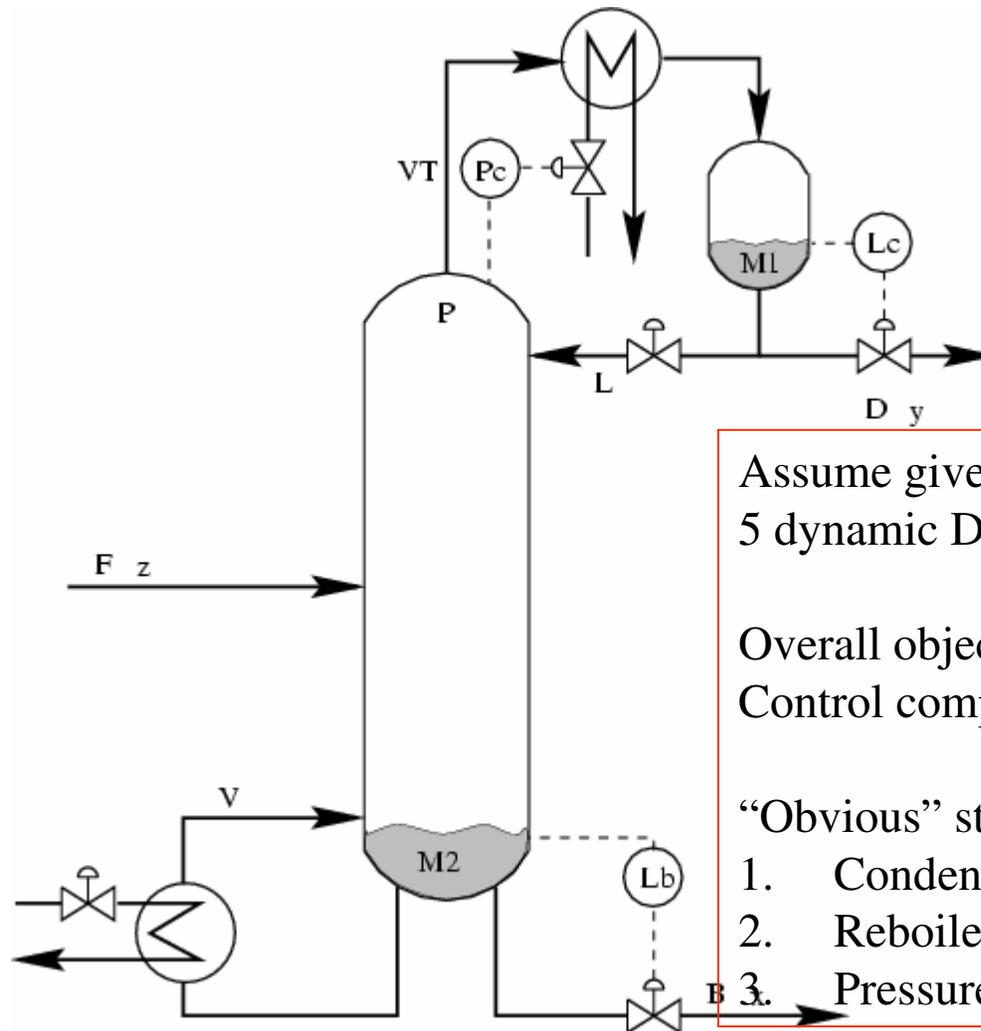


# Example regulatory control: Distillation



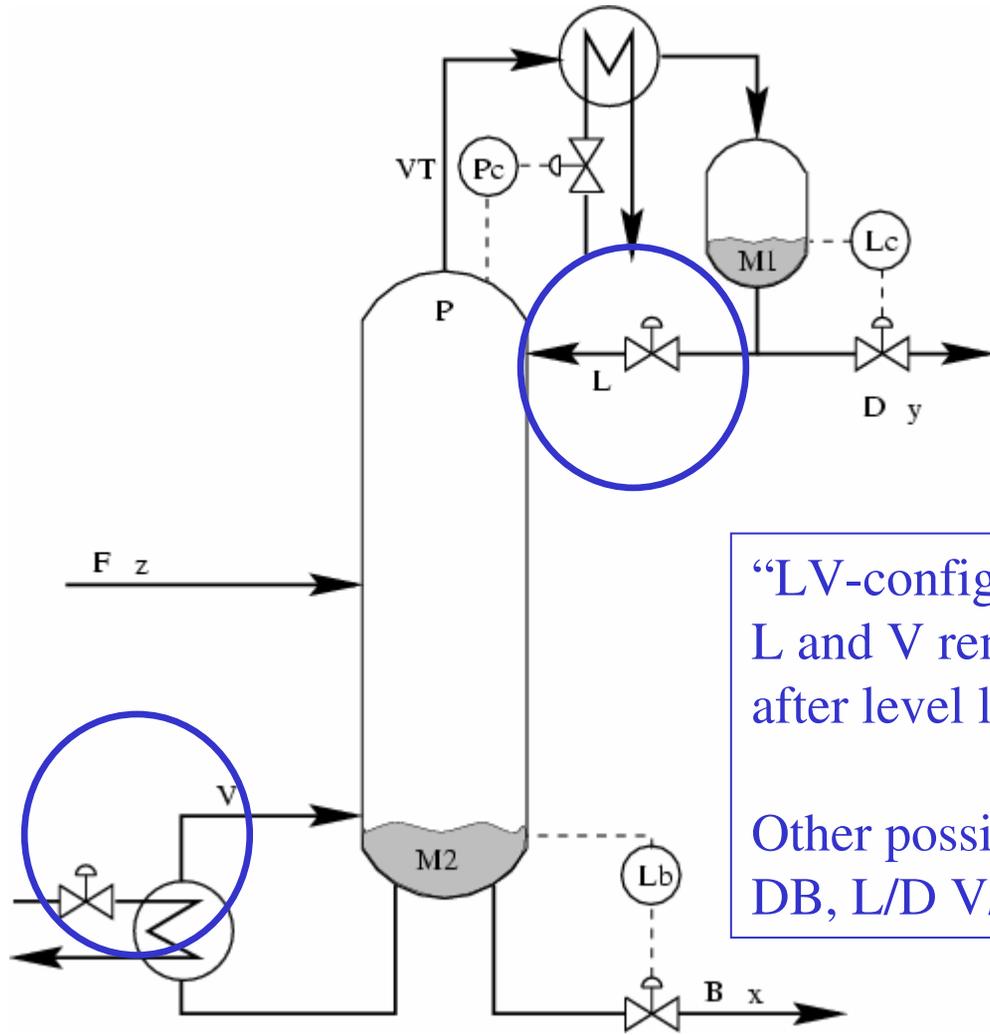
Assume given feed  
5 dynamic DOFs ( $L, V, D, B, V_T$ )

Overall objective:  
Control compositions ( $x_D$  and  $x_B$ )

“Obvious” stabilizing loops:

1. Condenser level ( $M_1$ )
2. Reboiler level ( $M_2$ )
3. Pressure

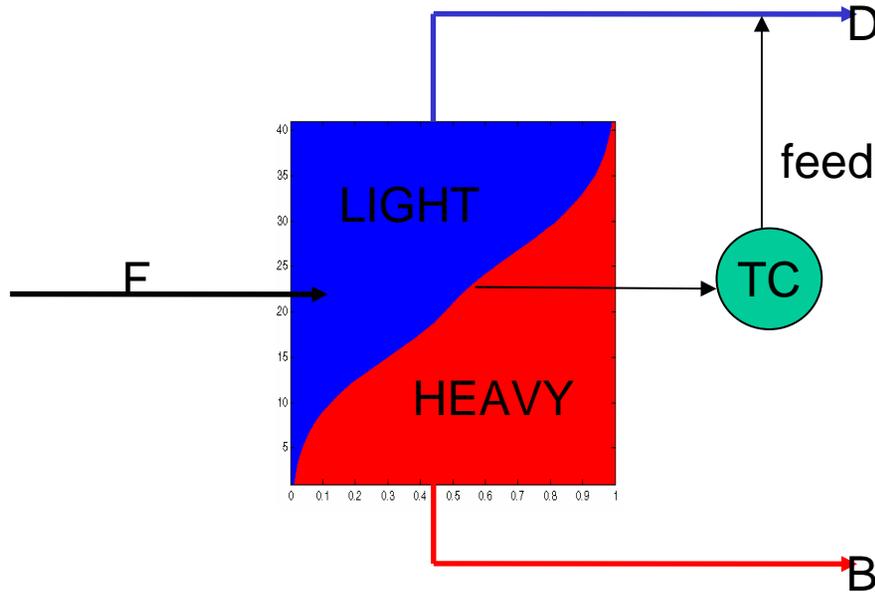
# LV-configuration used for levels (most common)



“LV-configuration”:  
 L and V remain as degrees of freedom  
 after level loops are closed

Other possibilities:  
 DB, L/D V/B, etc....

# BUT: To avoid strong sensitivity to disturbances: Temperature profile must also be “stabilized”



Even with the level and pressure loops closed the column is practically unstable - either close to integrating or even truly unstable ( e.g. with mass reflux: Jacobsen and Skogestad, 1991)

- To stabilize the column we must use feedback (feedforward will give drift)
- Simplest: “Profile feedback” using sensitive temperature

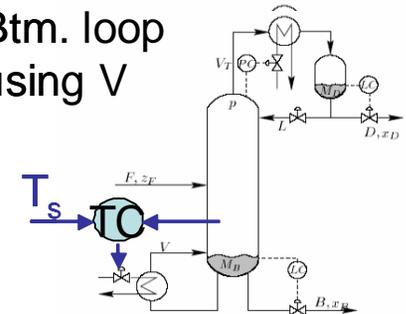
# Stabilizing the column profile

- Should close one “fast” loop (usually temperature) in order to “stabilize” the column profile
  - Makes column behave more linearly
  - Strongly reduces disturbance sensitivity
  - Keeps disturbances within column
  - Reduces the need for level control
  - Makes it possible to have good dual composition control
- P-control usually OK (no integral action)
  - Similar to control of liquid level

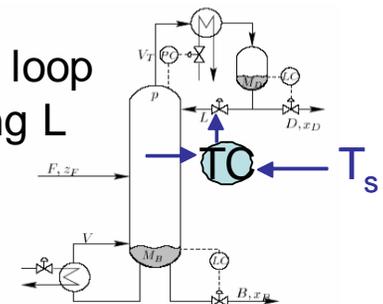
# Stabilizing the column profile

- Which fast loop should be closed (“pairing”)?
  - Which end? Close loop in end with “most important” product
  - Which output (temperature)? Choose “sensitive” stage
  - Which input (flow)? Want fast control  $\Rightarrow$  “pair close”
    - “Use same end” (reduces interactions for composition control):
      - Use V (or indirect by B) for temperature control in bottom section
      - Use L (or indirect by D) for temperature control in top section
- Dynamics
  - L: Some delay for liquid to go down the column
  - V: Vapor flow moves quickly up the column, but may take some time before it starts changing (heat transfer dynamics)
- In general, for stabilizing loops: Avoid using an input (flow) that can saturate

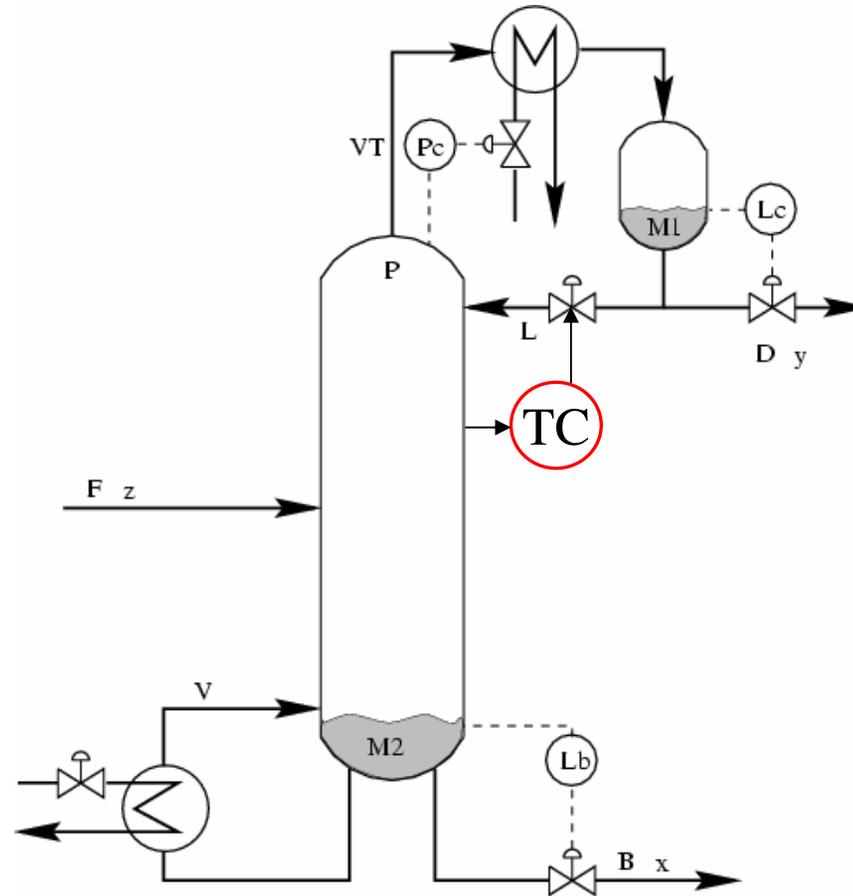
Btm. loop using V



Top loop using L



# Temperature control: Which stage?



# Example column

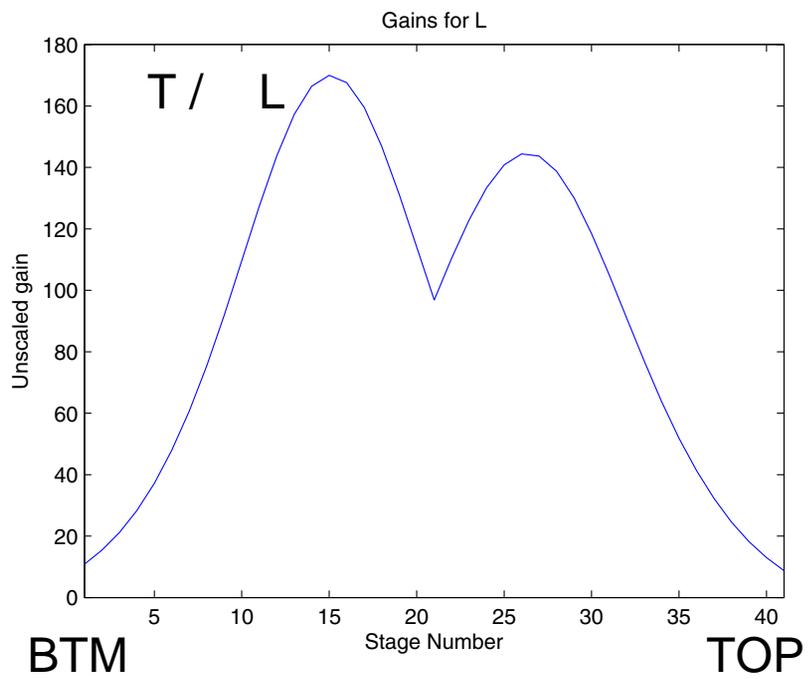
- Example: Ideal 4-component mixture (A,B,C,D) with all relative volatilities = 1.5
  - $\alpha_{AB} = \alpha_{BC} = \alpha_{CD} = 1.5$
- 40 stages and feed in middle of column
- Two cases:
  - Binary: 50% B and 50% C (“column A”)
  - Multicomponent: Equimolar feed (25% if each)
- B and C are key components
- Top product: 1% H (C), Bottom product: 1% L (B)

# Which temperature?

Rule: Maximize the scaled gain

- Scalar case. Minimum singular value = gain  $|G|$
- Maximize scaled gain:  $|G| = |G_0| / \text{span}$ 
  - $|G_0|$ : gain from independent variable (u) to candidate controlled variable (c)
  - span (of c) = variation (of c) = optimal variation in c + control error for c

Binary distillation: Unscaled steady-state gain  
 $G_0 = \Delta T / \Delta L$  for small change in L



# Procedure scaling

1. Nominal simulation
2. Unscaled gains (“steady-state sensitivity”)
  - Make small change in input (L) with the other inputs (V) constant.  
Find gain =  $T_i / L$
  - Do the same for change in V

3. Obtain scalings (“optimal variation for various disturbances”)

Find  $T_{i,opt}$  for the following disturbances

1. F (from 1 to 1.2)                       $y_{optf}$
2.  $z_F$  from 0.5 to 0.6                       $y_{optz}$

“Optimal” may be defined in two different ways

1. **SCALING 1 (normally used)**. Keep constant  $x_D$  and  $x_B$  by changing both L and V (disturbance in F has no effect in this case)
2. **SCALING 2 (in some cases)**. Change only L (or V) and minimize 2-norm of product composition offset

4. Control (implementation) error. Assume=0.5 K on all stages

5. Find

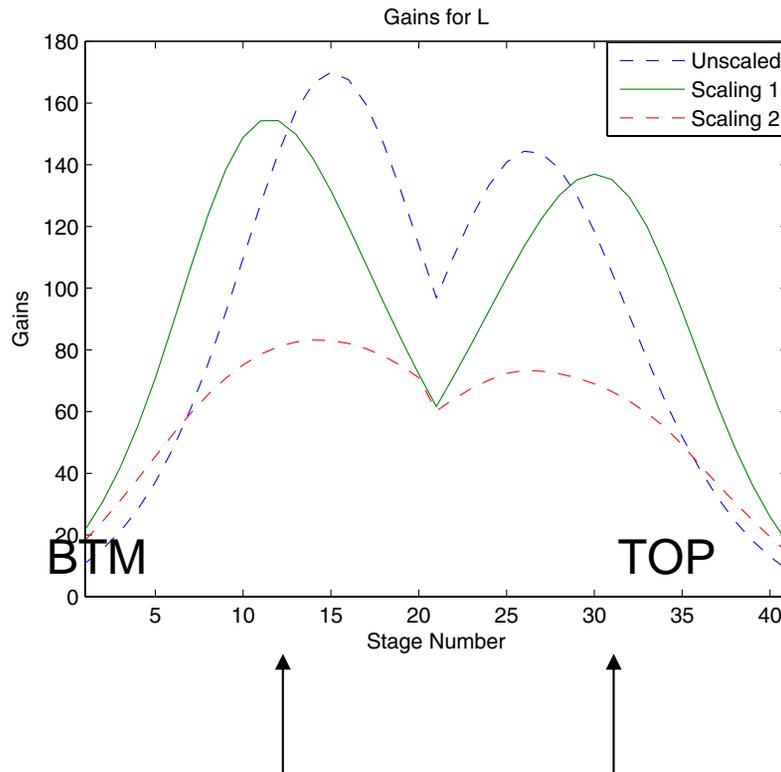
$$\text{scaled-gain} = \text{gain}/\text{span}$$

$$\text{where } \text{span} = \text{abs}(y_{optf}) + \text{abs}(y_{optz}) + 0.5$$

“Maximize gain rule”: Prefer stage where scaled-gain is large

$$\text{Scaled gain} = \frac{\text{Gain}}{\text{span}} = \frac{(\text{unscaled})\text{Gain}}{\text{noise} + \text{opt. variation}}$$

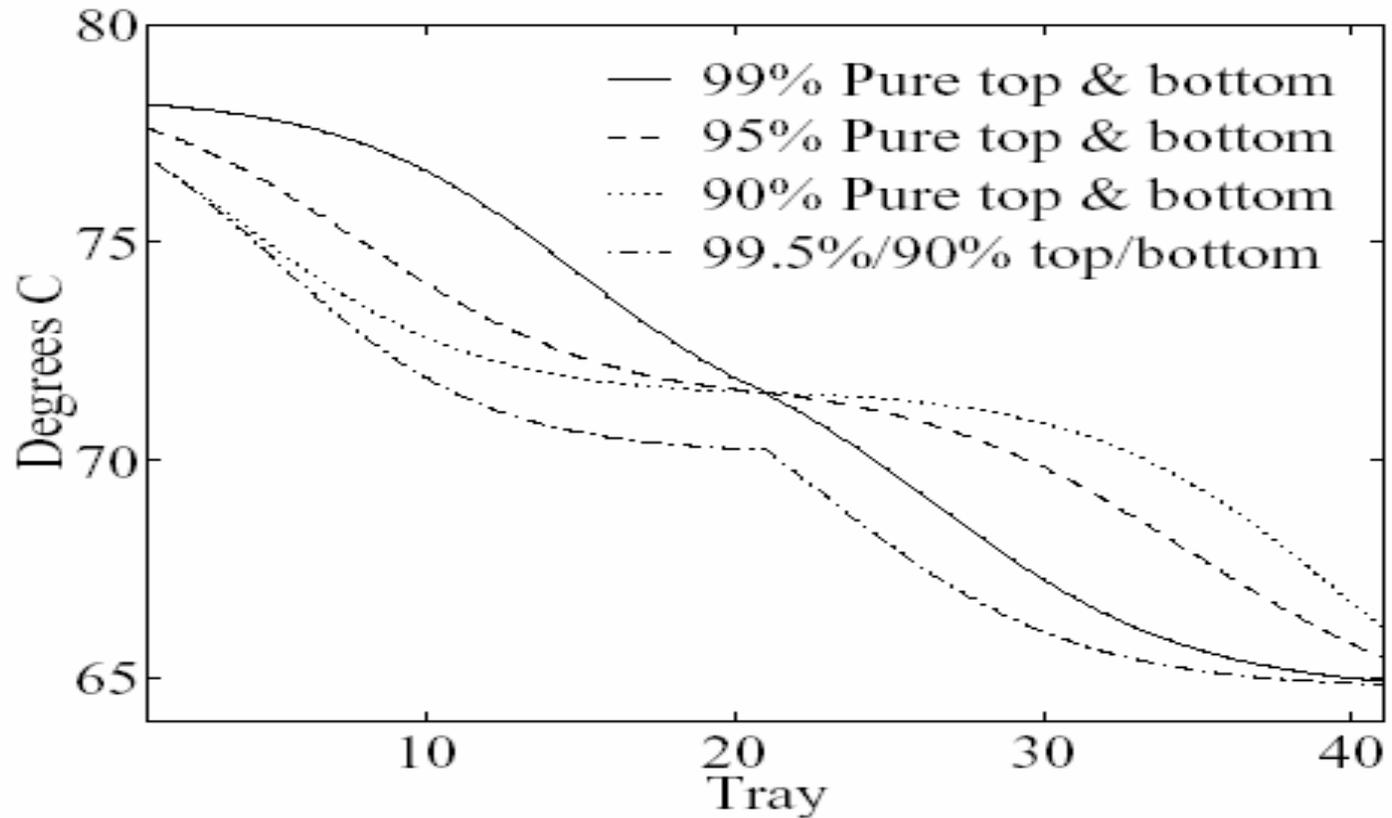
Implementation error used ,  $n = 0.5C$



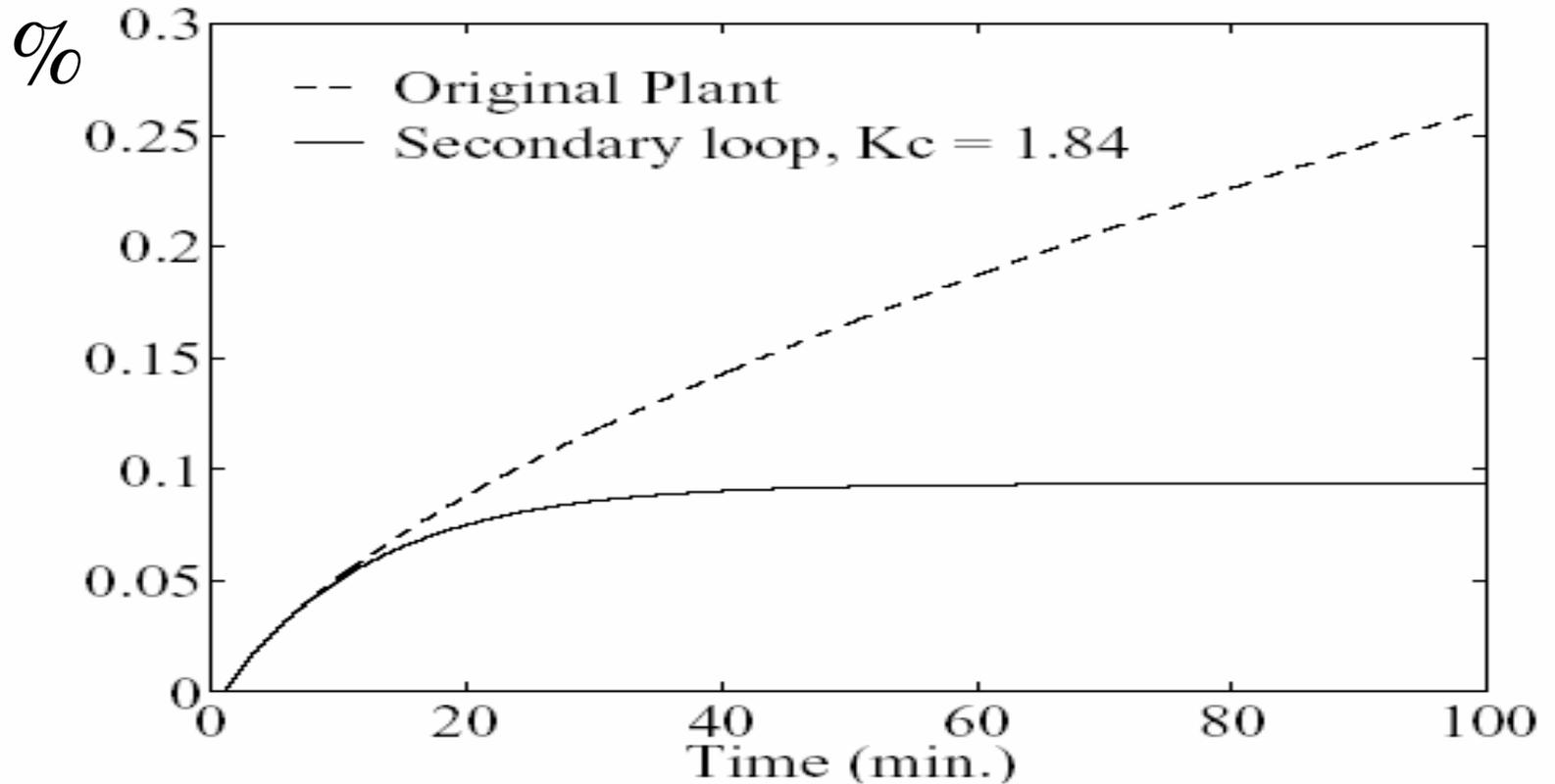
Conclusion:

- Control in middle of section (not at column ends or around feed)
- Scalings not so important here

Maximum gain rule:  
 Tray 30 is most sensitive (middle top section)

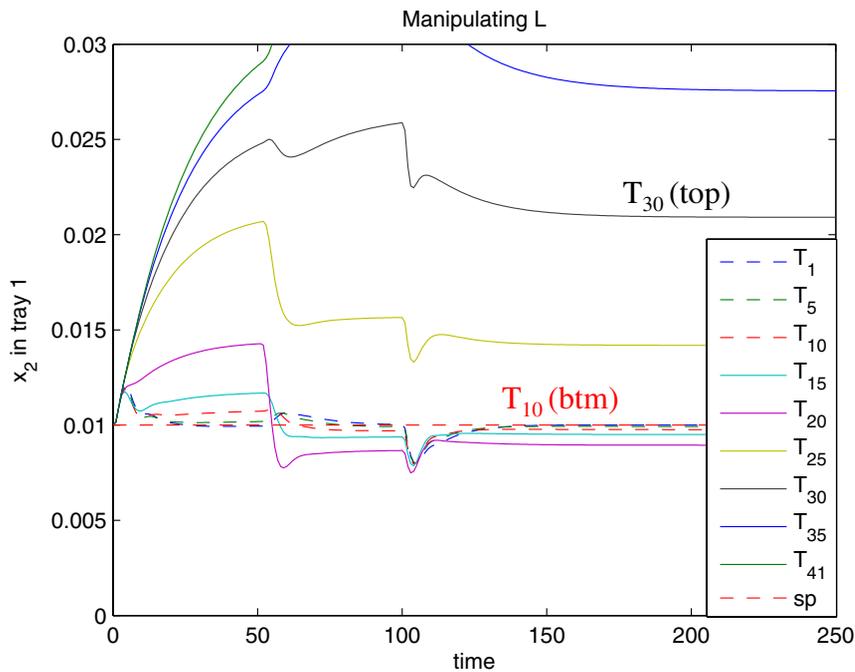


# Simulation with temperature loop closed: Response in $x_B$ to 1% feedrate change

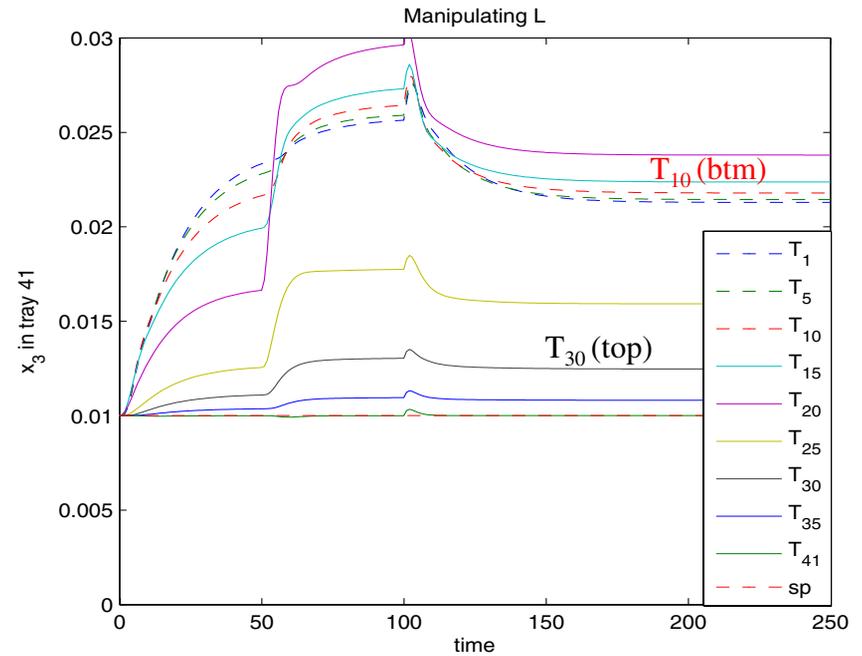


# Simulation: Response with temperature loop closed using L (can improve with L/F!)

## BTM COMPOSITION ( $x_{\text{impurity}}$ )



## TOP COMPOSITION ( $x_{\text{impurity}}$ )



Disturbances:

$F$  changes from 1 to 1.1 at  $t = 0$

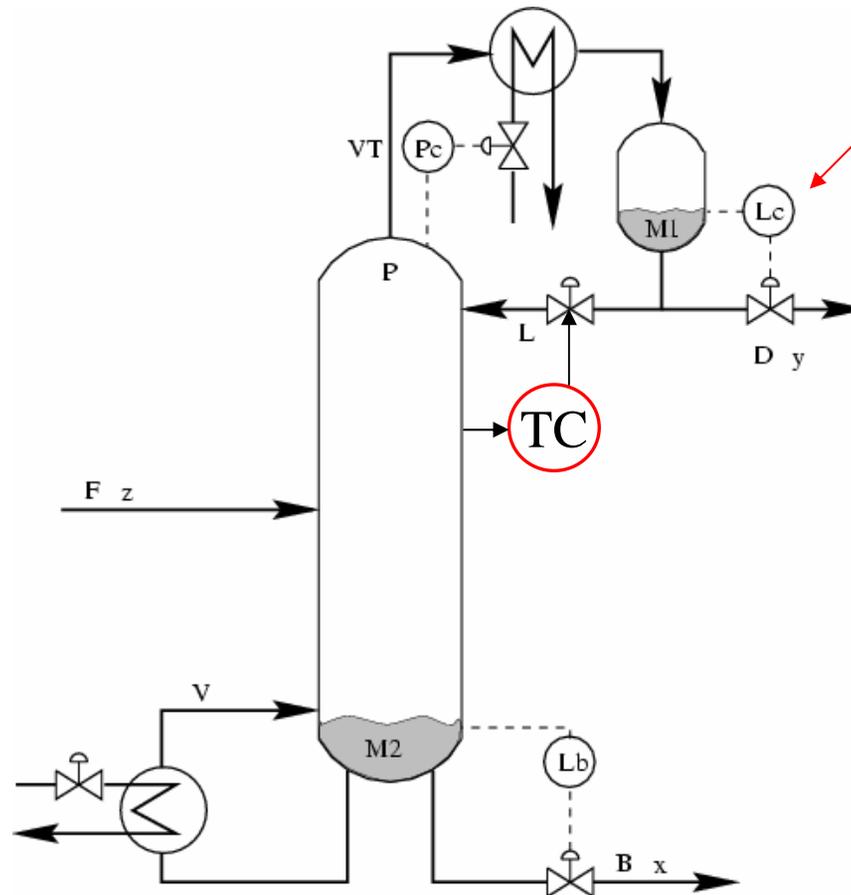
$z_F$  changes from 0.5 to 0.55 at  $t = 50$

$q_F$  changes from 1 to 0.9 at  $t = 100$

Note(as expected!):

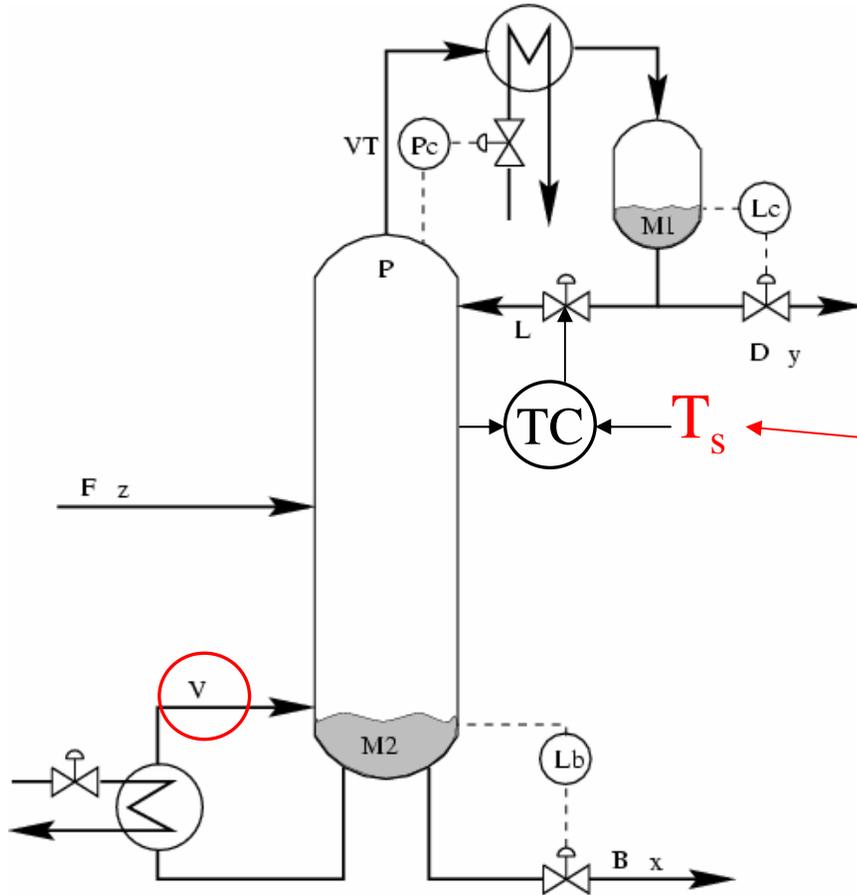
- Temp. meas. in top  $\rightarrow$  Top comp. OK
- Temp. meas. in btm  $\rightarrow$  Btm. comp. OK

# Bonus 1 of temp. control: Indirect level control



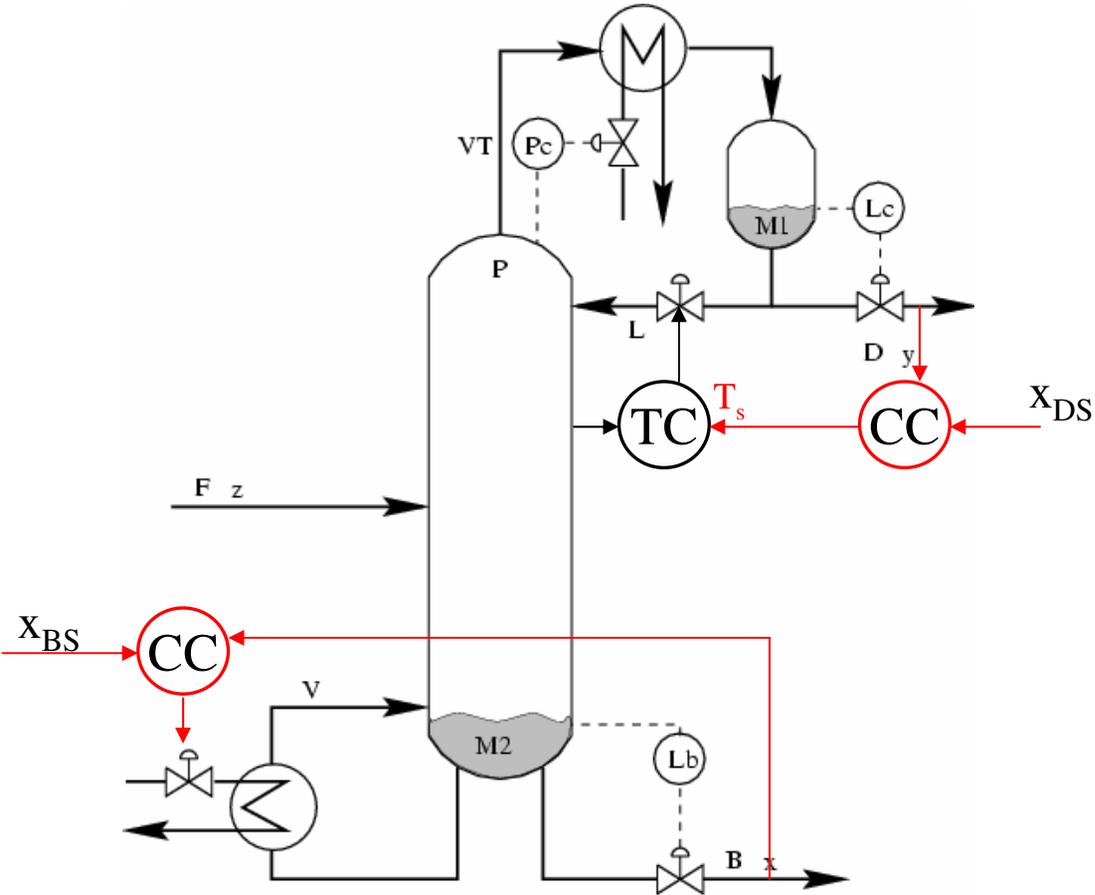
Disturbance in  $V, q_F$ :  
Detected by TC  
and counteracted by L  
-> Smaller changes  
in D required to keep  
 $M_d$  constant!

# Bonus 2 of temp. control: Less interactive

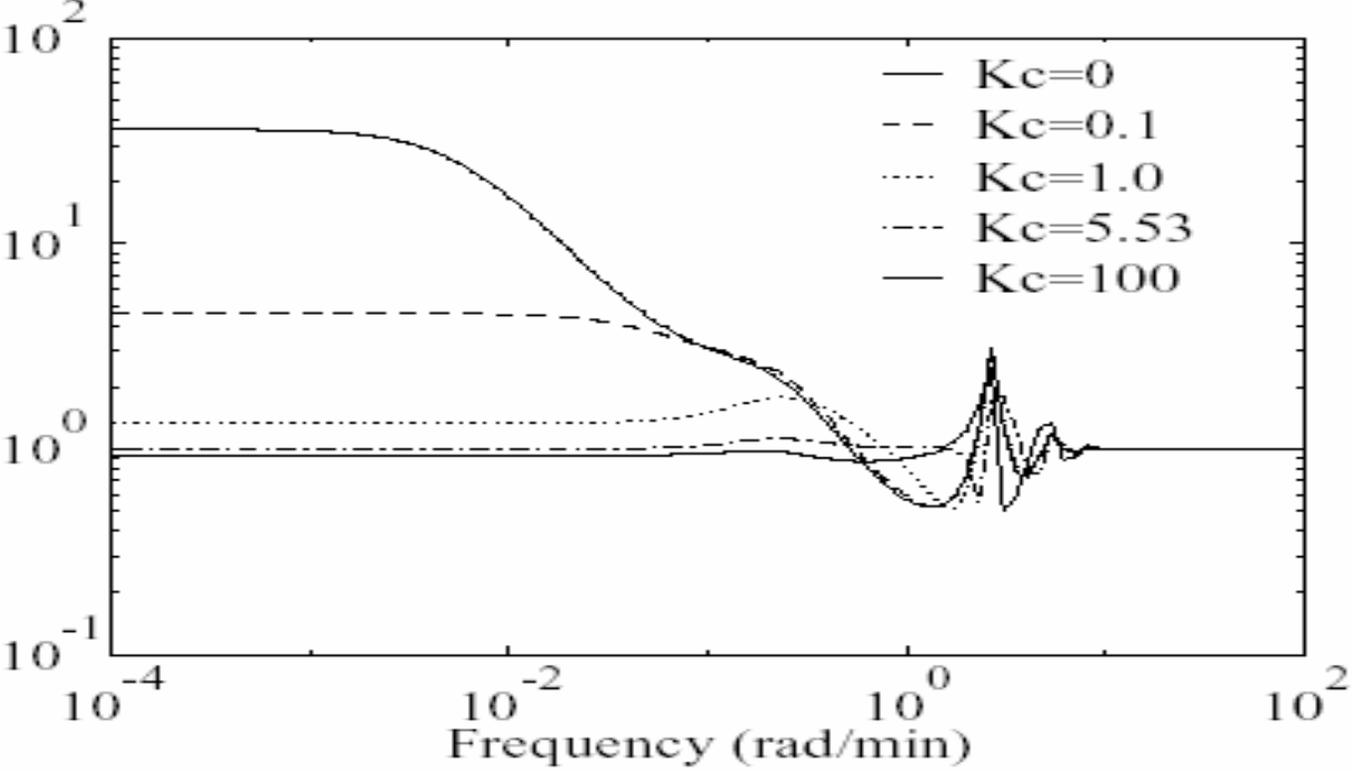


Setpoint T:  
New “handle”  
instead of L

# Bonus 2 of temp. control: Less interactive



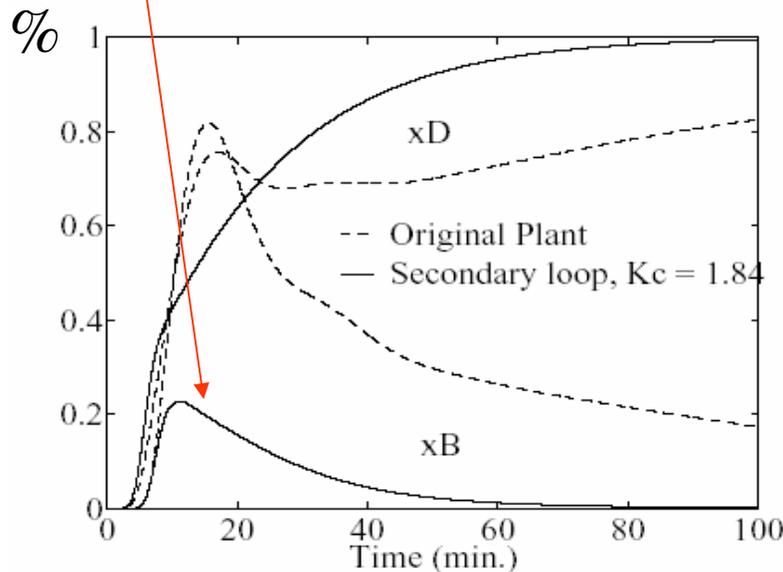
Less interactive:  
 RGA with temperature loop closed



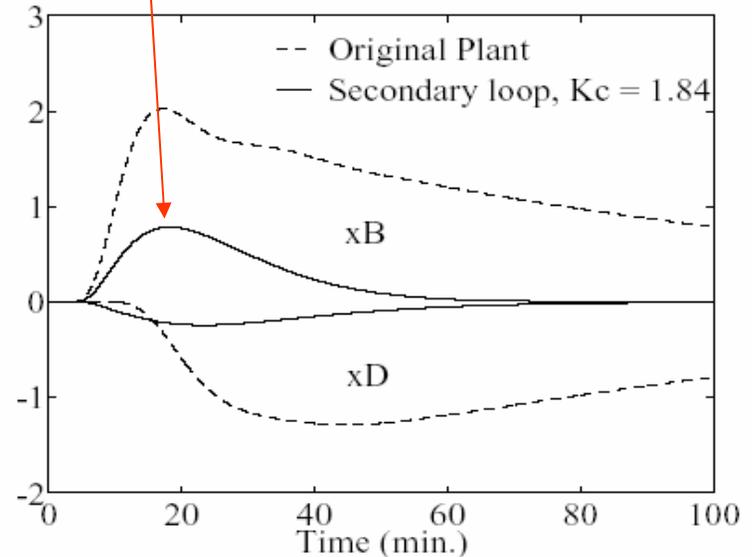
# Less interactive: Closed-loop response with decentralized PID-composition control

Interactions much smaller with “stabilizing” temperature loop closed

... and also disturbance sensitivity is expected smaller



(a) Response to a setpoint change in distillate;  $\Delta x_D = 0.01$  (scaled to 1).



(b) Response to a 50% step change in feed rate.

Figure 4.9: Time simulations with composition loops closed.

# Integral action in temperature loop has little effect

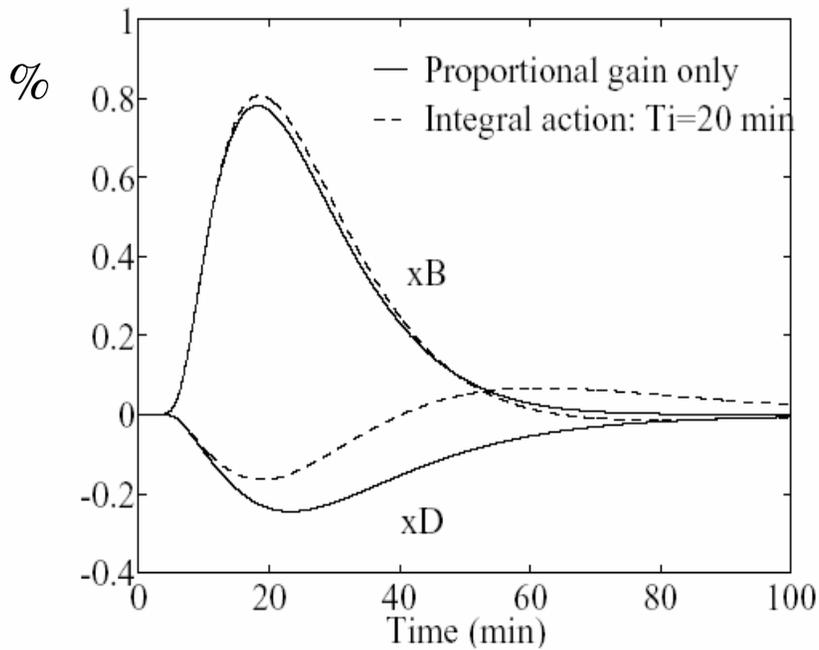
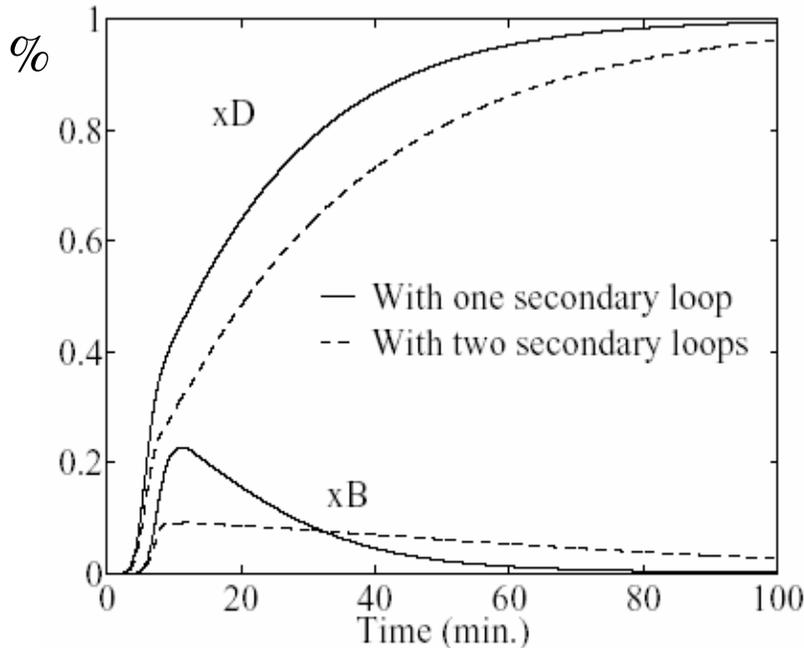
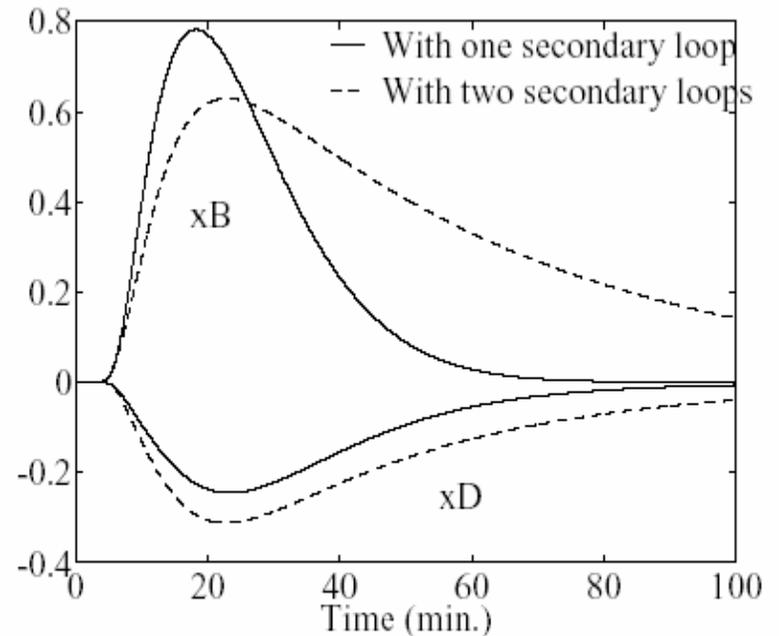


Figure 4.11: Response to a 50% step change in feed rate  $F$  with and without integral action in the secondary loop.

# No need to close two inner temperature loops



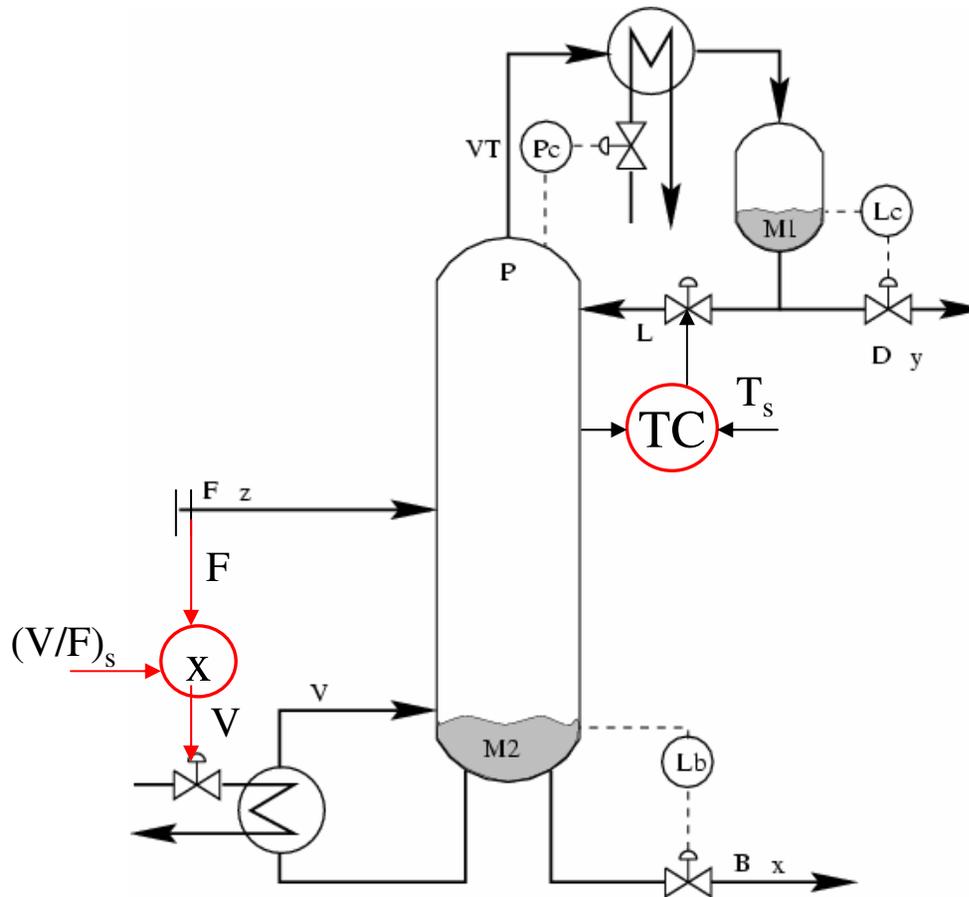
(a) Response to a setpoint change in distillate;  $\Delta x_D = 0.01$ .



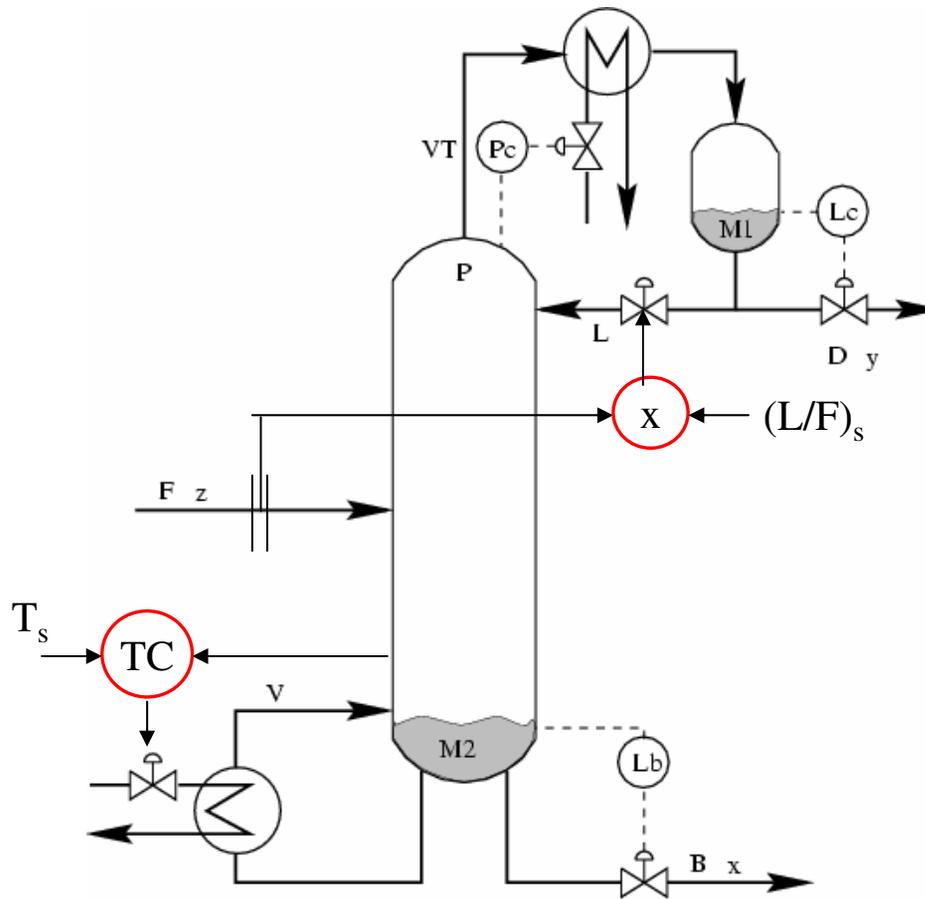
(b) Response to a 50% step change in feed rate.

Would be even better with V/F

Would be even better with V/F:



# A “winner”: L/F-T-congruration



Only caution: V should not saturate

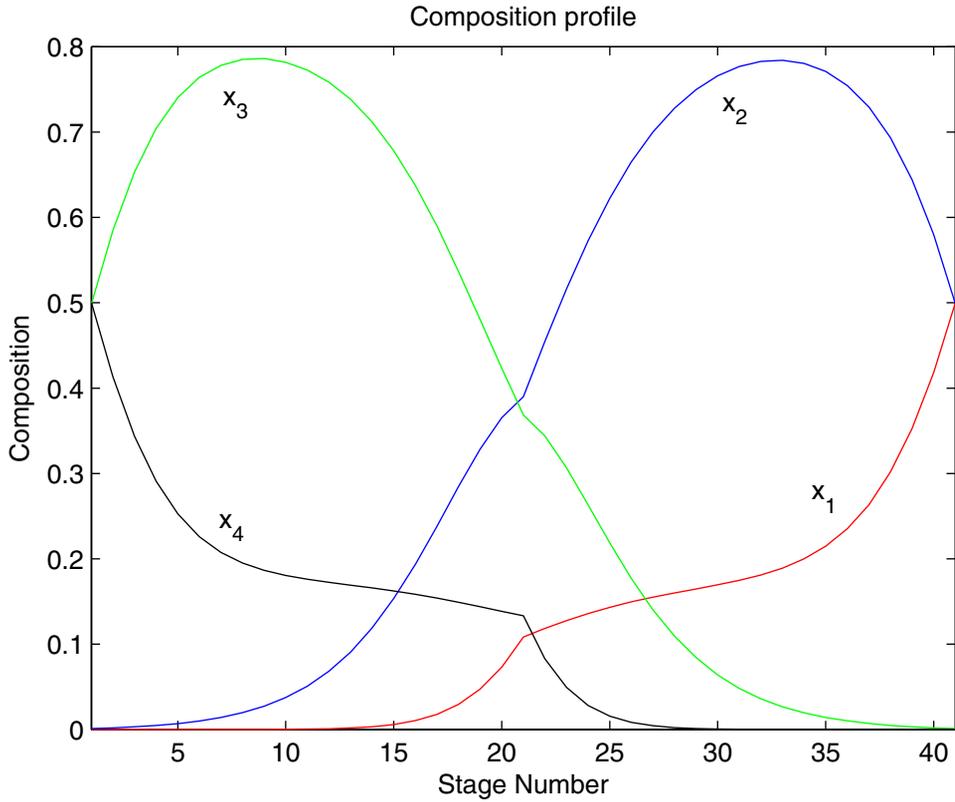
$$J = (x_D - x_{Ds})^2 + (x_B - x_{Bs})^2$$

Table 1: Losses of several possible configurations for binary mixture.

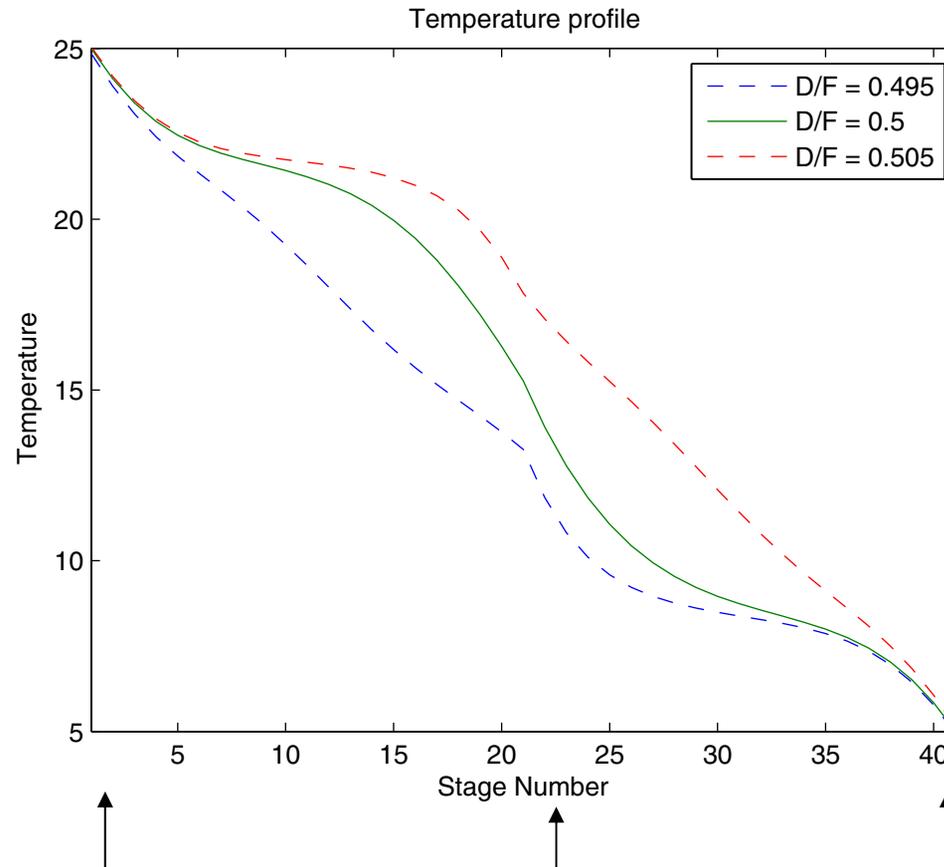
Configuration	Exact loss ( $\times 10^{-6}$ )	Configuration	Exact loss ( $\times 10^{-6}$ )
T <sub>12</sub> - T <sub>30</sub>	28	L - B	44300
T <sub>15</sub> - L/F	83	D - V	45000
T <sub>16</sub> - V/F	131	L/D - V	53400
T <sub>19</sub> - L	149	T <sub>40</sub> - B/F	62800
T <sub>15</sub> - L/D	174	T <sub>40</sub> - D/F	62800
T <sub>22</sub> - V	216	T <sub>40</sub> - B	89200
T <sub>24</sub> - V/B	292	T <sub>40</sub> - D	89200
L/D - V/B	25100	L - V	402200
L/F - V/B	34600	L/F - V/F	810600



# Multicomponent: Composition profiles



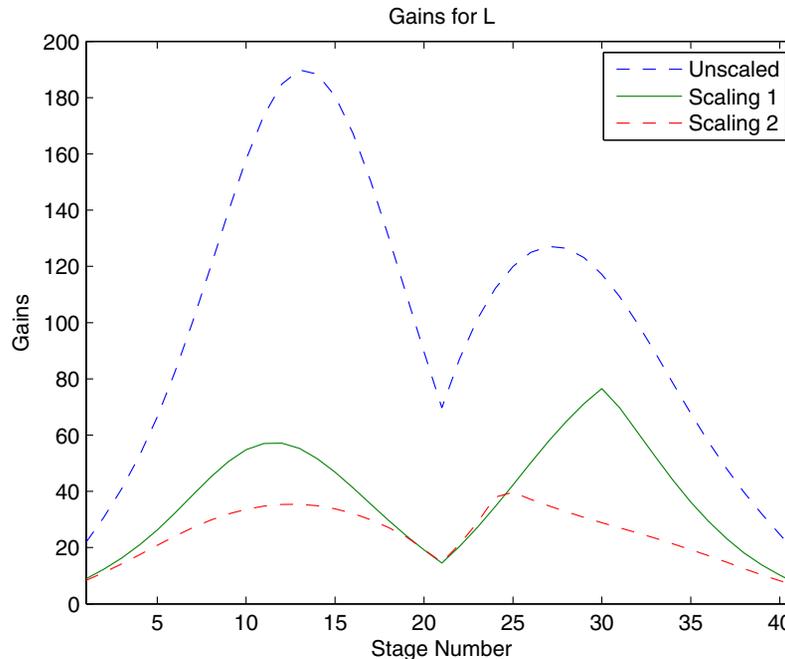
# Multicomponent: Temperature profile



Profile steepest in middle and at column ends (!??)

## Multicomponent distillation

$$\text{Scaled gain} = \frac{\text{Gain}}{\text{span}} = \frac{(\text{unscaled})\text{Gain}}{\text{noise} + \text{opt. variation}}$$



Conclusion: Control temperature in middle of sections

- Almost same as for binary
- Very different from slope of temperature profile (initial response):

# Conclusion: Stabilizing control distillation

- Control problem as seen from layer above becomes much simpler if we control a sensitive temperature inside the column ( $y_2 = T$ )
- Stabilizing control distillation
  1. Condenser level
  2. Reboiler level
  3. Pressure (sometimes left “floating” for optimality)
  4. Column temperature
- Most common pairing:
  - “LV”-configuration for levels
  - Cooling for pressure
  - (a) L for T-control (if V may saturate; or top composition important)
  - (b) V for T-control (if delay from L to T; or btm composition important)

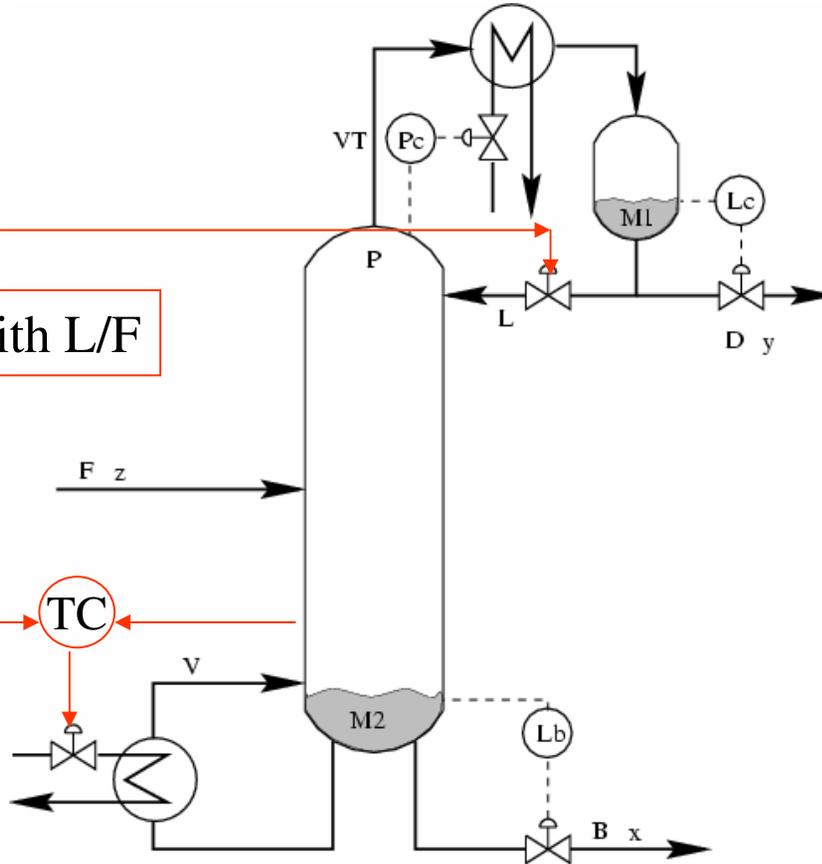
# Conclusion stabilizing control: Remaining supervisory control problem

$L_s$

Would be even better with L/F

$T_s$

With V for T-control



+ may adjust setpoints for p,  $M_1$  and  $M_2$  (MPC)