of runner

- Cost to be minimized,  $J=T$
- One degree of freedom. Input  $u$  (MV)=power
- What should we control?



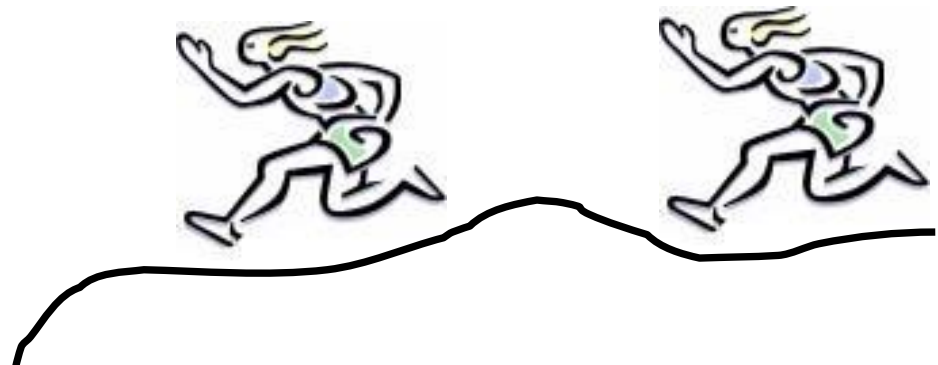
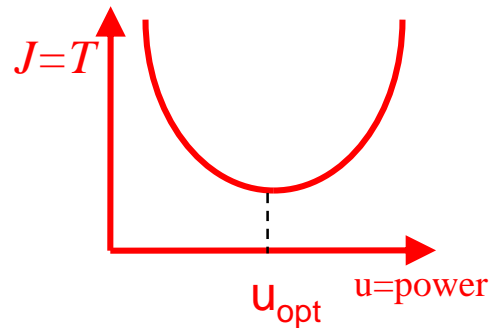
# 1. Optimal operation of Sprinter

- 100m.  $J=T$
- **Active constraint control:**
  - Maximum speed (“no thinking required”)
  - $CV = \text{power (at max)}$



## 2. Optimal operation of Marathon runner

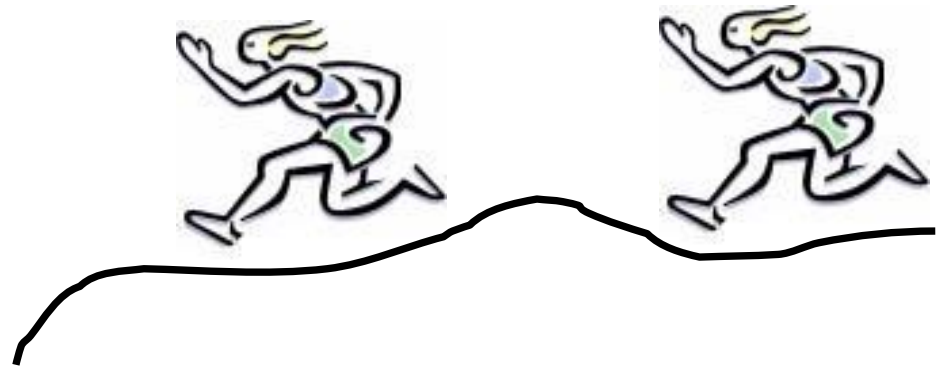
- 40 km.  $J=T$
- What should we control?
- **Unconstrained optimum**



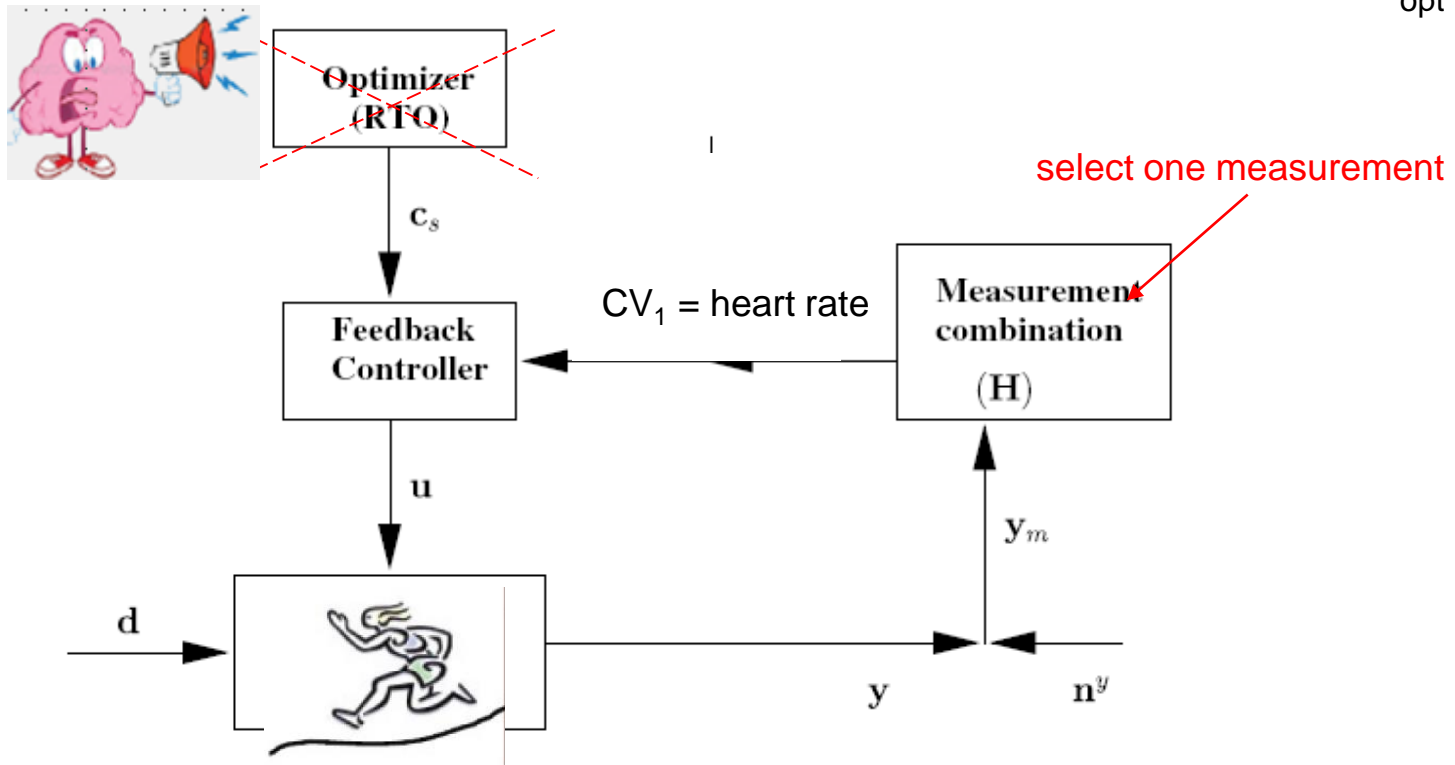
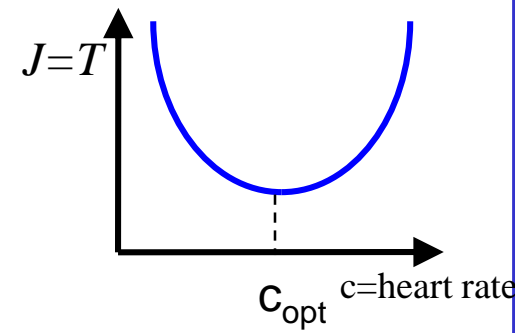


# Self-optimizing control: Marathon (40 km)

- Any **self-optimizing variable** (to control at constant setpoint)?
  - $c_1$  = distance to leader of race
  - $c_2$  = speed
  - $c_3$  = heart rate
  - $c_4$  = level of lactate in muscles



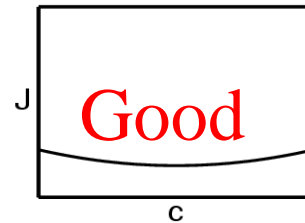
# Conclusion Marathon runner



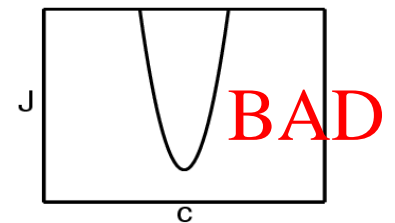
- CV = heart rate is good “self-optimizing” variable
- Simple and robust implementation
- Disturbances are indirectly handled by keeping a constant heart rate
- May have infrequent adjustment of setpoint ( $c_s$ )

# In practice: What variable $c=Hy$ should we control? (for self-optimizing control)

1. **The *optimal value* of  $c$  should be *insensitive* to disturbances**
  - Small  $HF = dc_{opt}/dd$
2.  **$c$  should be easy to measure and control**
3. **The *value* of  $c$  should be *sensitive* to the inputs (“maximum gain rule”)**
  - Large  $G = HG^y = dc/du$
  - Equivalent: Want flat optimum



(b) Flat optimum: Implementation easy



(c) Sharp optimum: Sensitive to implementation errors

Note: Must also find optimal setpoint for  $c=CV_1$

# Example: Cake Baking

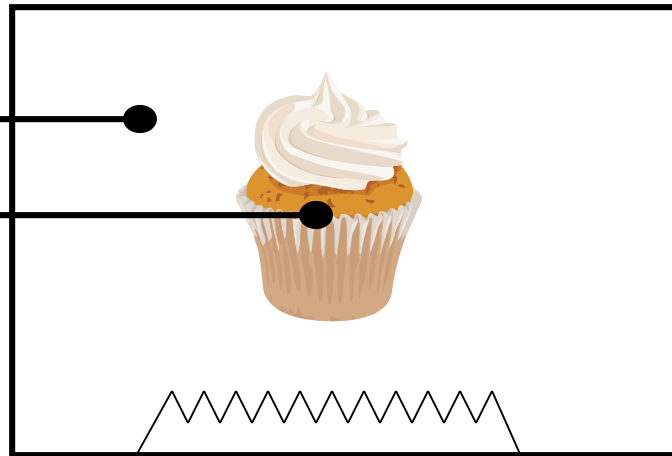
- Objective: Nice tasting cake with good texture

## Measurements

$y_1$  = oven temperature

$y_2$  = cake temperature

$y_3$  = cake color



$u_1$  = Heat input

$u_2$  = Final time

## Degrees of Freedom

## Disturbances

$d_1$  = oven specifications

$d_2$  = oven door opening

$d_3$  = ambient temperature

$d_4$  = initial temperature

# Further examples self-optimizing control

- **Central bank.**  $J$  = welfare.  $u$  = interest rate.  $c$ =inflation rate (2.5%)
- **Cake baking.**  $J$  = nice taste,  $u$  = heat input.  $c$  = Temperature (200C)
- **Business,**  $J$  = profit.  $c$  = "Key performance indicator (KPI), e.g.
  - Response time to order
  - Energy consumption pr. kg or unit
  - Number of employees
  - Research spendingOptimal values obtained by "benchmarking"
- **Investment** (portofolio management).  $J$  = profit.  $c$  = Fraction of investment in shares (50%)
- **Biological systems:**
  - "Self-optimizing" controlled variables  $c$  have been found by natural selection
  - Need to do "reverse engineering" :
    - Find the controlled variables used in nature
    - From this possibly identify what overall objective  $J$  the biological system has been attempting to optimize

Define optimal operation ( $J$ ) and look for "magic" variable ( $c$ ) which when kept constant gives acceptable loss (self-optimizing control)

# Summary Step 3.

## What should we control ( $CV_1$ )?

Selection of primary controlled variables  $c = CV_1$

- 1. Control active constraints!**
- 2. Unconstrained variables: Control self-optimizing variables!**

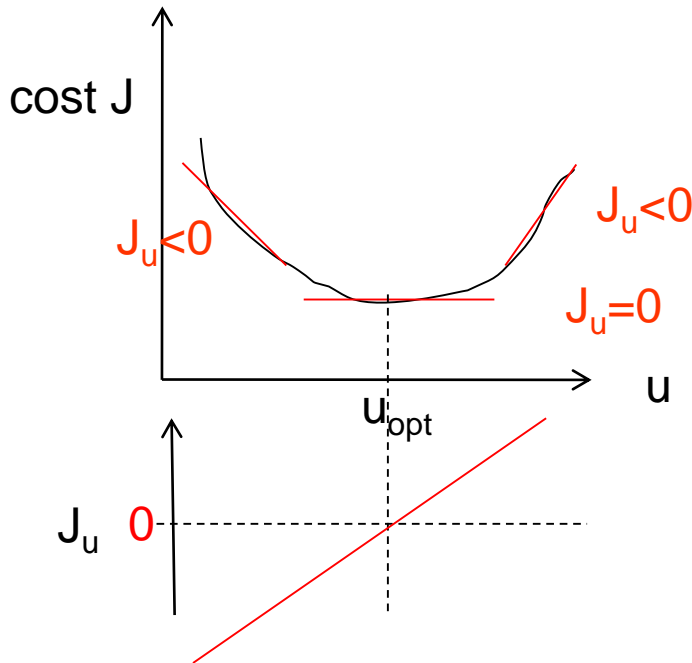
- Old idea (Morari *et al.*, 1980):

*“We want to find a function  $c$  of the process variables which when held constant, leads automatically to the optimal adjustments of the manipulated variables, and with it, the optimal operating conditions.”*

The ideal “self-optimizing” variable is the gradient,  $J_u$

$$\mathbf{c} = \partial J / \partial \mathbf{u} = J_u$$

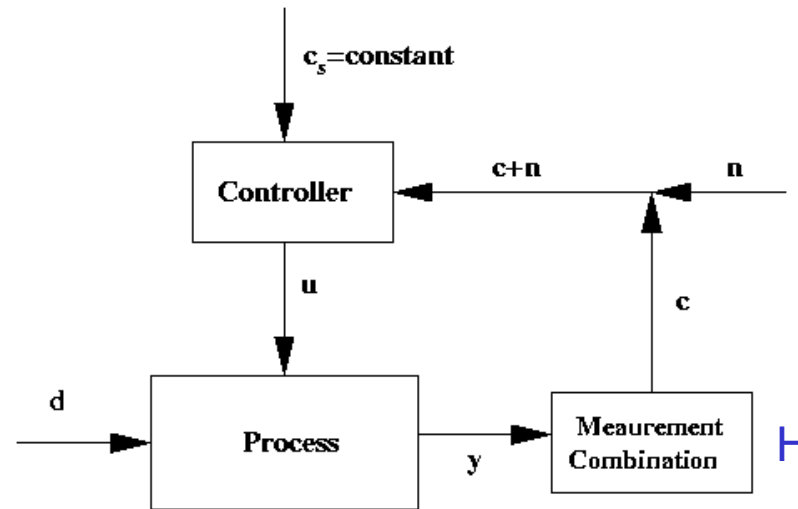
- Keep gradient at zero for all disturbances ( $\mathbf{c} = J_u = 0$ )
- Problem: Usually no measurement of gradient



Ideal:  $c = J_u$

In practise, use available measurements:  $c = H y$ .

**Task: Determine H!**



- Single measurements:

$$c = Hy \quad H = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

- Combinations of measurements:

$$c = Hy \quad H = \begin{bmatrix} h_{11} & h_{12} & h_{13} & h_{14} \\ h_{21} & h_{22} & h_{23} & h_{24} \end{bmatrix}$$



# “Exact local method”

$$\min_H \left\| \underbrace{J_{uu}^{1/2} (HG^y)^{-1}}_{\text{“Minimize” in Maximum gain rule (maximize } S_1 G J_{uu}^{-1/2}, G=HG^y)} \underbrace{H [FW_d \quad W_{ny}]}_{\text{“Scaling” } S_1} \right\|_2$$

“=0” in nullspace method (no noise)

Analytical solution:

$$H = G^y T (Y Y^T)^{-1} \text{ where } Y = [FW_d \quad W_{ny}]$$

- No measurement error: HF=0 (nullspace method)
- With measurement error: Minimize GF<sup>c</sup>
- Maximum gain rule

# Example. Nullspace Method for Marathon runner

$u$  = power,  $d$  = slope [degrees]

$y_1$  = hr [beat/min],  $y_2$  =  $v$  [m/s]

$$F = dy_{\text{opt}}/dd = [0.25 \quad -0.2]'$$

$$H = [h_1 \quad h_2]$$

$$\mathbf{HF} = \mathbf{0} \rightarrow h_1 f_1 + h_2 f_2 = 0.25 h_1 - 0.2 h_2 = 0$$

$$\text{Choose } h_1 = 1 \rightarrow h_2 = 0.25/0.2 = 1.25$$

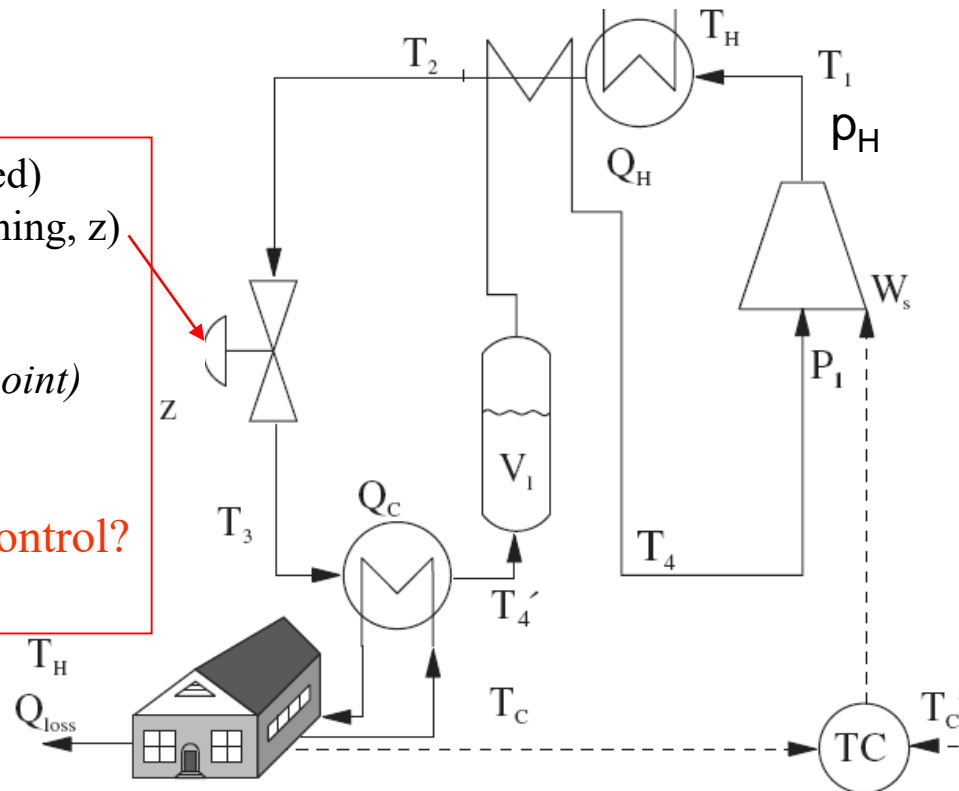
Conclusion:  $\mathbf{c} = \mathbf{hr} + 1.25 \mathbf{v}$

Control  $\mathbf{c} = \mathbf{constant}$   $\rightarrow$  hr increases when  $v$  decreases (OK uphill!)

# Example: CO<sub>2</sub> refrigeration cycle

$J = W_s$  (work supplied)  
 DOF =  $u$  (valve opening,  $z$ )  
 Main disturbances:  
 $d_1 = T_H$   
 $d_2 = T_{Cs}$  (setpoint)  
 $d_3 = UA_{loss}$

What should we control?



# CO2 refrigeration cycle

Step 1. One (remaining) degree of freedom ( $u=z$ )

Step 2. Objective function.  $J = W_s$  (compressor work)

Step 3. Optimize operation for disturbances ( $d_1=T_C$ ,  $d_2=T_H$ ,  $d_3=UA$ )

- Optimum always unconstrained

Step 4. Implementation of optimal operation

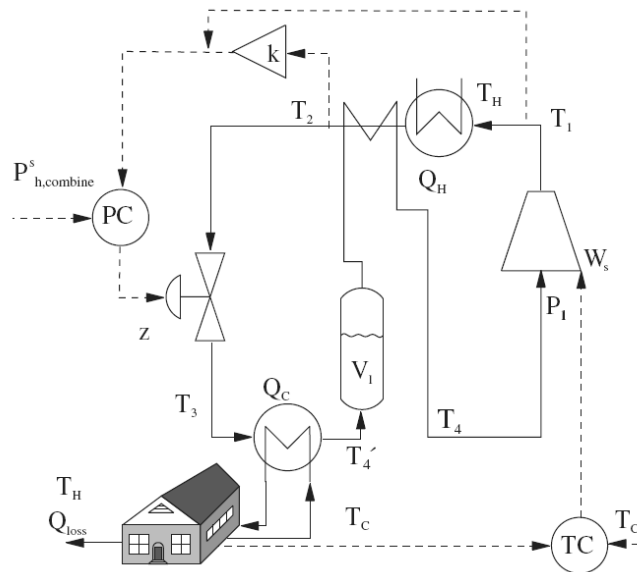
- No good single measurements (all give large losses):
  - $p_h, T_h, z, \dots$
- Nullspace method: Need to combine  $n_u+n_d=1+3=4$  measurements to have zero disturbance loss
- Simpler: Try combining two measurements. Exact local method:
  - $c = h_1 p_h + h_2 T_h = p_h + k T_h; \quad k = -8.53 \text{ bar/K}$
- Nonlinear evaluation of loss: OK!

# CO2 cycle: Maximum gain rule

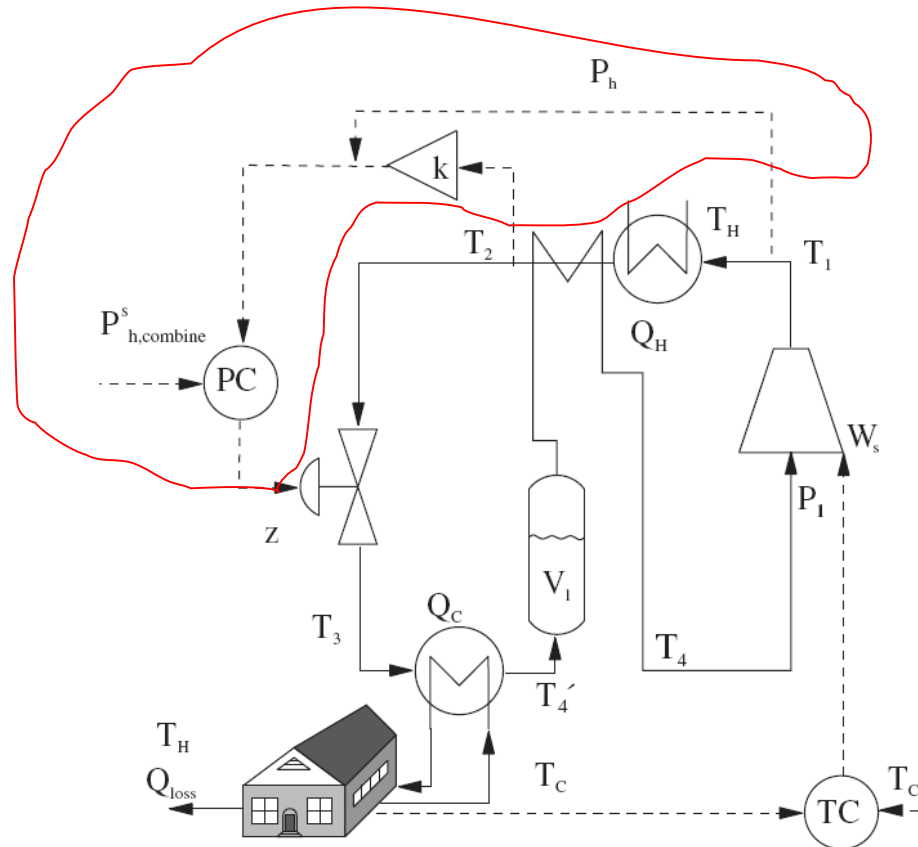
Linear "maximum gain" analysis of controlled variables for CO<sub>2</sub> case

Variable (y)	Nom.	G = $\frac{\Delta y}{\Delta u}$	$\Delta y_{opt}(d_i)$			$\Delta y_{opt}$	n	Span y   $\Delta y_{opt}$   + n	G'  = $\frac{ G }{span_y}$
			d <sub>1</sub> (T <sub>H</sub> )	d <sub>2</sub> (T <sub>C</sub> )	d <sub>3</sub> (UA <sub>loss</sub> )				
P <sub>h</sub> /T <sub>2</sub> ' (bar °C <sup>-1</sup> )	0.32	-0.291	0.140	-0.047	0.093	0.174	0.0033	0.177	0.25
P <sub>h</sub> (bar)	97.61	-78.85	48.3	-15.5	31.0	59.4	1.0	60.4	1.31
T <sub>2</sub> ' (°C)	35.5	36.7	16.27	-2.93	7.64	18.21	1	19.2	1.91
T <sub>2</sub> ' - T <sub>H</sub> (°C)	3.62	24	4.10	-1.92	5.00	6.75	1.5	8.25	2.91
z	0.34	1	0.15	-0.04	0.18	0.24	0.05	0.29	3.45
V <sub>1</sub> (m <sup>3</sup> )	0.07	0.03	-0.02	0.005	-0.03	0.006	0.001	0.007	4.77
T <sub>2</sub> (°C)	25.5	60.14	8.37	0.90	3.18	9.00	1	10.0	6.02
P <sub>h,combine</sub> (bar)	97.61	-592.0	-23.1	-23.1	3.91	33.0	9.53	42.5	13.9
m <sub>gco</sub> (kg)	4.83	-11.18	0.151	-0.136	0.119	0.235	0.44	0.675	16.55

Nullspace method:  $c = p_{h,combine} = h_1 p_h + h_2 T_2 = p_h + k T_2$ ;  $k = -8.53$  bar/K



# Refrigeration cycle: Proposed control structure



CV1= Room temperature

CV2= "temperature-corrected high CO2 pressure"

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7. Eksempler: Biologi, prosessregulering, økonomi, maraton

- **Konklusjon:** Vær systematisk og tenk på helheten når du skal bygge opp et styringssystem
- Enkle løsninger vinner alltid i det lange løp

# References

- The following paper summarizes the design procedure:
  - S. Skogestad, "Control structure design for complete chemical plants", *Computers and Chemical Engineering*, **28** (1-2), 219-234 (2004).
- The following paper updates the procedure:
  - S. Skogestad, "Economic plantwide control", Book chapter in V. Kariwala and V.P. Rangaiah (Eds), *Plant-Wide Control: Recent Developments and Applications*", Wiley (2012).
- More:
  - S. Skogestad "Plantwide control: the search for the self-optimizing control structure", *J. Proc. Control*, 10, 487-507 (2000).
  - S. Skogestad, "Near-optimal operation by self-optimizing control: From process control to marathon running and business systems", *Computers and Chemical Engineering*, 29 (1), 127-137 (2004).
- Mathematical details:
  - V. Alstad, S. Skogestad and E.S. Hori, "Optimal measurement combinations as controlled variables", *Journal of Process Control*, 19, 138-148 (2009)
- More information on my home page (Skogestad):

<http://www.nt.ntnu.no/users/skoge/plantwide>